

# Higgs Physics at the ILC



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Scalars 2013  
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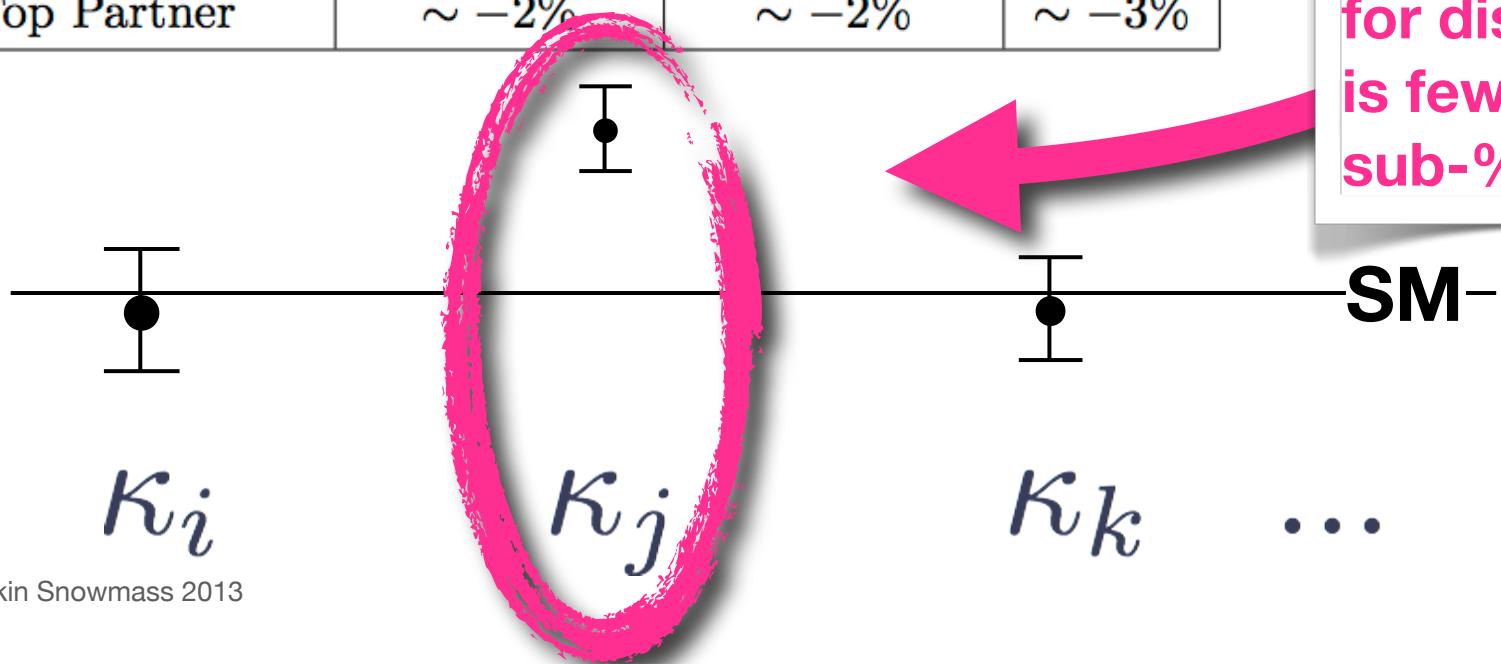
# Precision Higgs couplings at the ILC

Reference: *ILC Higgs White Paper*,  
by D. Asner, T. Barklow, H. Fujii, H.E. Haber,  
S. Kanemura, A. Miyamoto and G. Weiglein,  
contribution to the Snowmass 2013 Proceedings  
(to appear on the arXiV at the end of Sept. 2013)

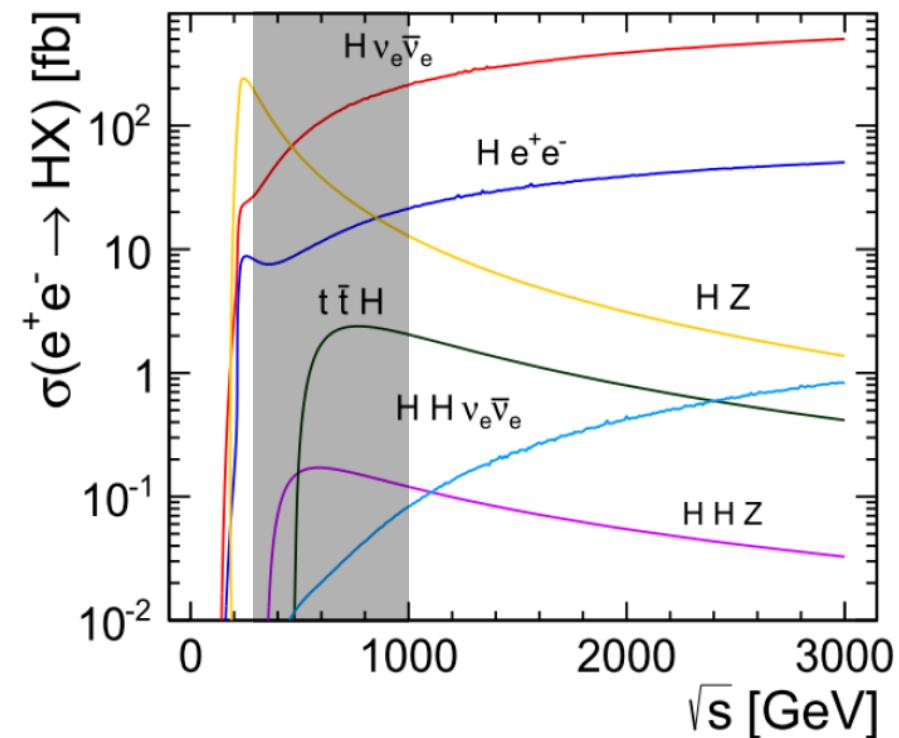
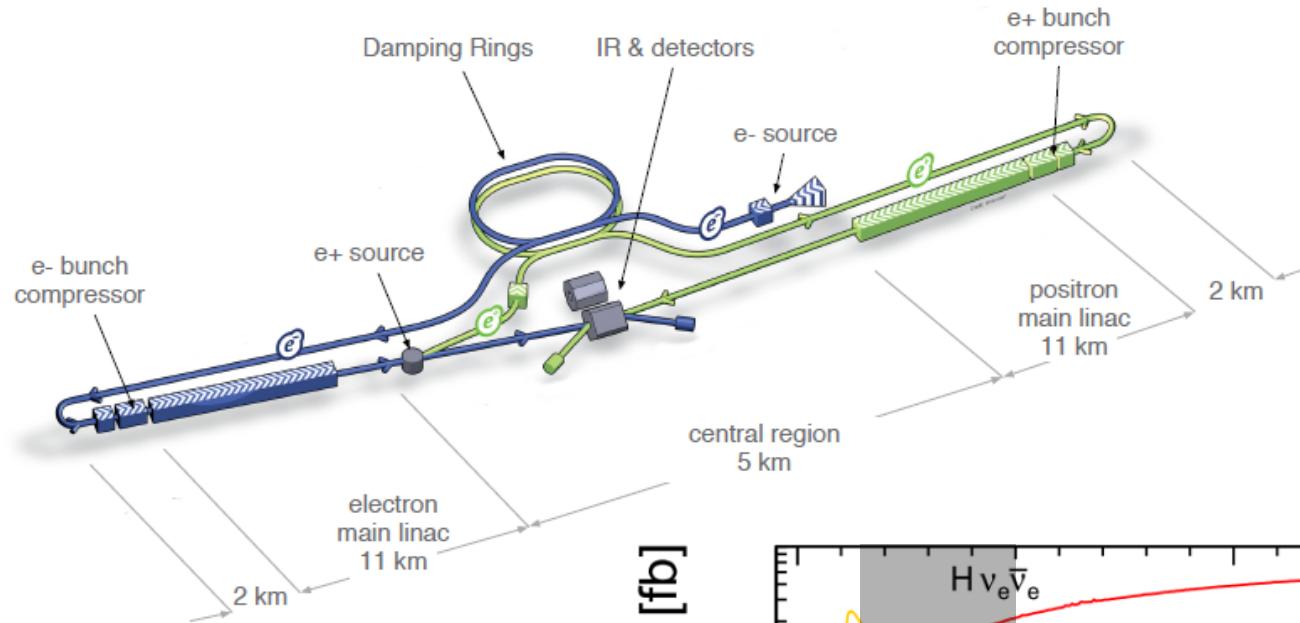
# precision for precision's sake?

