

#### **Probing TeV Scale** Left-Right Seesaw

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## Where does neutrino mass come from ?

For charged fermions, mass comes from the Higgs vev

$$m_f = h_f v_{wk} \quad v_{wk} = < h^0 >$$

The provide the the the the test of test

= For neutrinos, this formula gives too large a mass- requires  $h_{\nu} \sim 10^{-12}$ !!

= There is a second mass problem !!

## Weinberg Effective operator as a clue

 $\rightarrow$ 

• Weinberg effective operator:  $\lambda \frac{LHLH}{M}$ 

$$m_{\nu} = \lambda \frac{v_{wk}^2}{M}$$

 λ ~ 1; M big → m<sub>ν</sub> ≪ m<sub>f</sub> naturally !
 What is the Physics of M?
 To explore this, seek UV completion of Weinberg operator → SeesaW → M-physics

#### **Type I SEESAW**

 UV completion by adding SM singlet heavy Majorana neutrinos N to SM



(Minkowski'77; Gell-Mann, Ramond, Slansky; Yanagida; Glashow; Mohapatra, Senjanovic'79)

#### Questions raised by seesaw

- Where did N come from ?
- Where did the seesaw scale come from ?

- Two theories that provide answers to these questions very economically are:
  - (i) Left-right model where N is the parity partner
    - of  $\mathcal{V}$  and seesaw scale is SU(2)<sub>R</sub> scale !!
  - (ii) <u>SO(10) GUT</u> where N+15 SM fermions =16 spinor

and seesaw scale = GUT scale.

## Seesaw scale and testing seesaw experimentally

(ii) GUT embedding e.g. SO(10)  $\rightarrow$  very natural since  $h_{\nu} \sim h_q$  due to q-l unif. but since , M<sub>R</sub> ~10<sup>14</sup> GeV: very hard to test!!

(ii) Left-right can have  $M_R$  TeV scale: many tests ! However, even here, Generic theory  $\rightarrow h_{\nu} \leq 10^{-5.5}$ Leaves out a lot of seesaw parameter space e.g. theories with larger  $h_{\nu} \sim 0.1 - 0.01$  would allow access to it ! Are there such theories ?

#### **Testing TeV seesaw**

Neutrino Matrix:

$$\mathcal{M}_{
u} = egin{pmatrix} & ( m{
u} & N \ ) \ & m_D \ & m_D \ & M_N \end{pmatrix}$$

$$m_D = h_\nu v_{wk}$$

• Two ways: (i) Majorana mass  $M_N$  (breaks L):

(ii)  $\nu - N$  mixing:  $V_{\ell N} = \frac{h_{\nu} v_{wk}}{M_N}$ 

#### Two points of the talk:

• Are there <u>natural</u> models which have  $h_{\nu} \sim .01$ yet have both tiny  $m_{\nu} \sim .1 \ eV$  so that  $V_{\ell N}$  is large i.e. Allows excess to a larger part of seesaw parameter space !

What are the tell-tale experimental signatures of such a scenario ?

A Strategy for large 
$$V_{\ell N}$$
  
with TeV  $M_N$   
 $m_D = \begin{pmatrix} m_1 & \delta_1 & \epsilon_1 \\ m_2 & \delta_2 & \epsilon_2 \\ m_3 & \delta_3 & \epsilon_3 \end{pmatrix} \qquad M_N = \begin{pmatrix} 0 & M_1 & 0 \\ M_1 & M_2 & 0 \\ 0 & 0 & M_3 \end{pmatrix}$   
(Kersten, Smirnov'07)

Note if  $\epsilon_i, \delta_i, M_2 = 0 \rightarrow m_{\nu_i} = 0$  (sym lim.)
sym. Br.  $\delta_i, \epsilon_i \ll m_i; M_2 \ll M_{1,3}$ Seesaw  $\rightarrow m_{\nu} \sim \frac{m_i m_j M_2}{M_1^2} + \frac{\epsilon_i \epsilon_j}{M_1} << m_{e,q}$ 

For  $m_{i,j} \sim 1-10$  GeV,  $M_{1,3} > 100$  GeV,  $\rightarrow V_{\ell N} < .1-.01$ (other ex.: Pilaftsis, Underwood'05; Soni, Kiers..'06; Haba, Mimura ..'11; He et al'09; Mitra et al.'11)

