

# Global fitting with LHC Higgs signals in the 2HDMs

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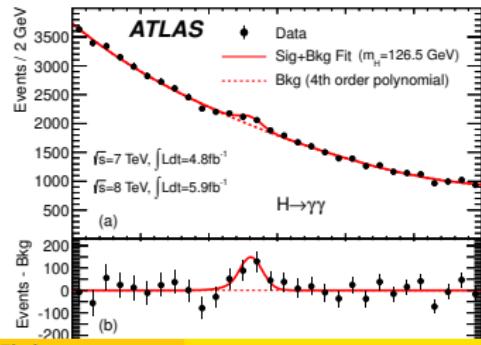
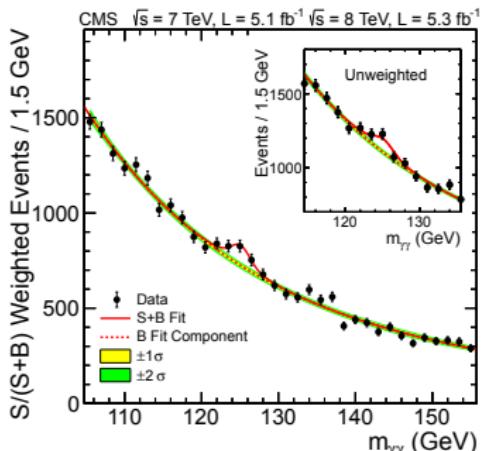
with J.F. Gunion, S. Kraml and B. Dumont, arXiv. 1309.XXXX

# SCALARS 2013

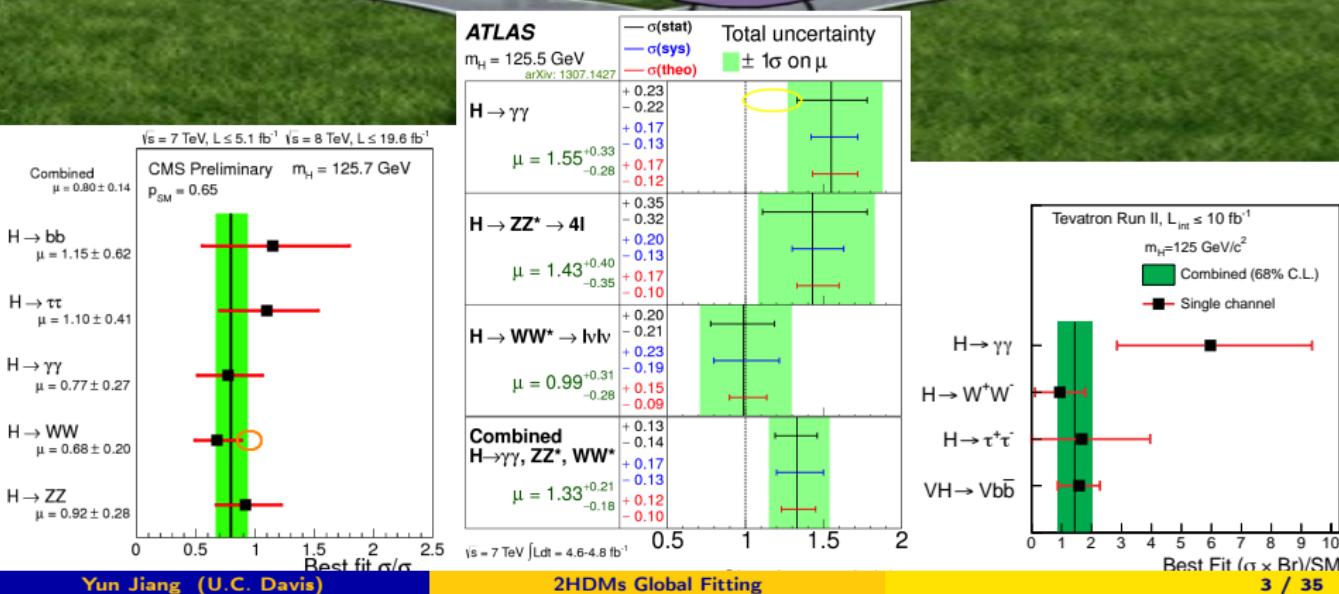
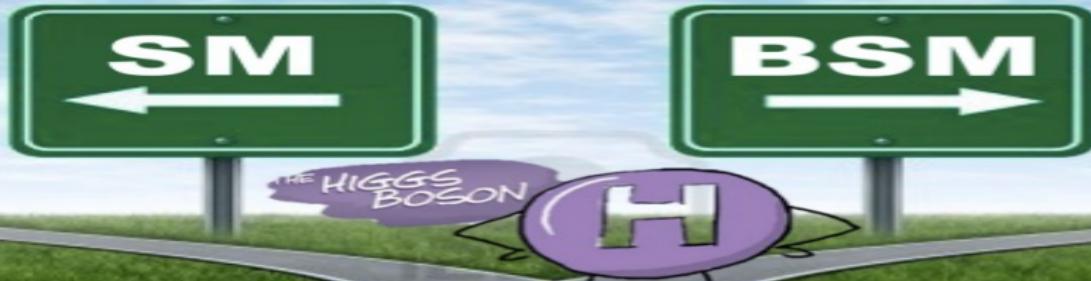
12-16 September 2013  
Warsaw, Poland

July 4th, 2012–A **HISTORIC** moment in science.

It is a privilege to witness the Higgs discovery.



# Whether or not it *is* the SM Higgs?



# What's the naive extension?



## Two Higgs Doublet Model

- ➊ The simplest non-trivial extension on the Higgs sector beyond the SM.
  - Duplicate a complex  $SU(2)_L$  Higgs doublet with the same hypercharge  $Y = +1$ .
  - More physical Higgs states.
- ➋ Type II realized in the MSSM.
- ➌ Existence of the charged Higgs boson  $H^\pm$ ?

## 2HDM Higgs sector

$$\begin{aligned}\mathcal{V} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - [m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}] \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right\}\end{aligned}$$

### The models we studied

- ① NO explicit  $\mathcal{CP}$  violation: all  $\lambda_i$  and  $m_{12}^2$  are assumed to be real.
- ② NO spontaneous  $\mathcal{CP}$  breaking: take  $\xi = 0$ .
- ③ "soft"  $Z_2$  symmetry ( $\Phi_1 \rightarrow \Phi_1$ ,  $\Phi_2 \rightarrow -\Phi_2$ ) breaking:  $m_{12}^2 \neq 0$ ;  $\lambda_6 = \lambda_7 = 0$ .

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free parameters:  $\tan \beta$ ,  $m_{12}^2$ ,  $\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5$

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### Electroweak symmetry breaking

$$\begin{aligned}\Phi_1 &= \begin{pmatrix} \phi_1^+ \\ (\nu \cos \beta + \rho_1 + i\eta_1)/\sqrt{2} \end{pmatrix} \\ \Phi_2 &= \begin{pmatrix} \phi_2^+ \\ (e^{i\xi} \nu \sin \beta + \rho_2 + i\eta_2)/\sqrt{2} \end{pmatrix}\end{aligned}$$

2 CP-even neutral scalars:  $h = -\rho_1 \sin \alpha + \rho_2 \cos \alpha$   
 $H = \rho_1 \cos \alpha + \rho_2 \sin \alpha$

1 CP-odd neutral pseudoscalar:  $A = -\eta_1 \sin \beta + \eta_2 \cos \beta$

2 charged scalars:  $H^\pm$

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our inputs:  $m_h$ ,  $m_H$ ,  $m_A$ ,  $m_{H^+}$ ,  $\tan \beta$ ,  $\sin \alpha$ ,  $m_{12}^2$