No - this is a *discovery search*

	$\kappa_V$	$\kappa_b$	$\kappa_\gamma$
Singlet Mixing	$\sim 6\%$	$\sim 6\%$	$\sim 6\%$
2HDM	$\sim 1\%$	$\sim 10\%$	$\sim 1\%$
Decoupling MSSM	$\sim -0.0013\%$	$\sim 1.6\%$	$< 1.5\%$
Composite	$\sim -3\%$	$\sim -(3 - 9)\%$	$\sim -9\%$
Top Partner	$\sim -2\%$	$\sim -2\%$	$\sim -3\%$



# ILC: $e^+e^-$ Linear Collider at $250 \text{ GeV} < \sqrt{s} < 1000 \text{ GeV}$



# Energy/Luminosity running scenarios



Baseline Luminosity



Upgrade Luminosity

From the ILC Technical Design Report

Centre-of-mass energy	$E_{CM}$	GeV	Baseline 500 GeV Machine			250	500	L Upgrade		$E_{CM}$ Upgrade	
			250	350	500			A 1000	B 1000		
Collision rate	$f_{rep}$	Hz	5	5	5	5	5	4	4		
Electron linac rate	$f_{linac}$	Hz	10	5	5	10	5	4	4		
Number of bunches	$n_b$		1312	1312	1312	1312	2625	2450	2450		
Bunch population	$N$	$\times 10^{10}$	2.0	2.0	2.0	2.0	2.0	1.74	1.74		
Bunch separation	$\Delta t_b$	ns	554	554	554	554	366	366	366		
Pulse current	$I_{beam}$	mA	5.8	5.8	5.8	5.8	8.8	7.6	7.6		
Main linac average gradient	$G_a$	$MV\ m^{-1}$	14.7	21.4	31.5	31.5	31.5	38.2	39.2		
Average total beam power	$P_{beam}$	MW	5.9	7.3	10.5	5.9	21.0	27.2	27.2		
Estimated AC power	$P_{AC}$	MW	122	121	163	129	204	300	300		
Luminosity	$L$	$\times 10^{34}\ cm^{-2}s^{-1}$	0.75	1.0	1.8	0.75	3.6	3.6	4.9		

Luminosity (in units of  $10^{34}\ cm^{-2}\ s^{-1}$ )

CM Energy:	250 GeV	500 GeV	1000 GeV
Baseline design	0.75	1.8	3.6
Luminosity upgrade	3.0*	3.6	4.9

\*not in ILC TDR; high rep rate operation proposed by Marc Ross and Nick Walker

# Luminosity Upgrade at $E_{cm}=250$ GeV

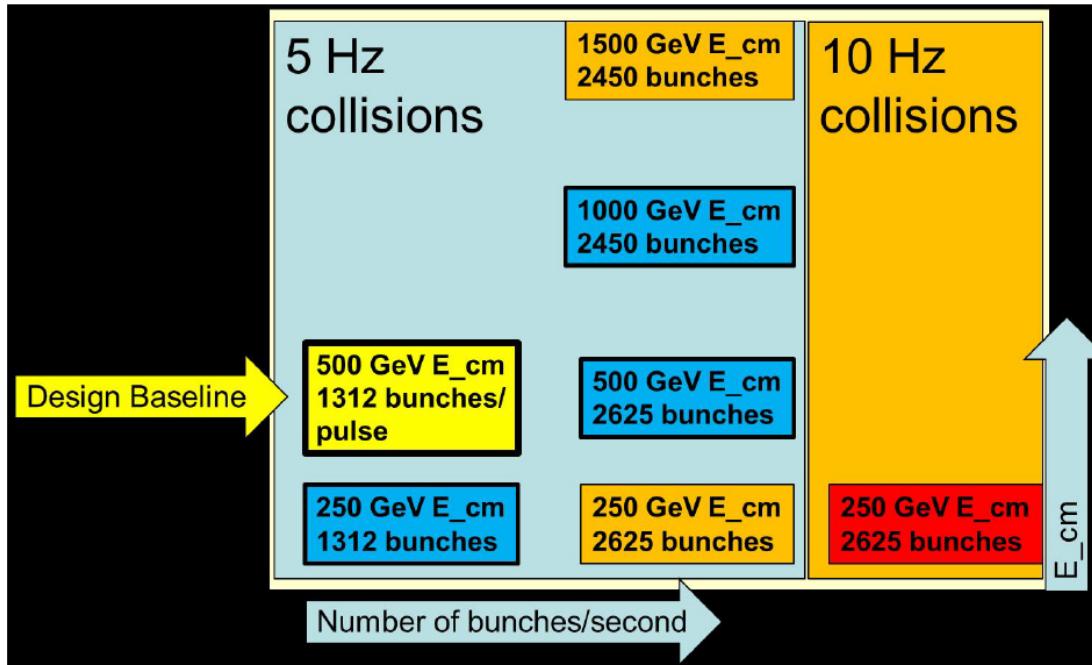


Table 1.2. ILC Higgs factory operational modes

			1st Stage Higgs Factory	Baseline ILC, after Lumi Upgrade	High Rep Rate Operation
Centre-of-mass energy	$E_{CM}$	GeV	250	250	250
Collision rate	$f_{rep}$	Hz	5	5	10
Electron linac rate	$f_{linac}$	Hz	10	10	10
Number of bunches	$n_b$		1312	2625	2625
Pulse current	$I_{beam}$	mA	5.8	8.75	8.75
Average total beam power	$P_{beam}$	MW	5.9	10.5	21
Estimated AC power	$P_{AC}$	MW	129	160	200
Luminosity	$L$	$\times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$	0.75	1.5	3.0

Baseline Luminosity

Upgrade Luminosity

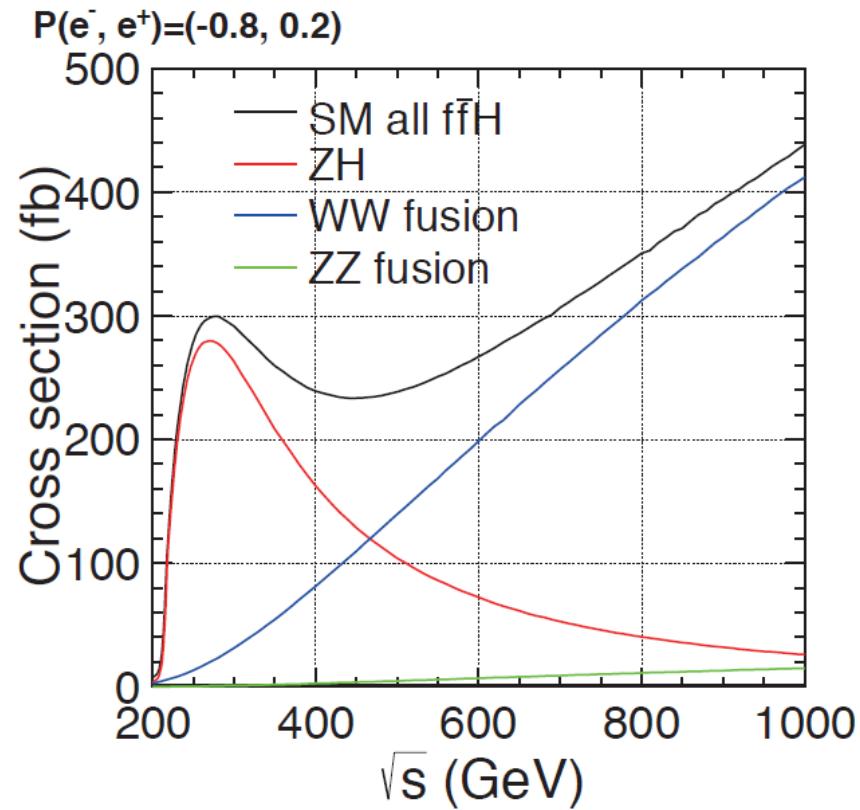
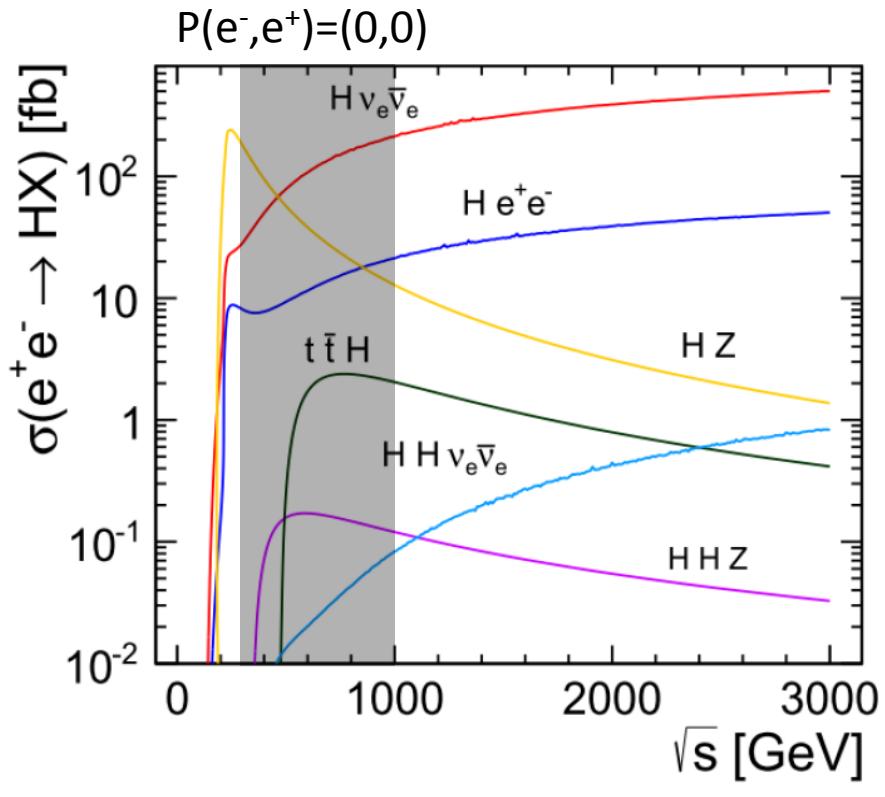
# Energy/Luminosity scenarios