### Left-Right Model embedding • LR basics: Gauge group: $SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$

# Fermions $\begin{pmatrix} u_L \\ d_L \end{pmatrix} \stackrel{P}{\Leftrightarrow} \begin{pmatrix} u_R \\ d_R \end{pmatrix} \begin{pmatrix} v_L \\ e_L \end{pmatrix} \stackrel{P}{\Leftrightarrow} \begin{pmatrix} v_R \\ e_R \end{pmatrix}$

$$L = \frac{g}{2} [\vec{J}_{L}^{\ \mu} \cdot \vec{W}_{\mu L} + \vec{J}_{R}^{\ \mu} \cdot \vec{W}_{\mu R}]$$

 $M_{W_B} \gg M_{W_L}$ 

 Parity a spontaneously broken symmetry:

#### Scalar sector and seesaw

 $\Delta = \begin{pmatrix} \frac{1}{\sqrt{2}} \Delta^{+} & \Delta^{++} \\ \Delta^{0} & -\frac{1}{\sqrt{2}} \Delta^{+} \end{pmatrix}$ 

■ 
$$SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_Y$$
 by

(Mohapatra and Senjanovic; Minkowski)

Vev: 
$$\langle \Delta \rangle = \begin{pmatrix} 0 & 0 \\ \nu_R & 0 \end{pmatrix} \Rightarrow M_N = f \nu_R$$
  
• SM Higgs is in:  $\phi = \begin{pmatrix} \phi_1^0 & \phi_2^+ \\ \phi_1^- & \phi_2^0 \end{pmatrix} \quad \phi = \begin{pmatrix} \kappa & 0 \\ 0 & \kappa' \end{pmatrix}$ 

Leads to seesaw matrix:

#### Parity breaking and neutrino mass

Seesaw formula from parity breaking:

$$M_{\nu,N} = \begin{pmatrix} 0 & h\kappa \\ h\kappa & fv_R \end{pmatrix} \rightarrow m_{\nu} \simeq -\frac{(h\kappa)^2}{fv_R}$$
$$M_{W_R} = gv_R$$

Generic version (I) needs  $h \le 10^{-5.5}$  and small  $V_{\ell N}$   $M_{W_R} \ge 2.9 TeV$  (CMS, ATLAS)

$$\begin{array}{l} \text{Realistic LR embedding of} \\ \text{enhanced } V_{\ell N} \quad (\text{II}) \\ \text{II} \\ \text{New model based on } \text{SU}(2)_{L} \text{xSU}(2)_{R} \text{xU}(1)_{B-L} \text{x}(Z_{4})^{3} \\ \mathcal{L}_{Y}^{\ell} &= h_{\alpha 1} \bar{L}_{\alpha} \tilde{\phi}_{1} R_{1} + h_{\alpha 2} \bar{L}_{\alpha} \phi_{3} R_{2} + h_{\alpha 3} \bar{L}_{\alpha} \phi_{2} R_{3} + \\ f_{12} R_{1} R_{2} \Delta_{R,1} + f_{33} R_{3} A_{3} \Delta_{R,2} + h.c. \\ \text{Sym lim.} &< \phi_{a} >= \begin{pmatrix} 0 & 0 \\ 0 & \kappa_{a} \end{pmatrix} \quad ; < \Delta_{R,i}^{0} >= v_{R,i} \\ M_{\ell} &= \begin{pmatrix} 0 & h_{12} \kappa_{3} & h_{13} \kappa_{2} \\ 0 & h_{22} \kappa_{3} & h_{23} \kappa_{2} \\ 0 & h_{32} \kappa_{3} & h_{33} \kappa_{2} \end{pmatrix} \quad \Rightarrow \text{m}_{e=0} ; \quad m_{\nu_{i}} = 0 \\ M_{D} &= \begin{pmatrix} h_{11} \kappa_{1} & 0 & 0 \\ h_{21} \kappa_{1} & 0 & 0 \\ h_{31} \kappa_{1} & 0 & 0 \end{pmatrix} M_{R} = \begin{pmatrix} 0 & M_{1} & 0 \\ M_{1} & 0 & 0 \\ 0 & 0 & M_{2} \end{pmatrix} \quad (\text{Lee,Dev, RNM'13)} \end{array}$$