### Electroweak symmetry breaking

$$\begin{aligned}\Phi_1 &= \begin{pmatrix} \phi_1^+ \\ (v \cos \beta + \rho_1 + i\eta_1)/\sqrt{2} \end{pmatrix} \\ \Phi_2 &= \begin{pmatrix} \phi_2^+ \\ (e^{i\xi} v \sin \beta + \rho_2 + i\eta_2)/\sqrt{2} \end{pmatrix}\end{aligned}$$

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## 2HDM Yukawa sector

$$\mathcal{L} = y_{ij}^1 \bar{\psi}_i \psi_j \Phi_1 + y_{ij}^2 \bar{\psi}_i \psi_j \Phi_2$$

We consider the Type I and Type II models, in which tree level FCNC are completely absent due to some symmetry.<sup>1</sup>

Model	$u_R^i$	$d_R^i$	$e_R^i$	Realization
Type I	$\Phi_2$	$\Phi_2$	$\Phi_2$	$\Phi_1 \rightarrow -\Phi_1$
Type II	$\Phi_2$	$\Phi_1$	$\Phi_1$	$\Phi_1 \rightarrow -\Phi_1, d_R^i \rightarrow -d_R^i$

$$\begin{aligned} \mathcal{L}_{\text{Yukawa}}^{\text{2HDM}} &= - \sum_{f=u,d,\ell} \frac{m_f}{v} \left( C_f^h \bar{f} f h + C_f^H \bar{f} f H - i C_f^A \bar{f} \gamma_5 f A \right) \\ &\quad - \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} \left( m_u C_u^A P_L + m_d C_d^A P_R \right) d H^+ + \frac{\sqrt{2} m_\ell C_\ell^A}{v} \bar{\nu}_L \ell_R H^1 + \text{h.c.} \right\} \end{aligned}$$

	$C_V^h$	$C_u^h$	$C_{d,\ell}^h$	$C_V^H$	$C_u^H$	$C_{d,\ell}^H$	$C_V^A$	$C_u^A$	$C_{d,\ell}^A$
Type I	$\sin(\beta - \alpha)$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\cos(\beta - \alpha)$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	0	$\cot \beta$	$-\cot \beta$
Type II	$\sin(\beta - \alpha)$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\cos(\beta - \alpha)$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	0	$\cot \beta$	$\tan \beta$

$$(C_V^h)^2 + (C_V^H)^2 + (C_V^A)^2 = 1$$

<sup>1</sup> Paschos-Glashow-Weinberg theorem: if all fermions with the same quantum numbers couple to the same Higgs multiplet, then FCNC will be absent.

# Theoretical Constraints on the 2HDMs

- Theoretically, (denoted jointly as SUP)

## ① Vacuum stability N.G. Deshpande and E. Ma, PRD18(1978)2574

The potential must be bounded from below (positivity).

$$\lambda_1 > 0$$

$$\lambda_2 > 0$$

$$\lambda_3 > -\sqrt{\lambda_1 \lambda_2}$$

$$\lambda_3 + \lambda_4 - |\lambda_5| > -\sqrt{\lambda_1 \lambda_2} \quad \text{if } \lambda_6 = \lambda_7 = 0$$

## ② Unitarity

Requiring the largest eigenvalue for the tree-level for full multi-state scattering matrix in  $(h, H, A)$  space to be less than the upper limit  $16\pi$ .

## ③ Perturbativity

All self couplings among the mass eigenstates and Yukawa coupling must be finite,  $|\Lambda_i| < 4\pi$ .

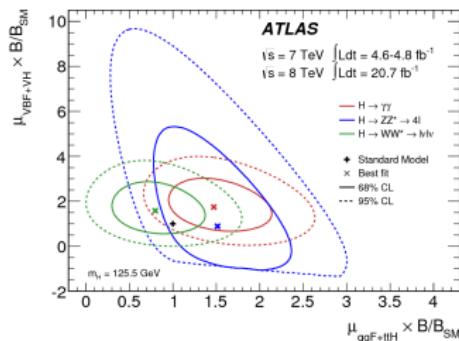
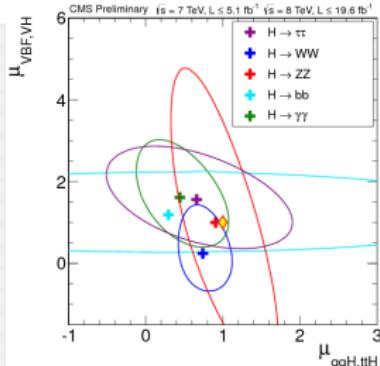
# Experimental constraints: what we consider ...

- preLHC: SUP, STU,  $B$ -physics,  $(g - 2)_\mu$ , LEP (applied for some scenarios)
- **SMHlimit**:
  - $H \rightarrow ZZ^* \rightarrow 4\ell$  for heavier Higgs up to 1 TeV
  - $gg \rightarrow H \rightarrow \tau\tau$  and  $gg \rightarrow bbH$  with  $H \rightarrow \tau\tau$  for heavier Higgs up to 500 GeV
- **postLHC**: additionally,  $\gamma\gamma$ ,  $ZZ$ ,  $WW$ ,  $bb$ ,  $\tau\tau$  signals for **125 GeV** Higgs

$$\mu_Y^H(X) \equiv \frac{\sigma(Y \rightarrow H) BR(H \rightarrow X)}{\sigma(Y \rightarrow h_{\text{SM}}) BR(h_{\text{SM}} \rightarrow X)}$$

	$\hat{\mu}_{\text{ggF}}$	$\hat{\mu}_{\text{VBF}}$
$\gamma\gamma$	$0.98 \pm 0.28$	$1.72 \pm 0.59$
$VV$	$0.91 \pm 0.16$	$1.01 \pm 0.49$
$bb/\tau\tau$	$0.98 \pm 0.63$	$0.97 \pm 0.32$
$bb$	$-0.23 \pm 2.86$	$0.97 \pm 0.38$
$\tau\tau$	$1.07 \pm 0.71$	$0.94 \pm 0.65$

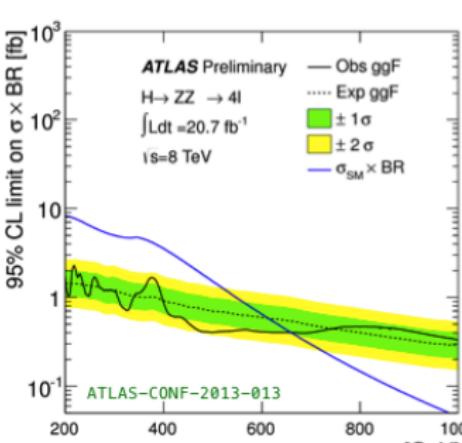
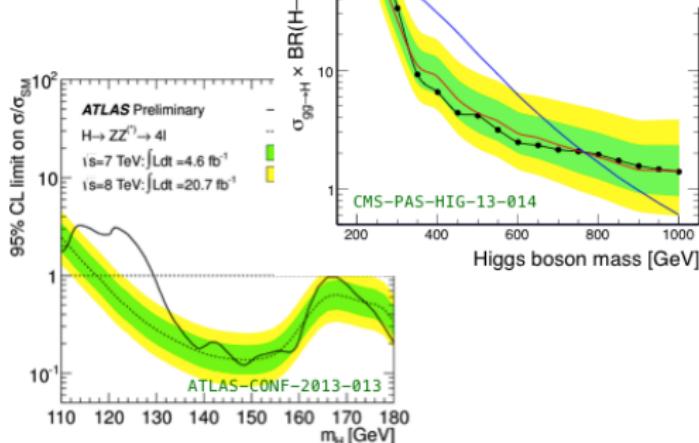
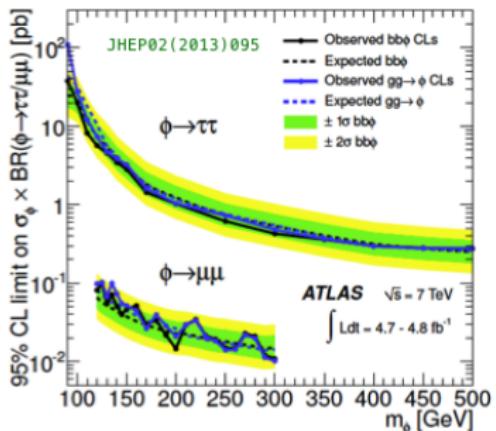
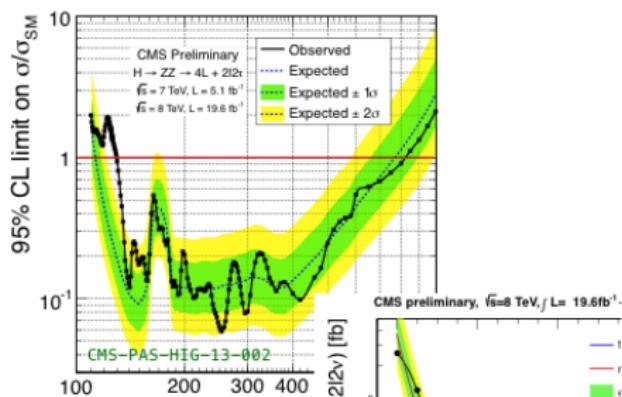
G.Belanger, B.Dumont, U. Ellwanger,  
J.F. Gunion & S. Kraml, arXiv:1306.2941