Stage #	nickname	$E_{cm}(1)$ (GeV)	Lumi (1) (fb $^{-1}$ )	$E_{cm}(2)$ (GeV)	Lumi (2) (fb $^{-1}$ )	$E_{cm}(3)$ (GeV)	Lumi (3) (fb $^{-1}$ )	Runtime (years)
1	ILC (250)	250	250					1.1
2	ILC (500)	250	250	500	500			2.0
3	ILC (1000)	250	250	500	500	1000	1000	2.9
4	ILC(LumUp)	250	1150	500	1600	1000	2500	5.8

- At each stage, the *accumulated* luminosity of a given energy is listed. The runtimes listed consist of actual elapsed *cumulative* running time at the end of each stage. Assuming that the ILC runs for 1/3 of the time, then **the actual time elapsed is equal to the runtime times 3.**
- Assume that the ILC is run at its baseline luminosity at 250 GeV (stage 1), then at 500 GeV (stage 2), and finally at 1000 GeV (stage 3)
- Then, stage 4 repeats the successive stages 1, 2 and 3 at the upgraded luminosity.

In real time, this entire program would require  $5.8 \times 3 = 17.4$  years.

Beam polarization can increase the vector boson fusion cross section,  $W^+W^- \rightarrow H$ , by as much as a factor of two.



Simulations: Full simulations performed with ILD and/or SiD detector.

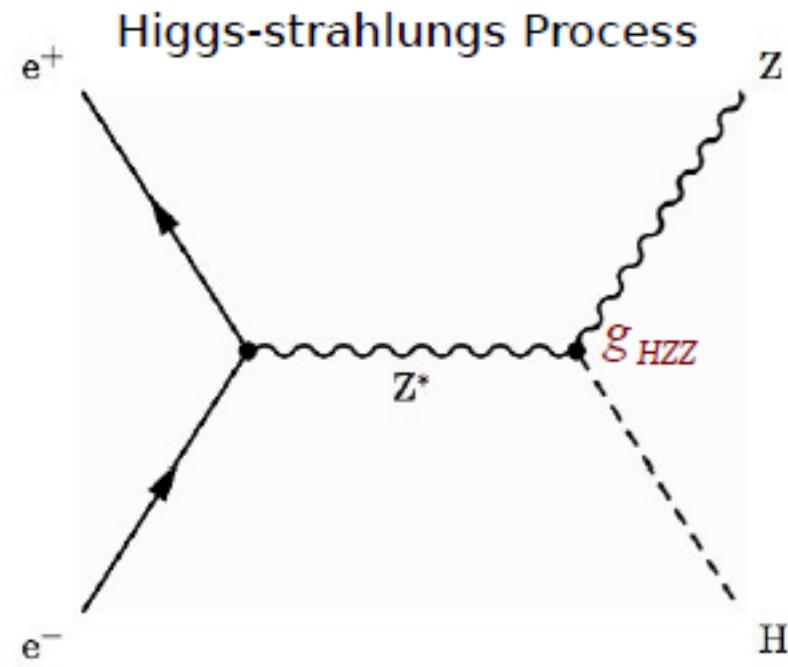
Systematic errors:

	Baseline	LumiUP
luminosity	0.1%	0.05%
polarization	0.1%	0.05%
b-tag efficiency	0.3%	0.15%

# What does the ILC actually experimentally measure?

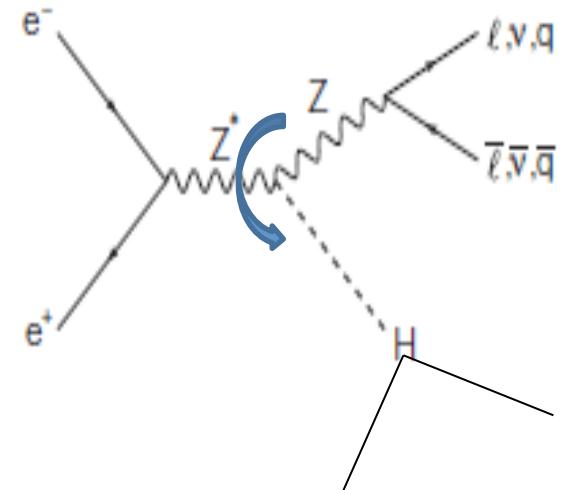
1.  $\sigma(e^+e^- \rightarrow ZH)$  at  $\sqrt{s} = 250$  GeV.

- The  $Z$  can be reconstructed in charged lepton and quark channels.
- The  $H$  can be “seen” in the mass spectrum recoiling against the  $Z$  (including the invisible Higgs decays).
- The  $H$  can be reconstructed in its main decay channels.



# Invisible Higgs Decay

- In the SM, an invisible Higgs decay is  $H \rightarrow ZZ^* \rightarrow 4\nu$  process and its BF is small ~0.1%
  - If we found sizable invisible Higgs decays, it is clear new physics signal.
    - The decay products are dark matter candidates.
  - At the LHC, one can search for invisible Higgs decays by using recoil mass from Z or summing up BFs of observed decay modes **with some assumptions**.
    - The upper limit is O(10%).
  - At the ILC, we can search for invisible Higgs decays using a recoil mass technique with **model independent way**!
    - $e^+e^- \rightarrow ZH$