**Realistic LR embedding of** enhanced  $V_{\ell N}$  (II) Break Discrete sym.  $<\phi_i>=\begin{pmatrix} \delta_i & 0\\ 0 & \kappa_i \end{pmatrix}$ with  $\delta_i \ll \kappa_i$  by sym. Leads naturally to  $m_D = \begin{pmatrix} m_1 & \delta_1 & \epsilon_1 \\ m_2 & \delta_2 & \epsilon_2 \\ m_2 & \delta_2 & \epsilon_2 \end{pmatrix} M_R = \begin{pmatrix} 0 & M_1 & o \\ M_1 & \delta M & 0 \\ 0 & 0 & M_2 \end{pmatrix} \qquad \delta_i, \epsilon_i \ll m_i$ 

$$\rightarrow m_e \neq 0; m_{\nu_{ij}} \sim \frac{\delta_i \epsilon_j}{M_i}, \frac{\delta_i \delta_j}{M_i}, \frac{\epsilon_i \epsilon_j}{M_i} \sim eV$$

#### Model as theory of leptons: Inputs and outputs

Model has 12 parameters:

• Outputs: 3 charged lepton masses, 3 nu masses, 3 mixing angles+must satisfy unitarity constraints on 9  $V_{\ell_i N_j} + V_{e_R 12}$  which enters into  $\mu \to 3e$ 

Hence predictive and testable !!

### NEUTRINO FITS AND ENHANCED $V_{\ell N}$ -typical soln.

 $M_D = \begin{bmatrix} 2.42239 & 2.23962 \times 10^{-10} & -0.000108617 \\ -1.81165 & 1.46738 \times 10^{-9} & 4.54245 \times 10^{-7} \\ -13.6056 & 6.21681 \times 10^{-10} & 0.000161672 \end{bmatrix} \quad \mathsf{M}_{\mathsf{e}} = \begin{bmatrix} 0.000266007 & 0.0151488 & -0.98912 \\ -0.000198941 & 0.0992534 & 0.00413658 \\ -0.00149406 & 0.0420506 & 1.47226 \end{bmatrix}$ 

$$M_{R} = \begin{bmatrix} 0 & 813.254 & 0 \\ 813.254 & 1.29732 \times 10^{-9} & 0 \\ 0 & 0 & -2488.96 \end{bmatrix}$$
  
$$V_{\text{PMNS (fit)}} = V_{e}^{\text{T}} V_{v} = \begin{pmatrix} 0.819226 & -0.553122 & 0.151304 \\ 0.35545 & 0.696887 & 0.622884 \\ -0.450027 & -0.456456 & 0.767386 \end{pmatrix}$$



(Lee, Dev, RNM'13)



#### Testing in Colliders: SM Seesaw

• Signal of SM seesaw:  $\ell^{\pm}\ell^{\pm}jj$  "Golden channel"

$$i^{q}$$
  $V_{\ell N}^{W^+}$   $V_{\ell N}^{\ell^+}$   $X$   $|V_{\ell N}|^2$ 

- Signal strength depends on how big  $V_{\ell N}$  is:
- $V_{\ell N}$  typically tiny;
- Even if it is big, less effective for M<sub>N</sub> > 200 GeV (del Aguila, Aguilar Saavedra)

## Situation changes with LR seesaw:

- New contribution via WR production:  $u\bar{d} \rightarrow W_R \rightarrow l^+ N$
- Subsequent N-decay via (a) N mixing and/or
   (b) W exchange
- Generic type I • Dominant graph(b) (RR diagram) •  $\frac{Generic type I}{P_{VN}} = \frac{P_{VN} <<10^{-3}, M_{W_R} < 4TeV}{P_{VN}}$  (a) negligible;  $\frac{P_{VN} <<10^{-3}, M_{W_R} < 4TeV}{P_{VN}}$  (b)  $\frac{P_{VN} <<10^{-3}, M_{W_R} < 4TeV}{P_{VN}}$  (c) negligible;  $\frac{P_{VN} <>10^{-3}, M_{W_R} < 4TeV}{P_{VN}}$  (c) negligible; (c) neg
- Same signal: valid for  $M_N >> 200$  GeV.