Jack et. al ...

- not individually but corporately treat CMS and ATLAS data.
- take the ggF,ttH–VBF,VH 2D correlation into consideration.

# Search limits on the heavier Higgs bosons



## 2HDM scan

vacuum) [18]. We scan over the following ranges <sup>1</sup>:

$$\begin{aligned} \sin \alpha &\in [-1, 1], \quad \tan \beta \in [0.5, 60], \quad m_{12}^2 \in [-(2 \text{ TeV})^2, (2 \text{ TeV})^2], \\ m_A &\in [5 \text{ GeV}, 2 \text{ TeV}], \quad m_{H^\pm} \in [m^*, 2 \text{ TeV}], \end{aligned} \quad (1)$$

where  $m^*$  is the lowest value of  $m_{H^\pm}$  allowed by B physics constraints. These lower bounds as a function of  $\tan \beta$  are as shown in Fig. 15 of [19] in the case of the Type II model (roughly  $m^* \sim 300 \text{ GeV}$  in this case) and as shown in Fig. 18 of [19] in the case of the Type I model. For the physical Higgs masses, we consider

$$m_h \in [123 \text{ GeV}, 128 \text{ GeV}], \quad m_H \in ]128 \text{ GeV}, 2 \text{ TeV}], \quad (2)$$

for the case that  $h$  is the observed state near 125.5 GeV, or

$$m_H \in [123 \text{ GeV}, 128 \text{ GeV}], \quad m_h \in [10 \text{ GeV}, 123 \text{ GeV}[ , \quad (3)$$

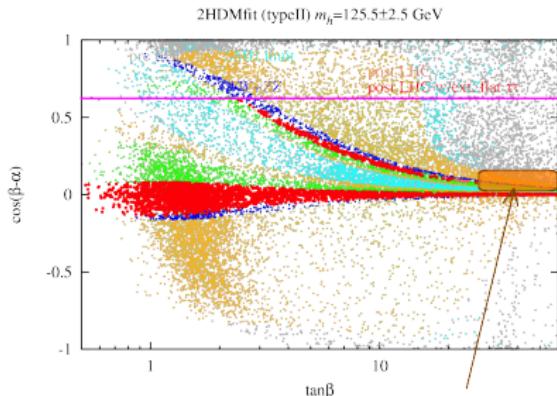
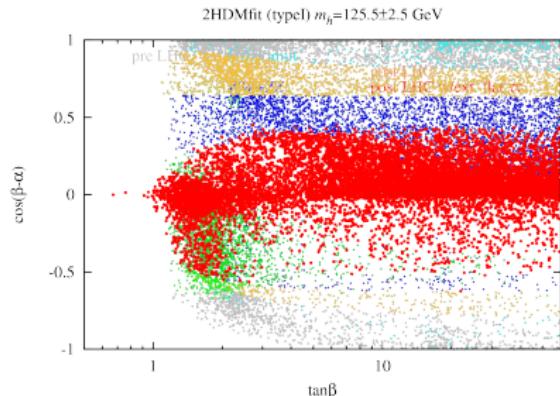
for the case that  $H$  is the observed state near 125.5 GeV. Moreover, we separately investigate degenerate scenarios, where two states ( $h$  and  $H$ ,  $h$  and  $A$ , or  $H$  and  $A$ ) or all three neutral Higgses fall into the 123–128 GeV mass window. The window of  $125.5 \pm 2.5 \text{ GeV}$  is adopted to account for theoretical uncertainties and to facilitate the study of near-degenerate scenarios.

<sup>1</sup> The lower bound on  $\tan \beta$  is chosen to ensure the top Yukawa coupling within the perturbativity region. Unlike  $Z_2$  symmetric 2HDM which constrains  $\tan \beta \lesssim 7$  [ref], high  $\tan \beta$  up to 100 is allowed when  $Z_2$  symmetry is softly broken.

## Single Higgs Scenarios

- $h$  or  $H$  either lies at 125 GeV.

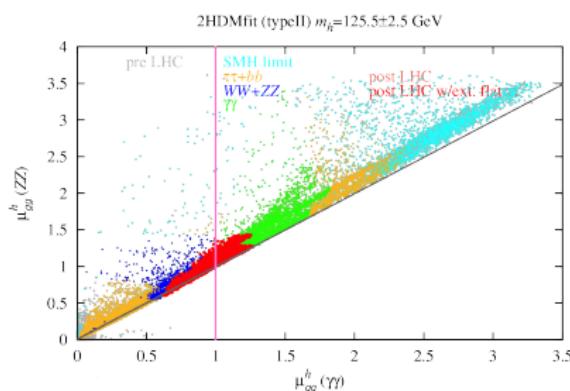
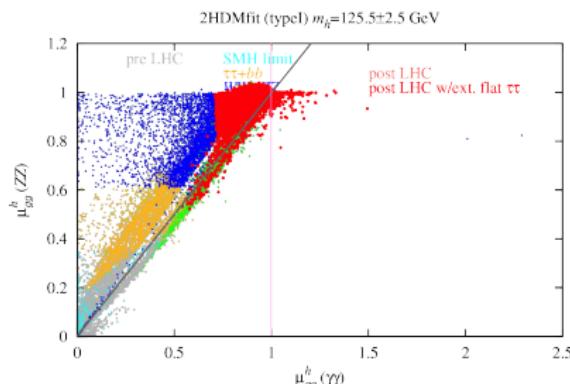
Most important  $\cos(\beta - \alpha)$  vs.  $\tan \beta$



- Generally, for the lightest Higgs boson  $h$  be SM like,  $C_V^h \sim \sin(\beta - \alpha) \sim 1$ .
- However, there are **two branches** present in Type II model. In addition to the trivial one, **the upper strip extends to  $C_V^h \sim 0.7$**  and also **terminates at large  $\tan \beta$**  due to **too large  $\tau\tau$  rate**.