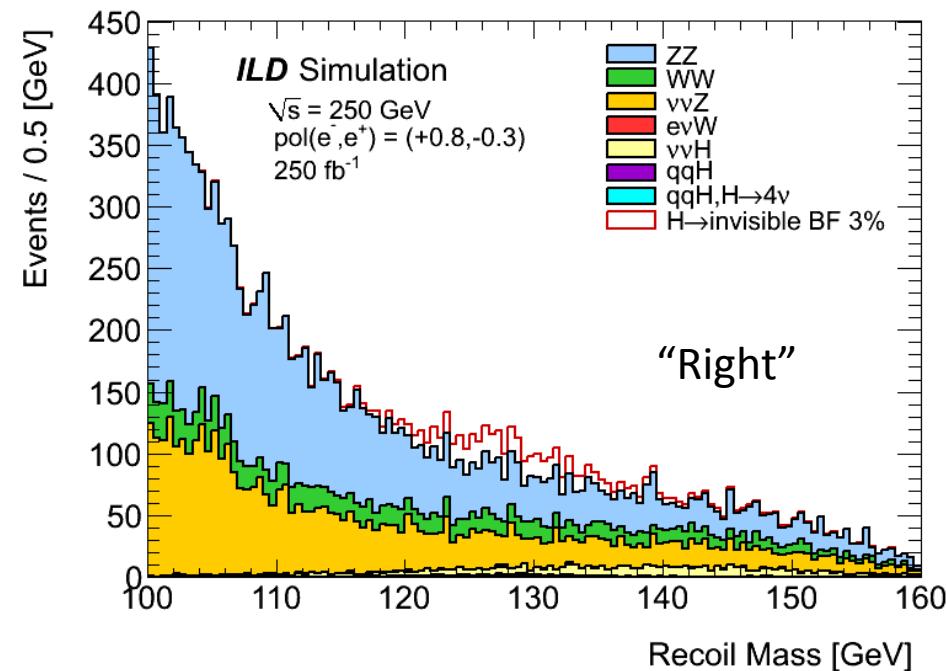
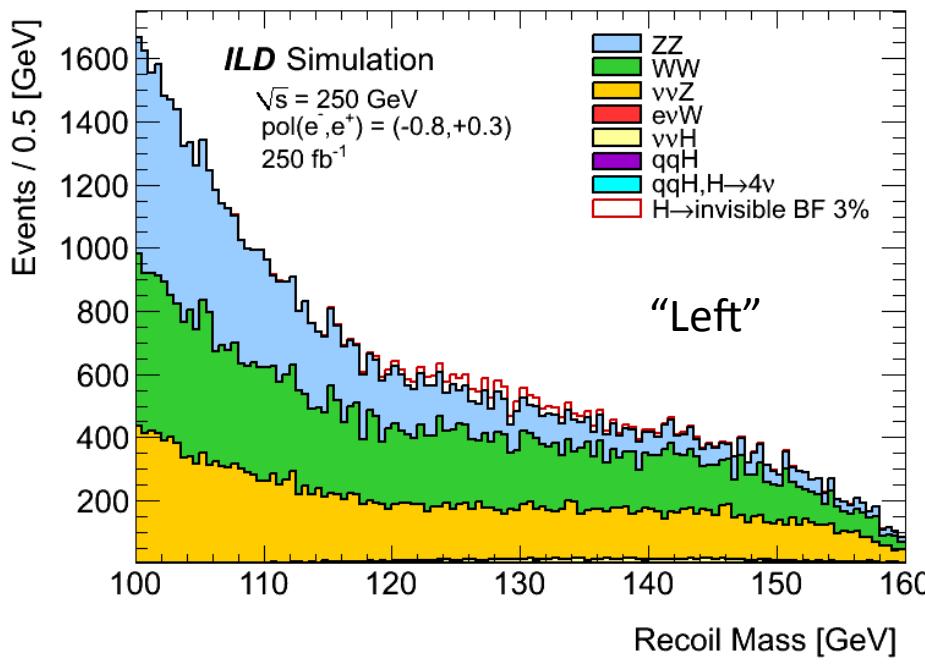
$$P_H = P_{e^+e^-} - P_Z$$

known                      measured

## Signal+Background

Polarizations  $P(e^+, e^-) = (+30\%, -80)$  [denoted below as “Left”]  
 $= (-30\%, +80\%)$  [denoted below as “Right”]

- If  $\text{BF}(H \rightarrow \text{invisible}) = 3\%$ 
  - Signal is clearly seen for “Right” polarization



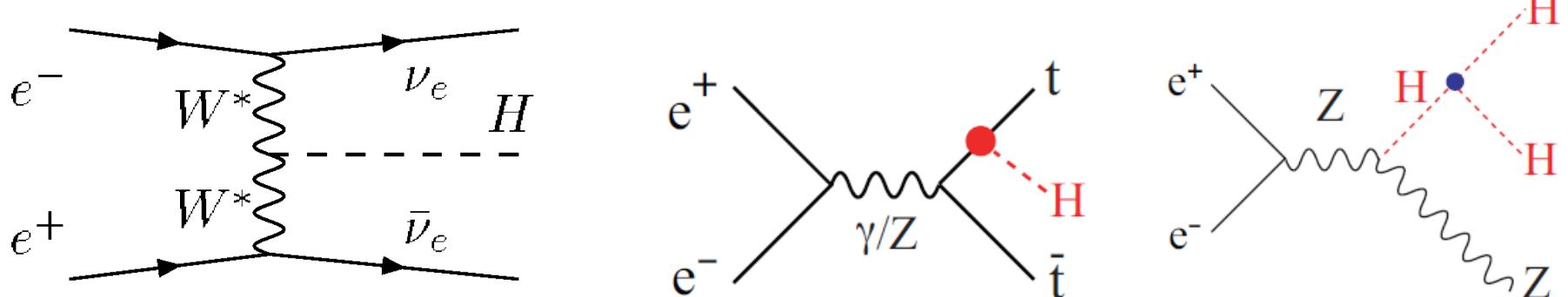
2. By explicitly reconstructing  $H$ , one obtains

$$\sigma_{ZH} \times \text{Br}(H \rightarrow XX)$$

for  $XX = b\bar{b}, c\bar{c}, gg, WW^*, \tau^+\tau^-, ZZ^*, \gamma\gamma$  and  $\mu^+\mu^-$ . Strictly speaking  $g$  stands for a hadron jet not identified as a  $b$  or  $c$  quark. For a SM-like Higgs boson, the Higgs decay into  $gg$  dominates over the decays into  $u\bar{u}$ ,  $d\bar{d}$  and  $s\bar{s}$ . (Likewise, Higgs decay into  $e^+e^-$  is assumed to be negligible.)

3. Since the  $ZH$  production cross section dominates the cross section for  $e^+e^- \rightarrow \nu\bar{\nu}W^+W^- \rightarrow \nu\bar{\nu}H$  at  $\sqrt{s} = 250$  GeV, one can only measure  $\sigma_{\nu\bar{\nu}H} \times \text{Br}(H \rightarrow b\bar{b})$ .

#### 4. $e^+e^- \rightarrow \nu\bar{\nu}H$ , $t\bar{t}H$ and $ZHH$ at $\sqrt{s} = 500$ GeV



- The  $WW$  fusion cross section is now competitive with the  $ZH$  cross section. Thus, one can now measure

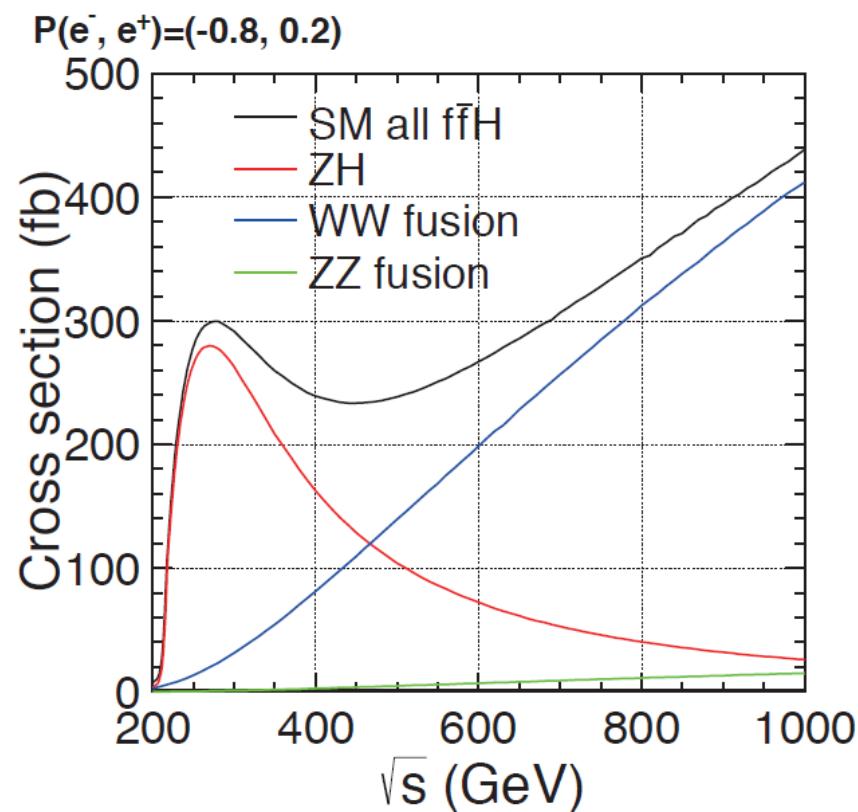
$$\sigma_{\nu\bar{\nu}H} \times \text{Br}(H \rightarrow XX),$$

for all the relevant Higgs channels.

- The cross section for  $e^+e^- \rightarrow t\bar{t}H$  is enhanced near threshold, and yields a measurement of  $\sigma_{t\bar{t}H} \times \text{Br}(H \rightarrow b\bar{b})$ . From this, one can determine the top quark–Higgs Yukawa coupling.
- The process  $e^+e^- \rightarrow ZHH$  is sensitive to the  $HHH$  coupling, although there are other diagrams contributing to  $ZHH$  production that do not depend on the triple Higgs vertex.