### **Current LHC analysis: only W<sub>R</sub> graph but not large V<sub>\ellN</sub>**

#### Current limits from CMS, ATLAS 2.5-2.9 TeV;



**Theory papers:** Datta, Guchait, Roy; A.Ferrari et al., S. N. Gninenko, M. M. Kirsanov, N. V. Krasnikov and V. A. Matveev, A.Maiezza, M.Nemevsek, F.Nesti and G.Senjanovic, Y.Zhang; V.Tello, M.Nemevsek, F.Nesti, G.Senjanovic and F.Vissani; J.Chakrabortty, J.Gluza, R.Sevillano and R.Szafron; P.Das, F.F.Deppisch, O.Kittel and J.W.F.Valle; T. Han, I. Lewis, R. Ruiz, Z. Si; Joaquim, Aguilar-Saavedra;

#### 14-TeV LHC reach for M<sub>WR</sub> 6 TeV with 300 fb<sup>-1</sup>

**New graph for golden channel with "large"**  $V_{\ell N}$  $V_{\ell N} \sim 0.01 - 0.001$  can be probed:

 New graphs can dominate WR signal (Chen, Dev, RNM' arXiv: 1306.2342- PRD)



$$q\bar{q} \to W_R \to \ell + N;$$
  
 $N \to \ell W_L$ 

(RL diagram)

Flavor dependence will probe Dirac mass M<sub>D</sub> profile:

## Domains where mixing dominates over RR

#### Phase diagram:



Relative signal strength: RR vs RL: (mu channel)

#### **Distinguishing RR from RL**

Dilepton invariant mass plots:



(Han, Lewis, Ruiz, Si)

#### **CLFV in left-right seesaw**

New contribution to CLFV for generic seesaw from in LRSM(I) (Riazuddin, Marshak, RNM'81; Cirigliano, Kurylov, Musolf, Vogel'04)

$$B(\mu \to e\gamma) = \frac{3\alpha}{32\pi} \left(\frac{m_{W_L}^2}{m_{W_R}^2}\right)^4 \left(\sin\theta'\cos\theta' \frac{m_{N_2}^2 - m_{N_1}^2}{m_{W_L}^2}\right)^2 < 10^{-14}$$

$$B(\mu^{-} \to e^{-}) = 10^{-6} \epsilon^{2} \sin^{2} \theta' \cos^{2} \theta' < 10^{-12}$$
(M<sub>2</sub>=100 GeV)
$$\epsilon = \frac{m_{2}^{2} - m_{1}^{2}}{\sin^{2} \theta_{W} m_{W_{L}}^{2}} \left(\frac{m_{W_{L}}^{2}}{m_{W_{R}}^{2}}\right)^{2} \left(\ln \frac{m_{W_{R}}^{2}}{M^{2}} - 2\right)$$

 $\rightarrow$  Can probe W<sub>R</sub> and M<sub>N</sub> to 10-30 TeV scale !!



Testable in the current round

Testable next round e.g. PJX

#### **Scalar spectrum**

- (i) New Higgs fields:  $\Delta^{++}, \Delta^{+}, \Delta^{0}$
- They track the seesaw profile and N spectrum:
- Decays  $f_{\alpha\beta}\ell_{\alpha}\ell_{\beta}\Delta^{++}$
- Have new effects on  $\mu 
  ightarrow 3e \propto f_{ee} f_{e\mu}$

$$\beta \beta_{0\nu} \propto f_{ee} \frac{v_R}{M_\Delta^2 M_{W_R}^4}$$

(ii) Sub-TeV lepto-philic SM like Higgs tests

(iii) Analog of SM Higgs:  $S \equiv Re(\Delta_R^0)$ 

#### LHC limits

### Pair production: cross section ~ fb at 350 GeV mass $pp \rightarrow \Delta^{++}\Delta^{--}$



Flavor dependent result assuming 100%  $\Delta^{++} \rightarrow \ell^+ \ell^+$  decay