# $h \sim 125$ -Higgs signals

Two most precisely measured  $\mu_{gg}^h(ZZ)$  vs.  $\mu_{gg}^h(\gamma\gamma)$



## Type I

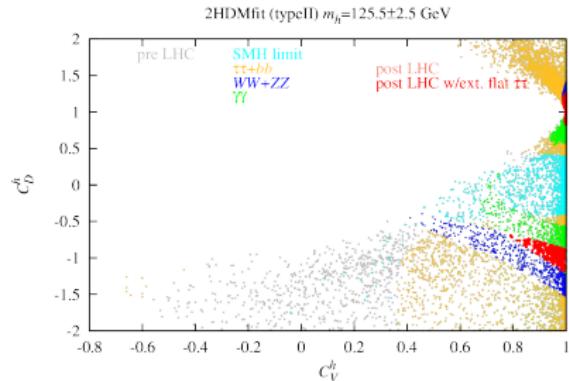
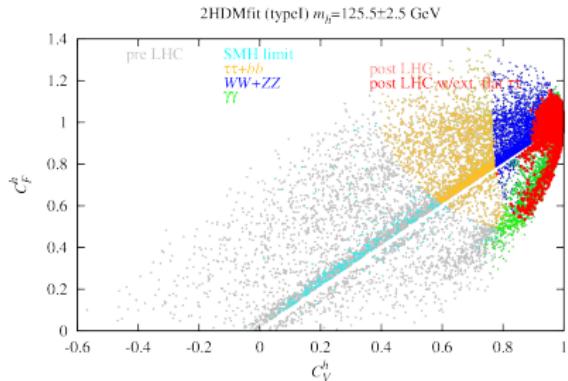
- **not too much above 1** because that gluon fusion production cannot be much enhanced (universal up and down type couplings).

- $\frac{\mu_{gg}^h(ZZ)}{\mu_{gg}^h(\gamma\gamma)} < 1$  for enhanced  $\mu_{gg}^h(\gamma\gamma)$  rate.

## Type II

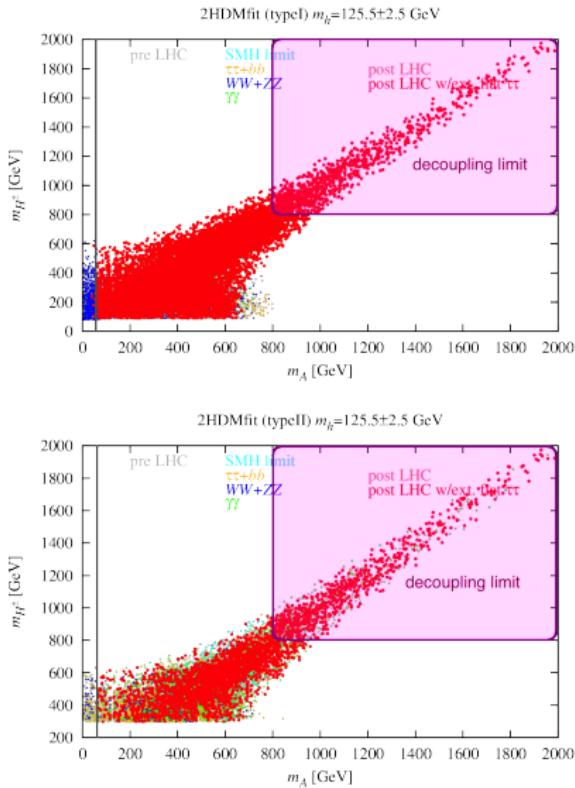
- **easy realization of substantial enhancement.**
- $\mu_{gg}^h(ZZ)$  is strictly larger than  $\mu_{gg}^h(\gamma\gamma)$  for enhanced  $\mu_{gg}^h(\gamma\gamma)$  rate.

## $h \sim 125$ -Coupling fits $C_D$ vs. $C_V$



- Remarkably, the coupling  $C_V^h$  prefers to be +1 or so.
- Type I:  $C_F^h$  and  $C_V^h$  have a moderate spread near the SM limit.
- Type II: in addition to a very SM-like region, there is another region where the deviation in the  $C_V^h$  is at most 20% from its SM value, and the  $C_D^h$  is slightly smaller in magnitude and have the opposite sign to its SM values.

# $h \sim 125$ -Constraints on the other Higgs bosons



- Perturbativity set bound on  $m_A$  for a certain  $m_{H^\pm}$ .

$$m_A^2 - m_{H^\pm}^2 = \frac{v^2}{2}(\lambda_4 - \lambda_5)$$

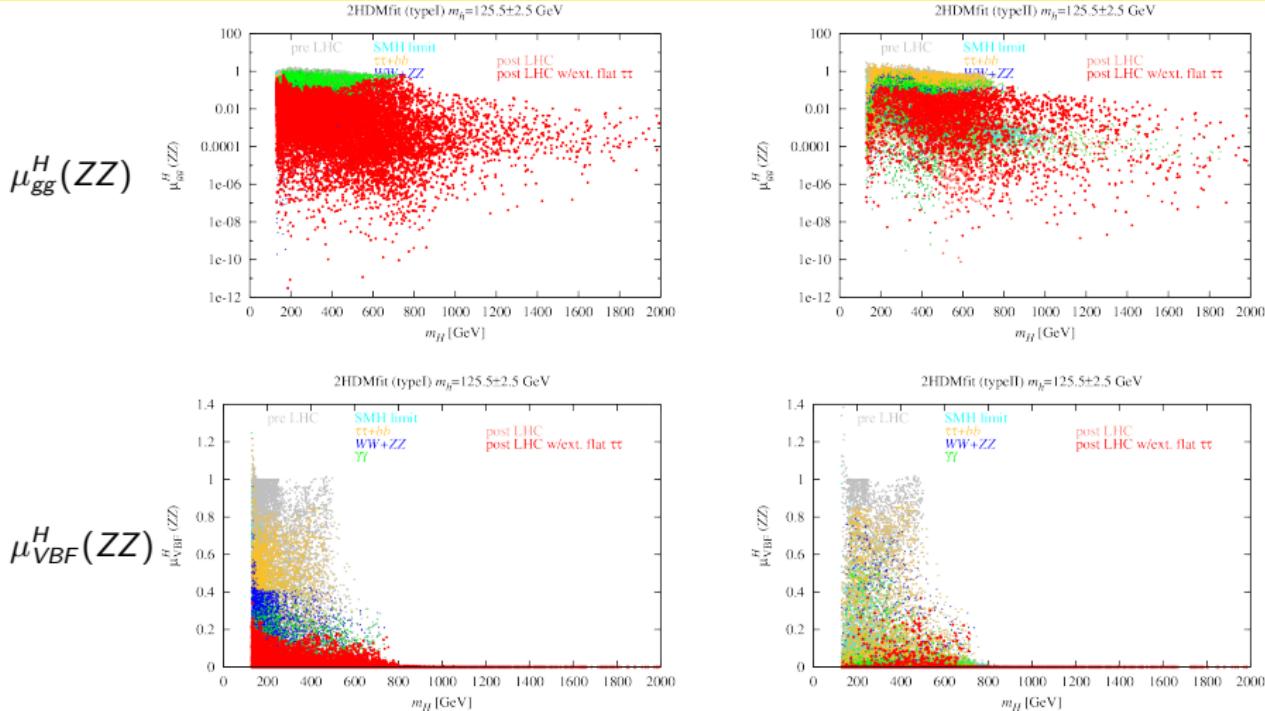
- $m_{H^\pm} > 80$  GeV in Type I and  $m_{H^\pm} > 295$  GeV in Type II.

- No strong correlation away from the decoupling limit ( $m_H > 800$  GeV).

- The lowest  $m_A \approx 40$  GeV. However, if  $m_A < \frac{m_h}{2}$ , rare decay  $h \rightarrow AA$  open.  $BR(h \rightarrow AA)$  at most 10%, otherwise it results in the suppression in the  $WW$  and  $ZZ$  to escape the LHC signals.

Whether is the Higgs boson(s) other than 125 GeV observable or not?