## 5. $e^+e^- \rightarrow \nu\bar{\nu}H$ , $t\bar{t}H$ and $\nu\bar{\nu}HH$ at $\sqrt{s} = 1$ TeV

At  $\sqrt{s} = 1$  TeV, the ILC provides better measurements of the top quark Yukawa coupling and the triple Higgs coupling. Moreover, the Higgs production rate has increased significantly from its rate at  $\sqrt{s} = 500$  GeV due to the increasing  $WW$  fusion cross section.



Expected precision for cross section and cross section times branching ratio at the baseline luminosity and a one year runtime (i.e. three years in real time) for each energy/luminosity

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e^-}, P_{e^+}$ )	250 $\text{fb}^{-1}$ at 250 GeV (-0.8,+0.3)		500 $\text{fb}^{-1}$ at 500 GeV (-0.8,+0.3)				1 $\text{ab}^{-1}$ at 1 TeV (-0.8,+0.2)		
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$Zhh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	2.6%	-	3.0	-		42.7%			26.3%
BR(invis.)	< 0.9 %	-	-	-	-				
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow bb$	1.2%	10.5%	1.8%	0.7%	28%		0.5%	6.0%	
$h \rightarrow c\bar{c}$	8.3%	-	13%	6.2%			3.1%		
$h \rightarrow gg$	7.0%	-	11%	4.1%			2.3%		
$h \rightarrow WW^*$	6.4%	-	9.2%	2.4%			1.6%		
$h \rightarrow \tau^+\tau^-$	4.2%	-	5.4%	9.0%			3.1%		
$h \rightarrow ZZ^*$	19%	-	25%	8.2%			4.1%		
$h \rightarrow \gamma\gamma$	34%	-	34%	23%			8.5%		
$h \rightarrow \mu^+\mu^-$	100%	-	-	-			31%		

For invisible decays, the 95% CL upper limit is given.

Note: Mass measurement at  $E_{\text{CM}}=250$  GeV yields  $\Delta M_H=32$  MeV.

Expected accuracies for cross section and cross section times branching ratio at the upgraded luminosity and a one year runtime (i.e. three years in real time) for each energy/luminosity

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e^-}, P_{e^+}$ )	1150 $\text{fb}^{-1}$ at 250 GeV (-0.8,+0.3)		1600 $\text{fb}^{-1}$ at 500 GeV (-0.8,+0.3)				2.5 $\text{ab}^{-1}$ at 1 TeV (-0.8,+0.2)		
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$Zhh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	1.2%	-	1.7	-		23.7%			16.7%
BR(invis.)	< 0.4 %	-	-	-			-		
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow bb$	0.6%	4.9%	1.0%	0.4%	16%		0.3%	3.8%	
$h \rightarrow c\bar{c}$	3.9%	-	7.2%	3.5%			2.0%		
$h \rightarrow gg$	3.3%	-	6.0%	2.3%			1.4%		
$h \rightarrow WW^*$	3.0%	-	5.1%	1.3%			1.0%		
$h \rightarrow \tau^+\tau^-$	2.0%	-	3.0%	5.0%			2.0%		
$h \rightarrow ZZ^*$	8.8%	-	14%	4.6%			2.6%		
$h \rightarrow \gamma\gamma$	16%	-	19%	13%			5.4%		
$h \rightarrow \mu^+\mu^-$	46.6%	-	-	-			20%		

For invisible decays, the 95% CL upper limit is given.

Note: Mass measurement at  $E_{\text{CM}}=250$  GeV yields  $\Delta M_H=15$  MeV.

# Model-independent determinations of Higgs couplings

Example--consider the following four independent measurements:

$$Y_1 = \sigma_{ZH} = F_1 \cdot g_{HZZ}^2$$

$$Y_2 = \sigma_{ZH} \times \text{Br}(H \rightarrow b\bar{b}) = F_2 \cdot \frac{g_{HZZ}^2 g_{Hb\bar{b}}^2}{\Gamma_T}$$

$$Y_3 = \sigma_{\nu\bar{\nu}H} \times \text{Br}(H \rightarrow b\bar{b}) = F_3 \cdot \frac{g_{HWW}^2 g_{Hb\bar{b}}^2}{\Gamma_T}$$

$$Y_4 = \sigma_{\nu\bar{\nu}H} \times \text{Br}(H \rightarrow WW^*) = F_4 \cdot \frac{g_{HWW}^4}{\Gamma_T}$$

$\Gamma_T$  is the Higgs total width,  $g_{HZZ}$ ,  $g_{HWW}$ , and  $g_{Hb\bar{b}}$  are the Higgs couplings to  $ZZ$ ,  $WW$ , and  $b\bar{b}$ , respectively, and  $F_1$ ,  $F_2$ ,  $F_3$ ,  $F_4$  are calculable quantities. For example,

$$F_2 = \left( \frac{\sigma_{ZH}}{g_{HZZ}^2} \right) \left( \frac{\Gamma_{H \rightarrow b\bar{b}}}{g_{Hb\bar{b}}^2} \right).$$

The couplings are obtained as follows:

1. From  $Y_1 \iff g_{HZZ}$
2. From  $Y_1 Y_3 / Y_2 \iff g_{HWW}$
3. From  $g_{HWW}$  and  $Y_4 \iff \Gamma_T$
4. From  $g_{HZZ}$ ,  $g_{HWW}$ ,  $\Gamma_T$  and  $Y_2$  or  $Y_3 \iff g_{Hb\bar{b}}$

We perform a global fit for the Higgs couplings and  $\Gamma_T$  using  $\sigma_{ZH}$  and the  $33\sigma \times \text{Br}$ 's listed in the previous tables. Each observable  $Y_i$  can be written formally as

$$Y_i = Y'_i(F_i, g_{HXX}, \Gamma_T),$$

where  $g_{HXX}$  runs over the various possible Higgs couplings. The  $F_i$  are theoretical quantities with some error. We expect that  $\Delta F_i = 0.5\%$  is a reasonable assumption at the time of ILC running (some suggest that errors as low as  $0.1\%$  are achievable).

Let  $(\Delta Y_i)^2$  be the sum in quadrature of the error on the measurement  $Y_i$  and the total theory error for  $Y'_i$ . We obtain the  $g_{HXX}$  by minimizing the chi-square function,

$$\chi^2 = \sum_i \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2.$$

# Summary of expected accuracies $\Delta g_i/g_i$ and $\Gamma_T$ for model independent determinations of the Higgs boson couplings

Mode	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
$\sqrt{s}$ (GeV)	250	250+500	250+500+1000	250+500+1000
L ( $\text{fb}^{-1}$ )	250	250+500	250+500+1000	1150+1600+2500
$\gamma\gamma$	18 %	8.4 %	4.0 %	2.4 %
$gg$	6.4 %	2.3 %	1.6 %	0.9 %
$WW$	4.9 %	1.2 %	1.1 %	0.6 %
$ZZ$	1.3 %	1.0 %	1.0 %	0.5 %
$t\bar{t}$	—	14 %	3.2 %	2.0 %
$b\bar{b}$	5.3 %	1.7 %	1.3 %	0.8 %
$\tau^+\tau^-$	5.8 %	2.4 %	1.8 %	1.0 %
$c\bar{c}$	6.8 %	2.8 %	1.8 %	1.1 %
$\mu^+\mu^-$	91 %	91 %	16 %	10 %
$\Gamma_T$	12 %	5.0 %	4.6 %	2.5 %
$hh$	—	83 %	21 %	13 %
BR(invis.)	< 0.9 %	< 0.9 %	< 0.9 %	< 0.4 %

The theory errors are  $\Delta F_i/F_i=0.5\%$ . For the invisible branching ratio, the numbers quoted are 95% confidence upper limits.