### Why sub-TeV leptophilic SM-Like Higgs ?

- $[Z_4]^3$  family sym for leptons allows only terms in Higgs potential of form:  $\lambda_a Tr[\phi_a^{\dagger}\tilde{\phi}_a\phi_a^{\dagger}\tilde{\phi}_a]$
- As  $\lambda_a \to 0$ , Z<sub>4</sub> gets promoted to U(1)<sub>a</sub> so that EWSB leads to Goldstone states. Their masses are therefore of order  $\lambda_a \kappa_a^2$  and hence sub-TeV.
- They couple only to leptons- hence lepto-philic !!
   LHC:  $\sigma(pp \to Z^* \to AH) \sim 50 \ fb$  (Aoki, Kanemura, Tsumura, Yagyu)  $4\tau, 4\mu$  final states

#### **Conclusion:**

- Seesaw: Compelling big picture for nu masses; A new Left-right model provides a natural TeV scale UV completion of seesaw with "large"  $V_{\ell N}$  !
- LHC could probe both Majorana mass as well as non-generic m<sub>D</sub> via l<sup>+</sup>l<sup>+</sup>jj mode.
   --Has 2 components: RR and RL due to V<sub>lN</sub>; can be separated allowing a test of such models !!
- The set of models we predict  $\mu \to e + \gamma~$  and  $\mu + N \to e + N~$  slightly below the current limits
- Sub-TeV SM like leptophilic Higgs states.



#### Extra slides

#### New Higgs Effects in LR seesaw

(i) Extra Higgs doublet:  $M_{H}$  in multi-TeV range. (ii) Triplet Higgs:  $\Delta = \begin{pmatrix} \delta^{+}/\sqrt{2} & \delta^{++} \\ \delta^{0} & -\delta^{+}/\sqrt{2} \end{pmatrix}_{L,R}$ 

 $\delta^{++}$  in  $\beta\beta_{0\nu}$  decay: (RNM, Vergados'81; piccioto, Zahir'82; INemesvek, Nesti, Senjanovic, Tello, Vissani'12; Goswami et al;12; Awasthi, Parida, Patra'12; Barry, Rodejohann'12)

$$\frac{M_N}{M_{\delta^{++}}^2} \leq 10^{-2} ~\rm{GeV}~^{-1}$$
 (for  $\rm{M_{WR}}$  =3 TeV)



#### **Future Sensitivities**

#### Experiment

No.	Observable	Upper Limit	Future Sensitivity
1.	$B(\mu  ightarrow e \gamma)$	$2.4  imes 10^{-12}$ [1]	$1-2 imes 10^{-13}$ [6], $10^{-14}$ [6]
2.	$B(\mu  ightarrow eee)$	$10^{-12}$ [2]	$10^{-16}$ [8], $10^{-17}$ [7]
3.	$R_{\mu e}^{ m Ti}$	$4.3  imes 10^{-12}$ [3],	$3-7 imes 10^{-17}$ [10, 9], $10^{-18}$ [11, 7]
4.	$R^{ m Au}_{\mu e}$	$7  imes 10^{-13}$ [4]	$3-7 imes 10^{-17}$ [10, 9], $10^{-18}$ [11, 7]
5.	$B( au  o e \gamma)$	$3.3  imes 10^{-8}$ [5]	$1-2 imes 10^{-9} \; [13,12]$
6.	$B( au  o \mu \gamma)$	$4.4  imes 10^{-8}$ [5]	$2 imes 10^{-9} \; [13,12]$
7.	B( au  ightarrow eee)	$2.7  imes 10^{-8}$ [5]	$2 imes 10^{-10} \ [13,12]$
8.	$B( au  ightarrow e \mu \mu)$	$2.7  imes 10^{-8}$ [5]	$10^{-10}$ [12]
9.	$B( au  o \mu \mu \mu)$	$2.1  imes 10^{-8}$ [5]	$2 imes 10^{-10} \; [13,12]$
10.	$B( au  ightarrow \mu ee)$	$1.8  imes 10^{-8}$ [5]	$10^{-10}$ [12]

Table 1: Current upper limits and future sensitivities of CLFV observables under study.