# $h \sim 125$ -Heavier Higgs boson $H$ search

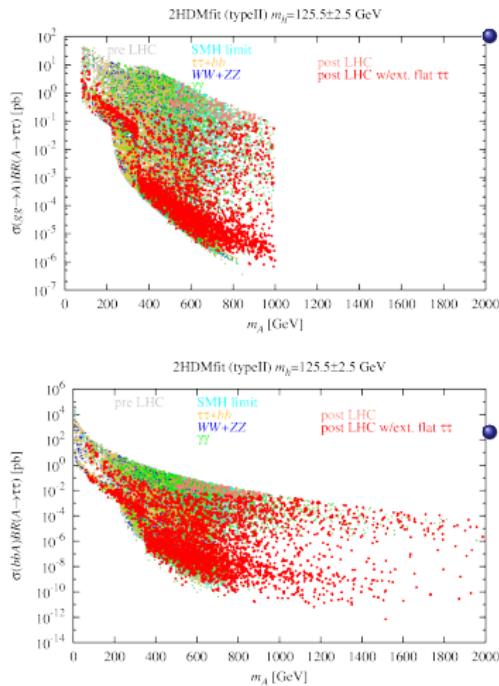
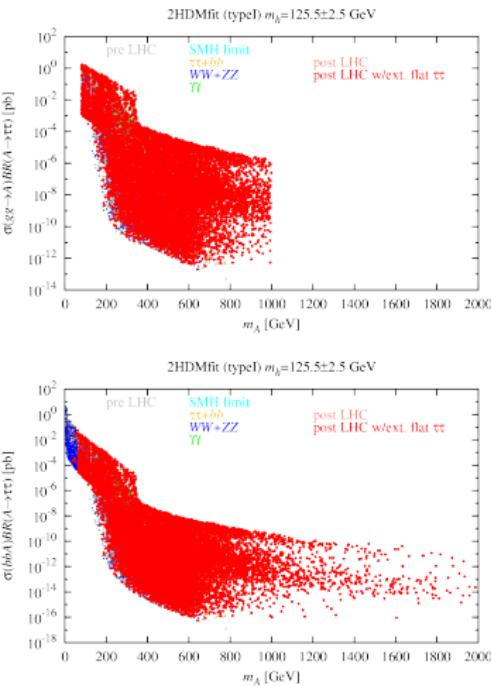


For heavier CP-even Higgs boson  $H$ , easier to access are  $\mu_{gg}(ZZ)$  and  $\mu_{VBF}(ZZ)$ , about 0.2. This level of signal would eventually accessible in light of much smaller width <sup>a</sup>.

<sup>a</sup>We correct for the width difference by rescaling the observed limits on  $\sigma \times BR$  by  $f = \sqrt{\frac{\Gamma_H^2 + (4 \text{ GeV})^2}{\Gamma_{hSM}^2 + (4 \text{ GeV})^2}}$ .

# $h \sim 125$ -Heavier Higgs boson $A$ search

For heavier CP-odd Higgs boson  $A$ , the potential interest are  $gg \rightarrow A \rightarrow \tau\tau$  and the bottom quark associated processes:  $gg \rightarrow bbA$  with  $A \rightarrow \tau\tau$ .

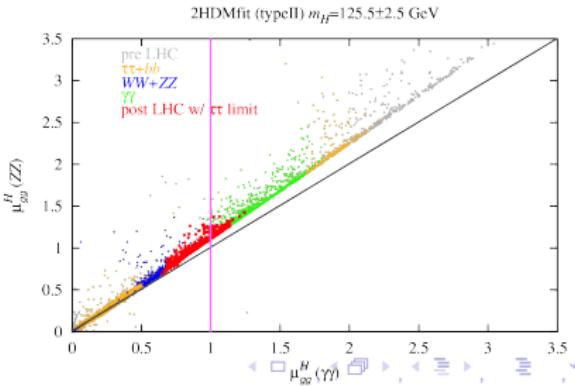
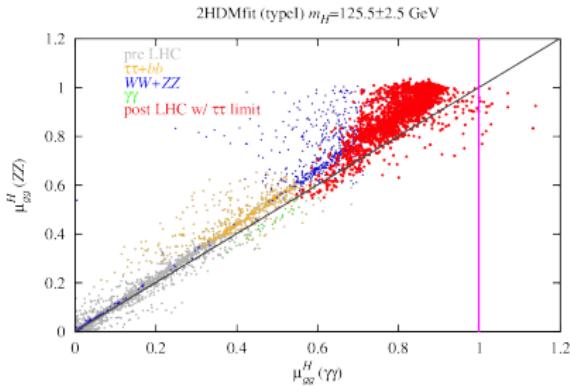
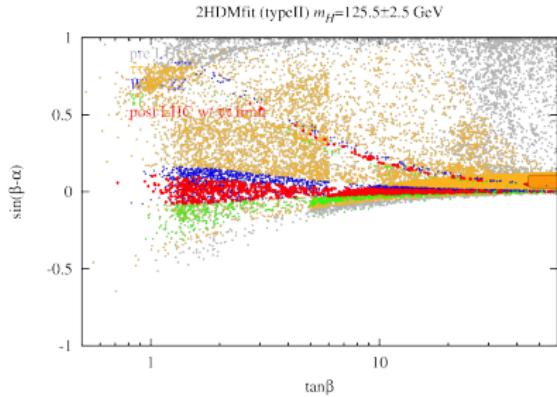
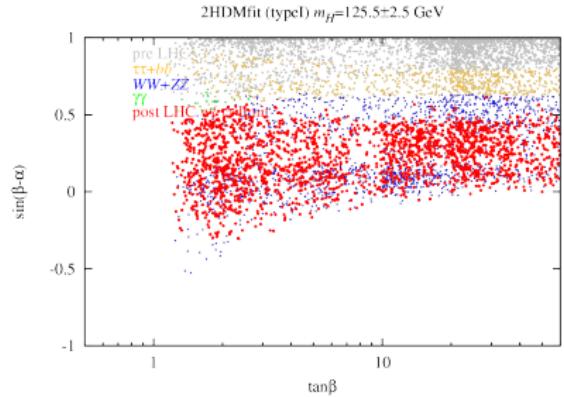


Overall speaking, heavy Higgs boson searches has NO impact on the LHC favored points in the Type I as  $\sigma < 10^{-2}$  pb for b-associated production.

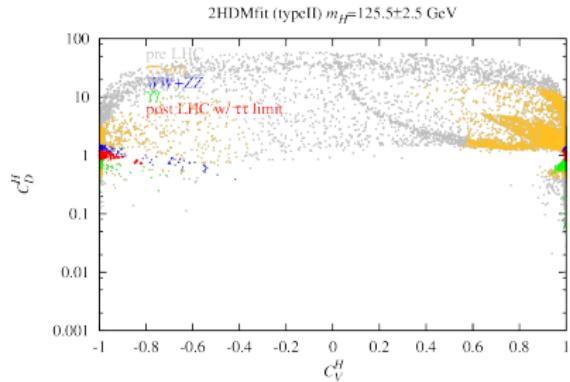
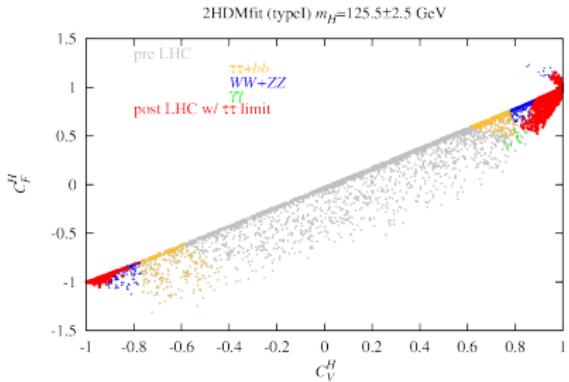
But exclude a few points in Type II for  $m_A \sim 500 - 1000$  GeV b.c.  $C_\tau^A$  can be very large at high  $\tan \beta$ .