## Model-independent determinations of Higgs cross sections and branching ratios

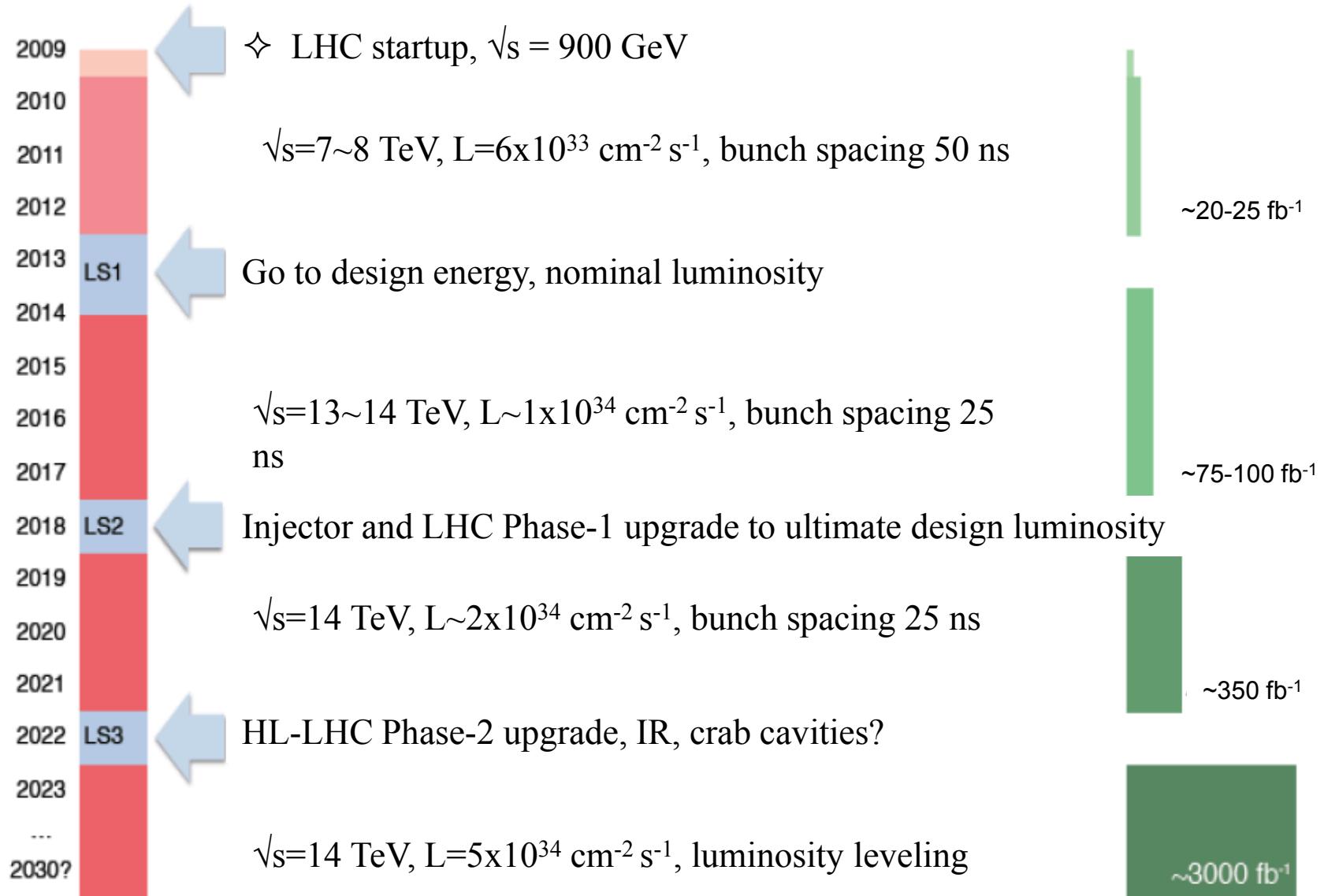
We choose the fit parameters to be three cross sections,  $\sigma_{ZH}$ ,  $\sigma_{\nu\bar{\nu}H}$ ,  $\sigma_{t\bar{t}H}$ , and eight branching ratios,  $\text{Br}(H \rightarrow b\bar{b})$ ,  $\text{Br}(H \rightarrow c\bar{c})$ ,  $\text{Br}(H \rightarrow gg)$ ,  $\text{Br}(H \rightarrow WW^*)$ ,  $\text{Br}(H \rightarrow ZZ^*)$ ,  $\text{Br}(H \rightarrow \tau^+\tau^-)$ ,  $\text{Br}(H \rightarrow \mu^+\mu^-)$ ,  $\text{Br}(H \rightarrow \gamma\gamma)$ .

For example, in the ILC(1000) luminosity scenario we use the measured cross-section  $\sigma_{ZH}$ , the 33 independent  $\sigma \times \text{Br}$  measurements and the appropriately redefined  $Y'_i$  functions to solve for the 11 fit parameters through the minimization of an alternate  $\chi^2$  function.

# Summary of expected accuracies for the three cross sections and eight branching ratios obtained from an eleven parameter global fit of all available data.

	ILC(250)	ILC500	ILC(1000)	ILC(LumUp)
process	$\Delta\sigma/\sigma$			
$e^+e^- \rightarrow ZH$	2.6 %	2.0 %	2.0 %	1.0 %
$e^+e^- \rightarrow \nu\bar{\nu}H$	11 %	2.3 %	2.2 %	1.1 %
$e^+e^- \rightarrow t\bar{t}H$	-	28 %	6.3 %	3.8 %
mode	$\Delta\text{Br}/\text{Br}$			
$H \rightarrow ZZ$	19 %	7.5 %	4.2 %	2.4 %
$H \rightarrow WW$	6.9 %	3.1 %	2.5 %	1.3 %
$H \rightarrow b\bar{b}$	2.9 %	2.2 %	2.2 %	1.1 %
$H \rightarrow c\bar{c}$	8.7 %	5.1 %	3.4 %	1.9 %
$H \rightarrow gg$	7.5 %	4.0 %	2.9 %	1.6 %
$H \rightarrow \tau^+\tau^-$	4.9 %	3.7 %	3.0 %	1.6 %
$H \rightarrow \gamma\gamma$	34 %	17 %	7.9 %	4.7 %
$H \rightarrow \mu^+\mu^-$	100 %	100 %	31 %	20 %

# The LHC Timeline



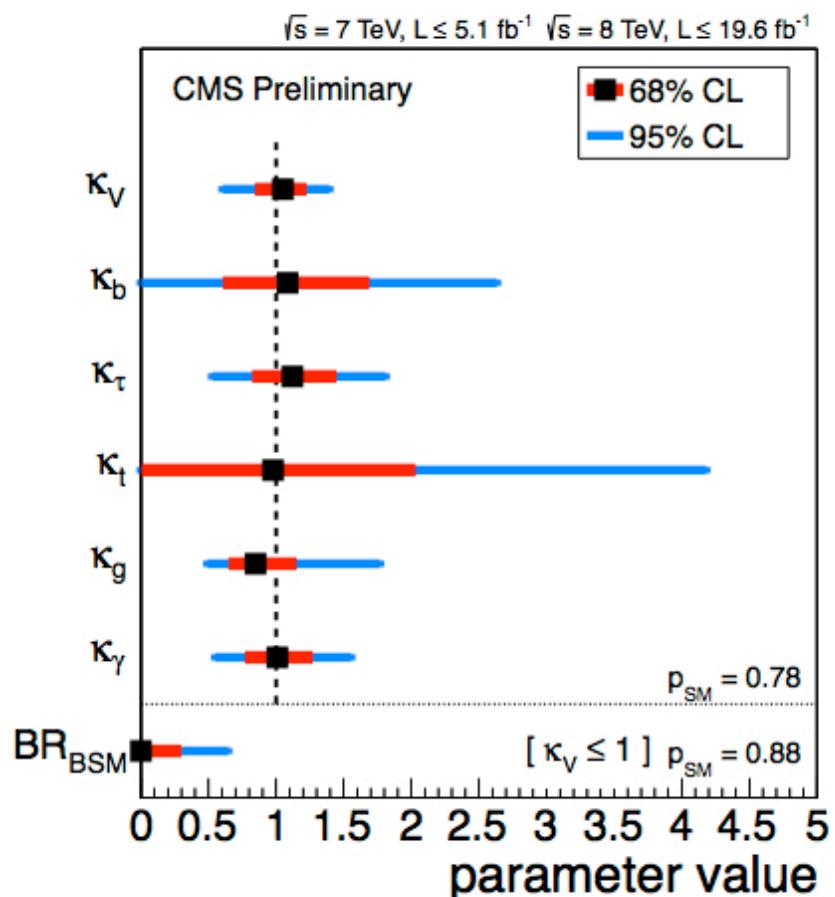
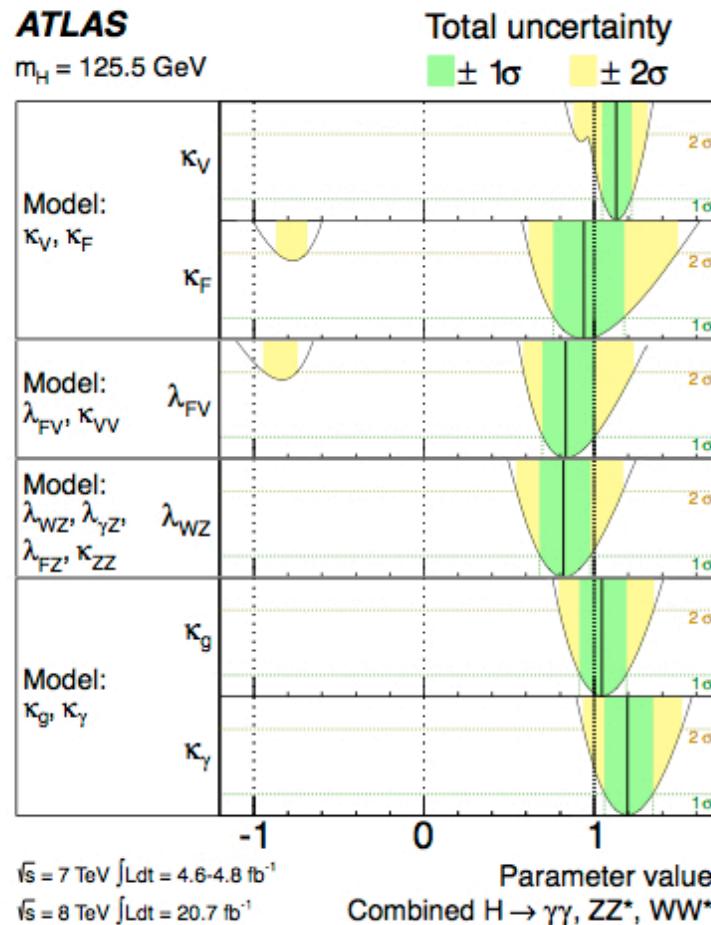
# Comparing LHC and ILC Projected Precision