#### **BEYOND LEFT-RIGHT: QUARK-LEPTON UNIF.**

- If Q-L unified at the seesaw scale, a model is  $SU(2)_L \times SU(2)_R \times SU(4)_c \begin{pmatrix} u & u & u & \nu \\ d & d & d & e \end{pmatrix}_{L,R}$
- →SU(4) generalization of the seesaw Higgs field  $\Delta_R$  has partners  $\Delta_{qq}$  connecting to quarks:
- →leads to neutron-anti-neutron oscillation: (Mohapatra, Marshak'80)
- $\rightarrow$ No proton decay.
- -Example of nu mass-NNbar connection



observable for TeV sextets

#### **Baryogenesis constraints**

- If NN-bar is observable, it will erase all pre-existing baryon asymmetry: need to generate baryons below weak scale:
- Baryogenesis via higher dim operators: Post-sphaleron baryogenesis (Babu, Nasri, RNM'07) 0.06upper bound on Nnbar 0.05 Probability 0.04 transition time  $< 5 \times 10^{10}$  sec. 0.03 0.02 (Babu, Dev, Fortes, RNM'arXiv:1303.6918) 0.01 0.00 10. 100  $\tau_{n-\bar{n}}/(10^8 \text{ sec})$ 
  - Predicts ~TeV color sextet fields for LHC.

### **CLFV that directly relates to neutrino Majorana mass**

- $\mu \to e\gamma, \mu \to 3e, \mu^- \to e^-$  conserve L and are not true tests of Majorana nu mass.
- However  $\mu^- \to e^+, \mu^- \to \mu^+$  are  $\Delta L \neq 0$  $B(\mu^- Ti \to e^+ Ca) \leq 3.6 \times 10^{-11}$
- Flavor analog of  $\beta\beta_{0\nu}$  decay
- Small in minimal type I
- Other related processes:  $K^+ \to \pi^- e^+ e^+, \pi^- e^+ \mu^+$

### $V_{\ell N}$ constraints from 125 GeV Higgs for >100 GeV M<sub>N</sub>

• 125 Higgs bound on  $V_{\ell N}$ 

 $\mathcal{L}_{h} = h_{\nu} \bar{\nu} Nh \rightarrow pp \rightarrow h \rightarrow \ell N$  LHC Higgs search final states  $\rightarrow e^{+} e^{-} E_{T}^{N \rightarrow W^{+} \ell^{-}, Z + \nu}$ 



## WR production cross section at LHC

Ginienko et al.



### LR Higgs induced CLFV : Generic case (I)

(V. Tello, Nemevsek, Nesti, Senjanovic, Vissani'12; Cirigliano, Kurylov, Ramsey-Musolf, Vogel'04)

(Tello,..)

5.00

• Loops involving  $\delta^{++}$  and  $\delta^+$ 

$$ightarrow \mu 
ightarrow e|_{Au}$$
 ,  $\mu 
ightarrow e\gamma$ 

$$B(\mu Au 
ightarrow eAu) \simeq 5 imes 10^{-10} \left(rac{3.5 {
m TeV}}{M_{W_R}}
ight)^4 \left|rac{M_N M_N^*}{m_\Delta^{++}}
ight|_{e\mu}^2$$

Bounds the mass ratio: $M_N/M_\Delta$ 



PSI Limit :  $< 3G_F 10^{\circ}$ 

Muonium-anti-muonium osc.
 Unique signature  $G_{M-\bar{M}} \sim \frac{f_{ee}f_{\mu\mu}}{8M^2}$ 



#### Maximally testable seesaw

- Has both  $M_N$  sub-TeV-TeV ;  $V_{\ell N}$  "large".

• Situation in generic models with  $M_N \sim TeV$ 

(i)  $m_{\nu} \simeq \frac{(h_{\nu}v_{wk})^2}{M_N} \sim .1 \text{ eV} \Rightarrow h_{\nu} \leq 10^{-5}$ (ii) Small  $h_{\nu} \Rightarrow V_{\ell N} = \frac{h_{\nu}v_{wk}}{M_N} \simeq \sqrt{\frac{m_{\nu}}{M_N}} \sim 10^{-6}$ 

#### Other tests of TeV WR: manifestation in $\beta\beta_{0\nu}$





• Nonzero signal for  $\beta \beta_{0\nu}$  + NH  $\rightarrow$  could be TeV WR

■ This model→contribution small !!