# $H \sim 125$ -Parameter and Signals

For  $H$  be SM like,  $C_V^H \sim \cos(\beta - \alpha) \sim 1$ , that is,  $\cos(\beta - \alpha) \rightarrow \sin(\beta - \alpha) \sim 0$ .



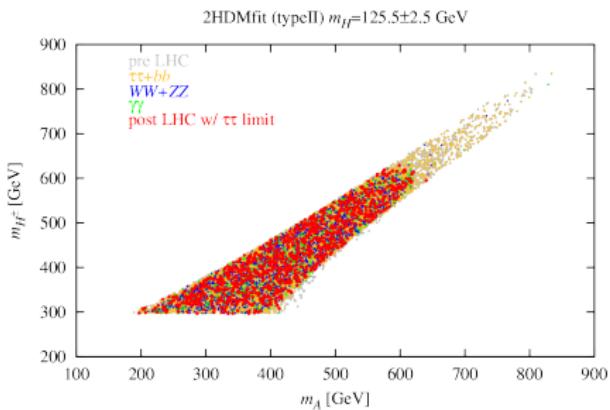
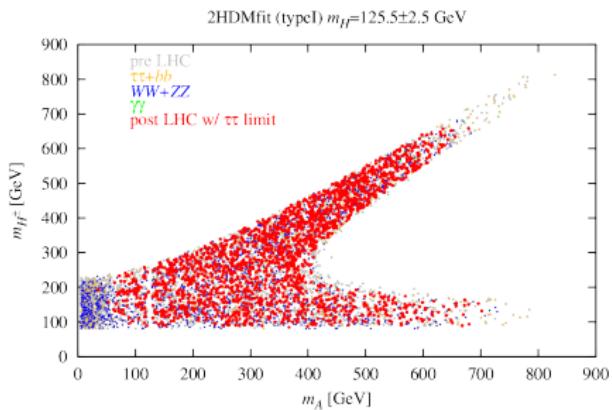
## $H \sim 125$ -Coupling fits $C_D$ vs. $C_V$



In the contrast to the case of  $m_h \sim 125$  GeV,

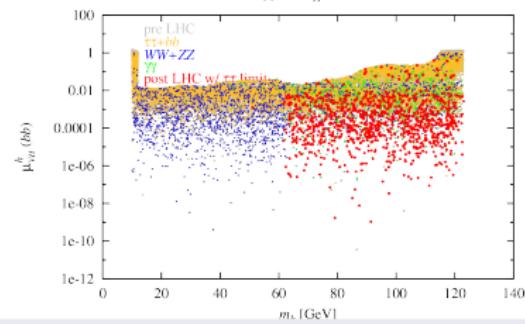
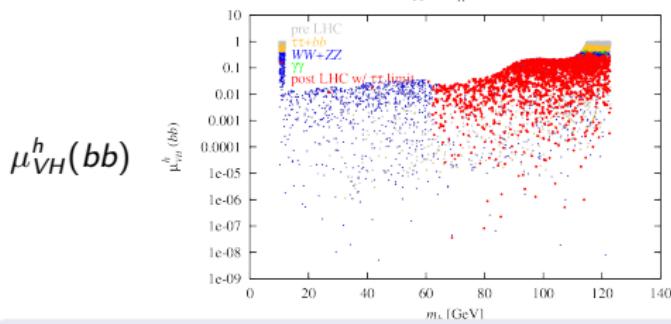
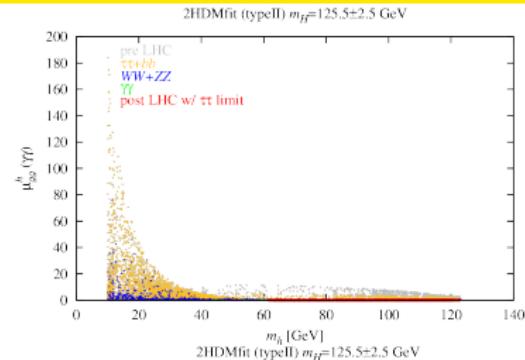
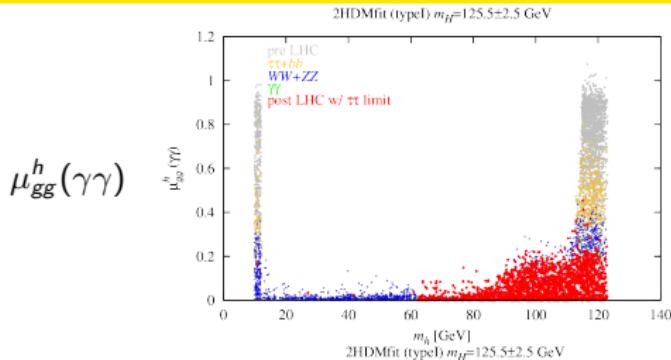
- The coupling  $C_V^H$  could be both  $-1$  and  $+1$ .
- $C_F^H$  has about 10% derivation from  $+1$  in Type I whereas  $C_D^H$  is strictly constrained near  $+1$  in Type II.

## $H \sim 125$ -Constraints on the other Higgs bosons



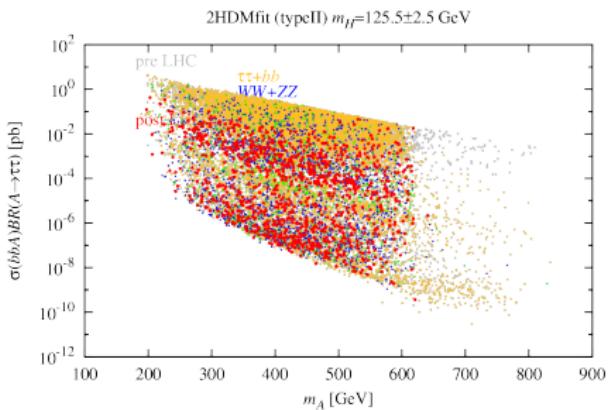
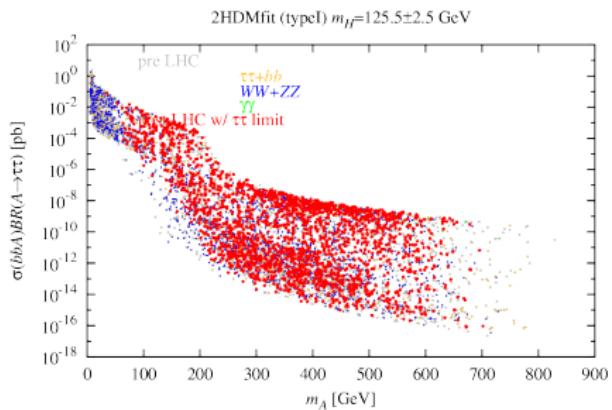
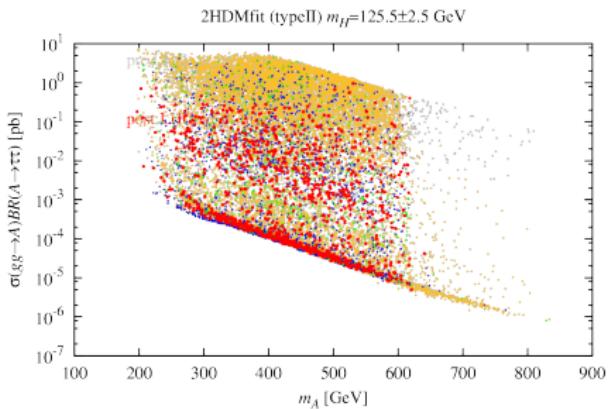
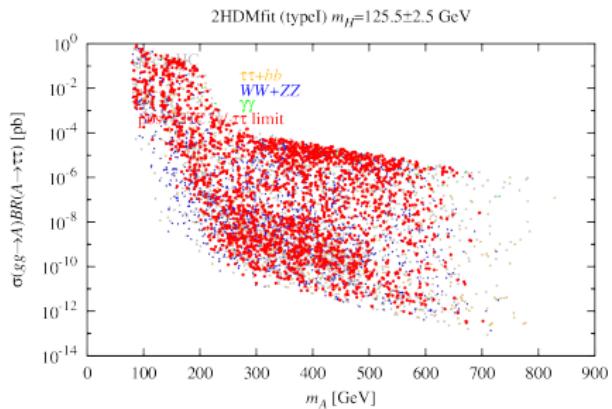
SAME pattern but the decoupling limit does NOT apply.