ATLAS and CMS have provided projections for the ultimate accuracies of Higgs coupling measurements based on the currently planned six year program (accumulating  $300 \text{ fb}^{-1}$  of data) and a proposed high-luminosity ten year program (accumulating  $3000 \text{ fb}^{-1}$  of data).

Results are quoted in terms of the LHC Higgs Cross Section Working Group (HXSWG) benchmark Higgs coupling parameterizations. In one example, deviations from SM–Higgs couplings are expressed in terms of  $\kappa_g$ ,  $\kappa_\gamma$ ,  $\kappa_W$ ,  $\kappa_Z$ ,  $\kappa_b$ ,  $\kappa_t$ ,  $\kappa_\tau$  and a dependent parameter  $\kappa_H$  ( $\kappa_i$ ) which parameterize the departures from the Standard Model couplings and width. In addition, it is assumed that  $\kappa_c = \kappa_t$ ,  $\kappa_\mu = \kappa_\tau$ , etc. and the total Higgs width is the sum of the partial widths for all SM Higgs decays.

We can adopt the same model-dependent assumptions for our ILC analysis by imposing these assumptions as constraints on our model-independent  $\chi^2$  function.

# to date:



# couplings by facility

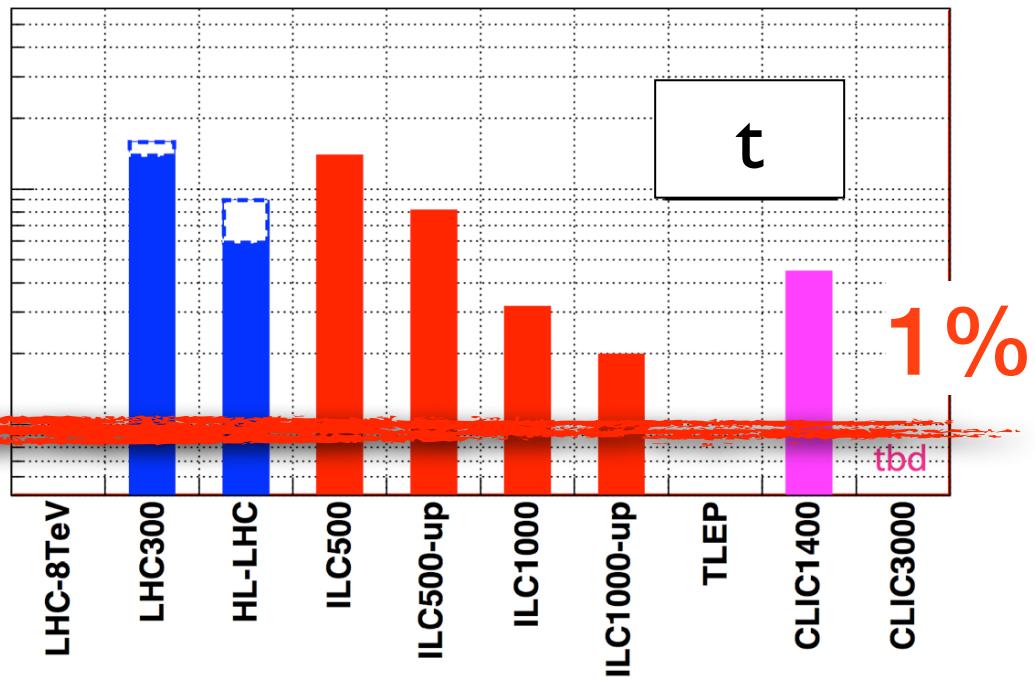
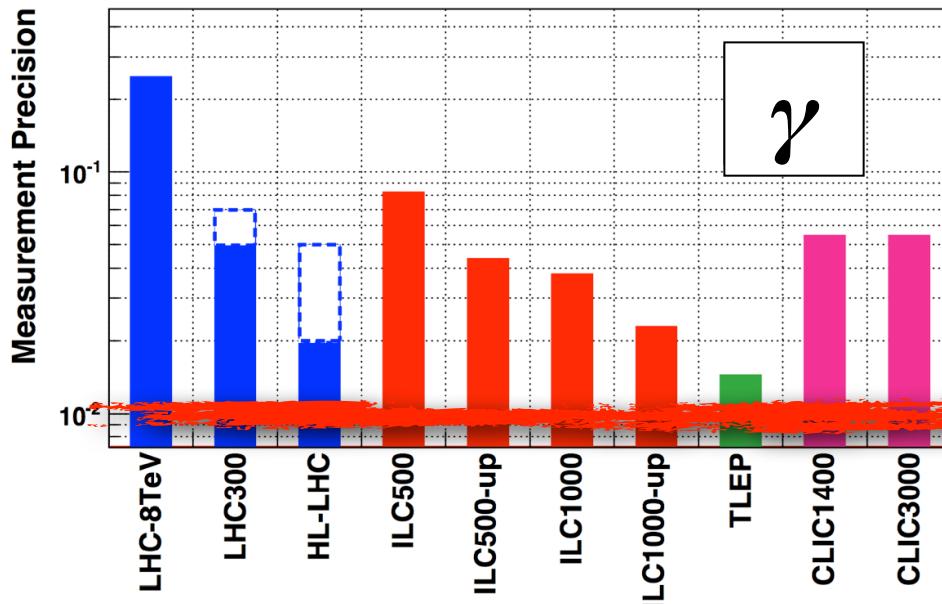
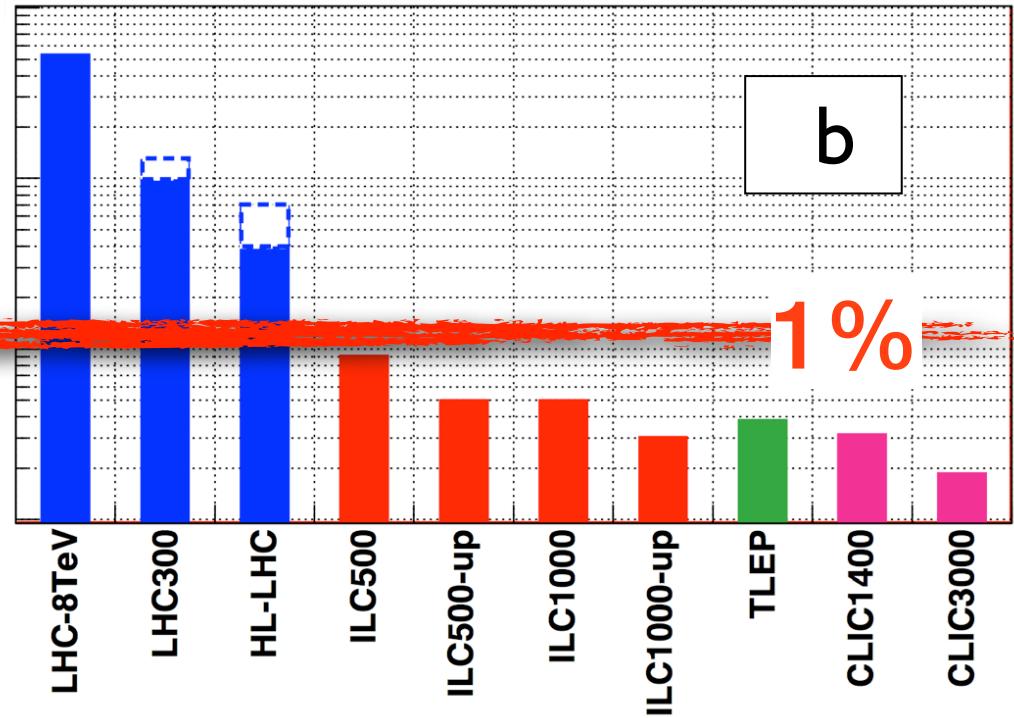
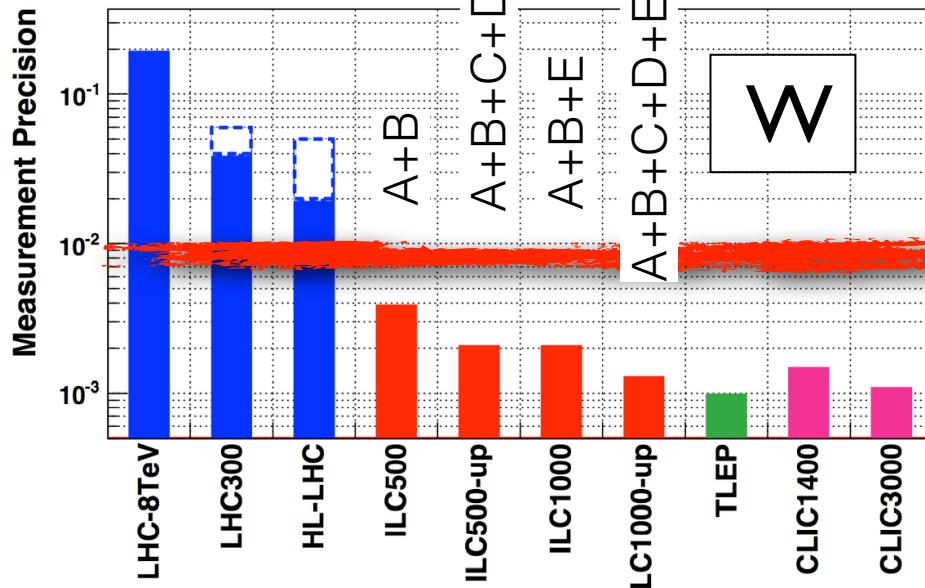
Extrapolating LHC requires a strategy