# $H \sim 125$ -light Higgs boson $h$ search



- $m_h \geq 60$  GeV with a few exception in which  $H \rightarrow hh$  decay opens.  $BR(H \rightarrow hh)$  at most 20 (10)% in Type I (II) to fit the LHC signals.
- Expected rates for most points are obviously too small to allow the detection of the  $h$ .
- But there are also allowed parameter choices for which detection in the  $\gamma\gamma$  final state and, especially, the  $Vh(bb)$  might prove possible with HL-LHC.

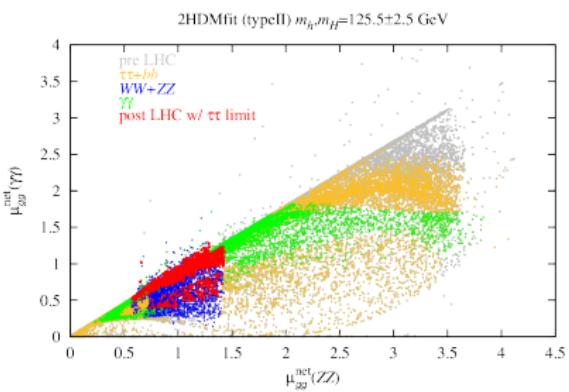
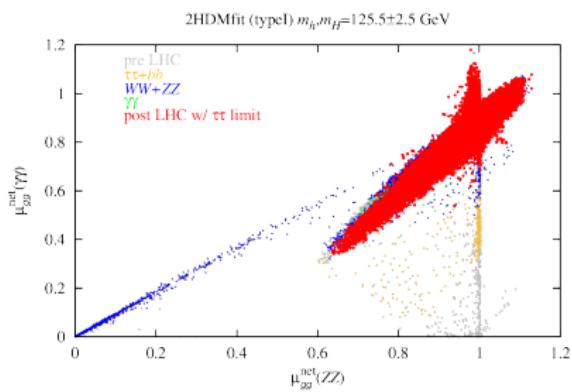
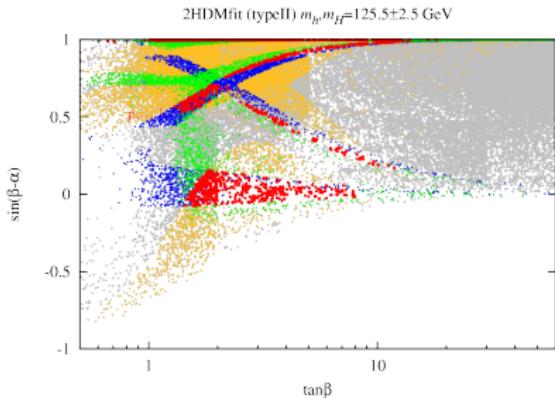
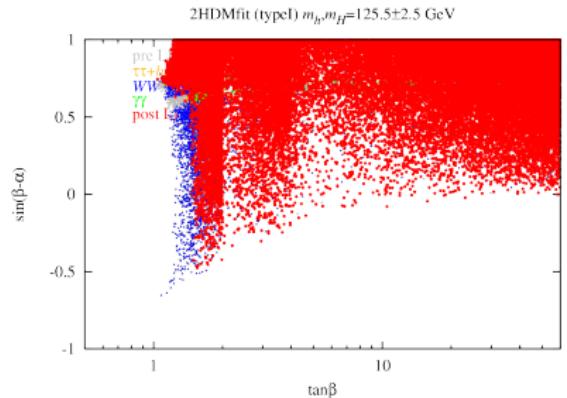
# $H \sim 125$ -Heavier Higgs boson $A$ search



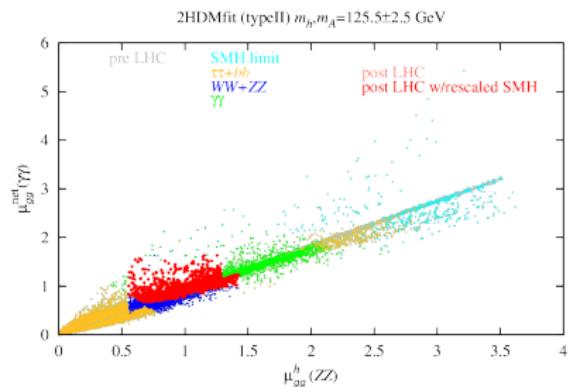
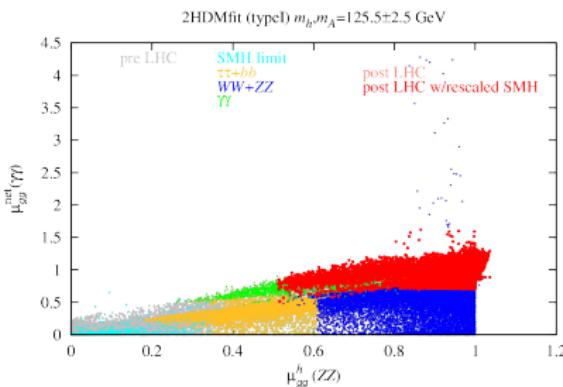
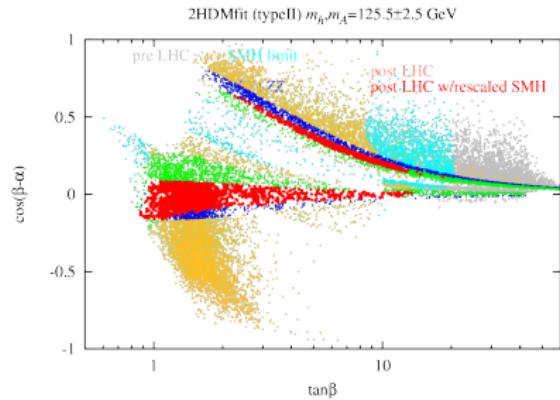
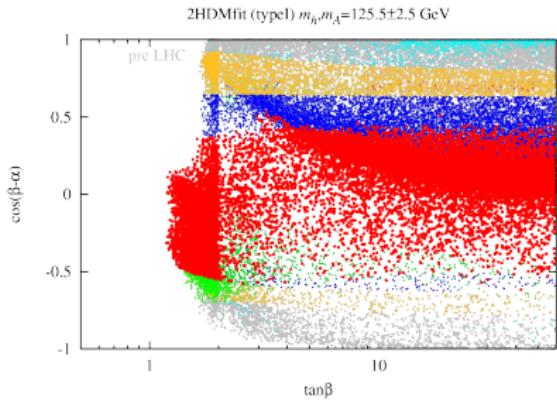
Is it possible that the excess in the  $H \rightarrow \gamma\gamma$  is due to two 2HDMs degenerate states?

Yes, the signal at 125 GeV cannot be pure  $A$  since at the tree level the  $A$  does not couple to  $ZZ$ , a final state that is definitely present at 125 GeV.