2 numbers shown:  
optimistic\* – conservative

Facility	LHC	HL-LHC	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC	TLEP (4 IPs)
$\sqrt{s}$ (GeV)	14,000	14,000	250/500	250/500	250/500/1000	250/500/1000	350/1400/3000	240/350
$\int \mathcal{L} dt$ (fb $^{-1}$ )	300/expt	3000/expt	250+500	1150+1600	250+500+1000	1150+1600+2500	500+1500+2000	10,000+2600
$\kappa_\gamma$	5 – 7%	2 – 5%	8.3%	4.4%	3.8%	2.3%	- / 5.5 / <5.5%	1.45%
$\kappa_g$	6 – 8%	3 – 5%	2.0%	1.1%	1.1%	0.67%	3.6 / 0.79 / 0.56%	0.79%
$\kappa_W$	4 – 6%	2 – 5%	0.39%	0.21%	0.21%	0.13%	1.5 / 0.15 / 0.11%	0.10%
$\kappa_Z$	4 – 6%	2 – 4%	0.49%	0.24%	0.44%	0.22%	0.49 / 0.33 / 0.24%	0.05%
$\kappa_\ell$	6 – 8%	2 – 5%	1.9%	0.98%	1.3%	0.72%	3.5 / 1.4 / <1.3%	0.51%
$\kappa_d$	10 – 13%	4 – 7%	0.93%	0.51%	0.51%	0.31%	1.7 / 0.32 / 0.19%	0.39%
$\kappa_u$	14 – 15%	7 – 10%	2.5%	1.3%	1.3%	0.76%	3.1 / 1.0 / 0.7%	0.69%

\*  $\delta(\text{sys}) \propto \frac{1}{\sqrt{\mathcal{L}}} \quad \& \quad \delta(\text{theory}) \downarrow 1/2$

# Precision in kappa by facility

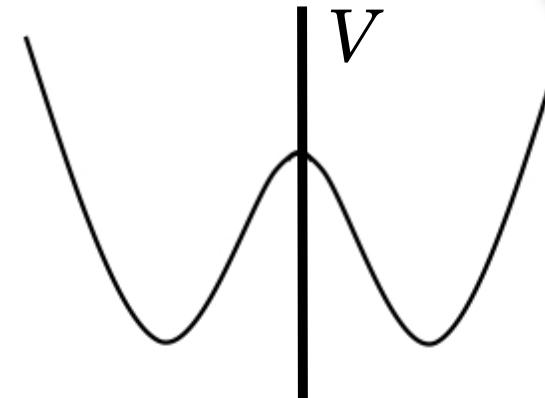
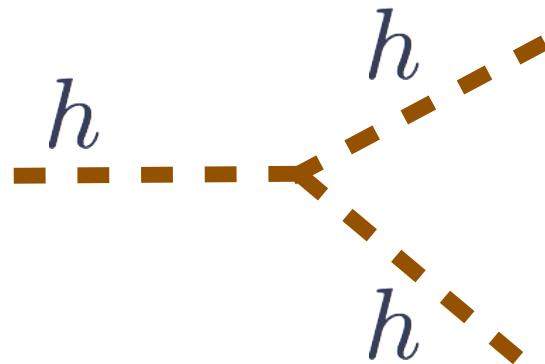


# Higgs Self-Coupling

Critical feature of SM

- extremely challenging

$$V = -\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$



	HL-LHC	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC1400	CLIC3000	HE-LHC	VLHC
$\sqrt{s}$ (GeV)	14000	500	500	500/1000	500/1000	1400	3000	33,000	100,000
$\int \mathcal{L} dt$ (fb $^{-1}$ )	3000	500	1600 $^{\ddagger}$	500/1000	1600/2500 $^{\ddagger}$	1500	+2000	3000	3000
$\lambda$	50%	83%	46%	21%	13%	21%	10%	20%	8%

Higgs self-coupling is difficult to measure precisely at any facility.

## The Bottom Line

- The ILC will provide the next significant step in the precision study of Higgs boson properties. LHC precision measurements in the 5–10% range will be brought down to the 1% level.
- The ILC is able to provide a model-independent determination of Higgs couplings via the measurement of  $\sigma_{ZH}$ , in addition to measuring  $\sigma \times Br$  in numerous channels. (In contrast, LHC only can measure  $\sigma \times Br$ ).
- Together with the LHC Higgs data, the ILC will provide critical measurements that can probe new physics beyond the Standard Model and provide important clues as to what may lie ahead.

# Back-up slides

Summary of expected accuracies  $\Delta g_i/g_i$  and  $\Gamma_T$  using the model-dependent seven parameter HXSWG benchmark parameterization, assuming all theory errors are 0.5%

Mode	ILC(250)	ILC(500)	ILC(1000)	ILC(LumUp)
$\gamma\gamma$	17 %	8.3 %	3.8 %	2.3 %
$gg$	6.1 %	2.0 %	1.2 %	0.7 %
$WW$	4.7 %	0.5 %	0.3 %	0.2 %
$ZZ$	0.8 %	0.5 %	0.5 %	0.3 %
$t\bar{t}$	6.4 %	2.6 %	1.4 %	0.9 %
$b\bar{b}$	4.7 %	1.0 %	0.6 %	0.4 %
$\tau^+\tau^-$	5.2 %	2.0 %	1.3 %	0.8 %
$\Gamma_T$	9.0 %	1.8 %	1.1 %	0.9 %