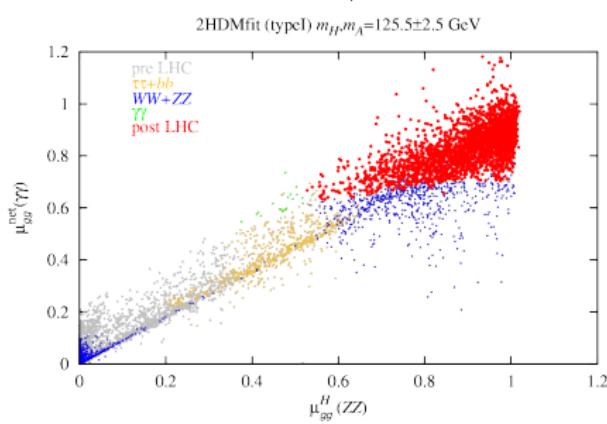
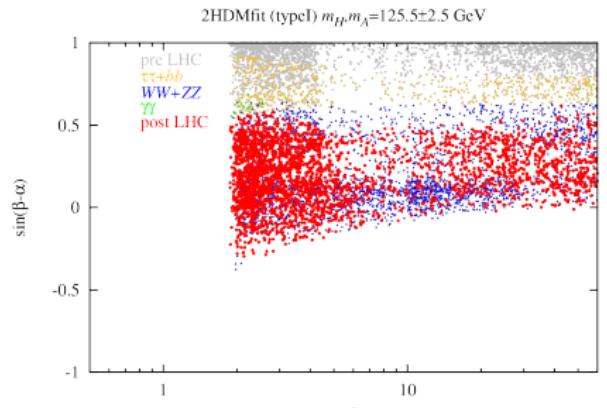
# $h, H \sim 125$ -Parameter and Signals



# $h, A \sim 125$ -Parameter and Signals



# $H, A \sim 125$ -Parameter and Signals



## Conclusions

- ➊ The latest Higgs data from LHC clearly favors a fairly SM-like Higgs boson with mass of 125.5 GeV.
- ➋ There is consistent descriptions with the LHC Higgs signal in the both Type I and Type II 2HDMs. The ratio  $\frac{\mu_{gg}(ZZ)}{\mu_{gg}(\gamma\gamma)}$  might be a possible signature to examine the Type I and II 2HDM if the diphoton rate is confirmed to be very SM-like or a bit enhanced in the future.
- ➌ The search associated with other (heavier) Higgs bosons is awaiting.
- ➍ More interesting conclusions about Higgs self-interactions is being studied, please stay tuned.
- ➎ 2HDM+singlet with a dark matter candidate is a natural extension which we (with Bohdan, Jack and Ola) are now working in progress.

*Thank you*

To me, 2012 was a productive year.  
It is just the start of my research career, wish your staying tuned.

# Back Up

## Stability condition in the 2HDM

Apparently,  $A$  matrix reduces to  $4 \times 4$  in the 2HDM for real  $\lambda_5$  and  $\lambda_6 = \lambda_7 = 0$ . In the basis  $a = H_1^\dagger H_1$ ,  $b = H_2^\dagger H_2$ ,  $c = \text{Re}(H_1^\dagger H_2)$ ,  $d = \text{Im}(H_1^\dagger H_2)$ ,

$$A = \begin{pmatrix} \frac{\lambda_1}{2} & \frac{\lambda_3}{2} & 0 & 0 \\ \frac{\lambda_3}{2} & \frac{\lambda_2}{2} & 0 & 0 \\ 0 & 0 & \lambda_4 + \lambda_5 & 0 \\ 0 & 0 & 0 & \lambda_4 - \lambda_5 \end{pmatrix} \quad (6)$$

Using the positivity condition on the root of a quadratic polynomial equation for upper left block, we obtain the conditions requiring all eigenvalues positive are

$$\begin{aligned} \lambda_1 + \lambda_2 &> 0 \\ \lambda_1 \lambda_2 - \lambda_3^2 &> 0 \\ \lambda_4 + \lambda_5 &> 0 \\ \lambda_4 - \lambda_5 &> 0 \end{aligned} \quad (7)$$

Or essentially,

$$\begin{aligned} \lambda_1, \lambda_2 &> 0 \\ -\sqrt{\lambda_1 \lambda_2} < \lambda_3 &< \sqrt{\lambda_1 \lambda_2} \\ \lambda_4 &> |\lambda_5| \end{aligned} \quad (8)$$

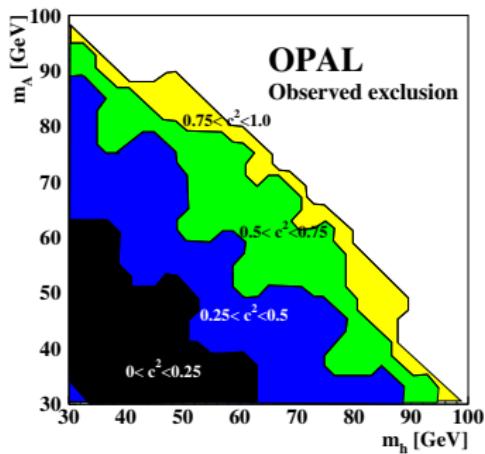
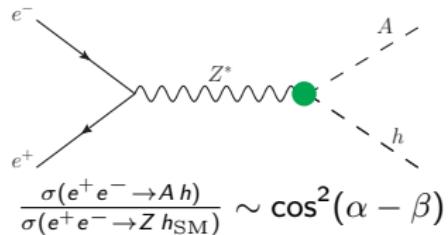
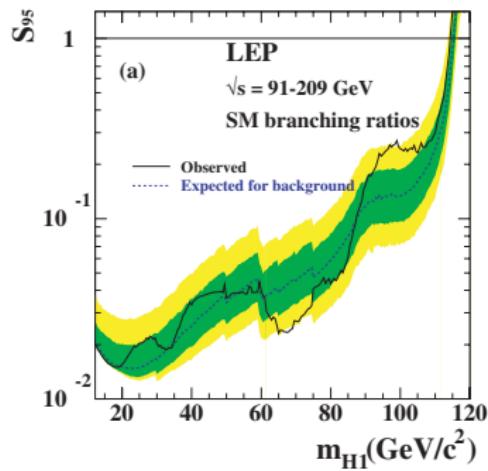
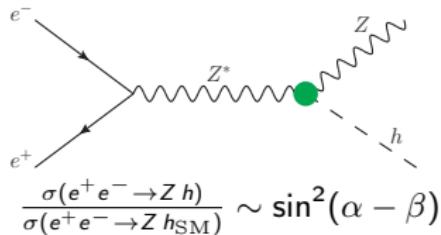
This combination seems to be a bit more strict than the ones adopted in most 2HDM papers.

$$\begin{aligned} \lambda_1 &> 0 \\ \lambda_2 &> 0 \\ \lambda_3 &> -\sqrt{\lambda_1 \lambda_2} \\ \lambda_3 + \lambda_4 - |\lambda_5| &> -\sqrt{\lambda_1 \lambda_2} \end{aligned} \quad (9)$$

Here  $\lambda_5$  is assumed to be real.

# Basic Constraints – LEP

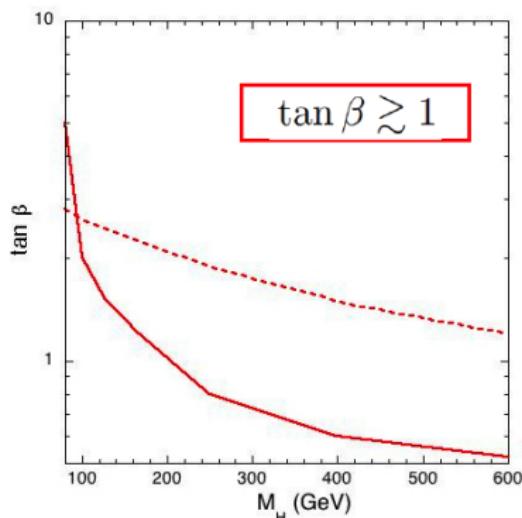
LEP constraints on Higgs mass limits



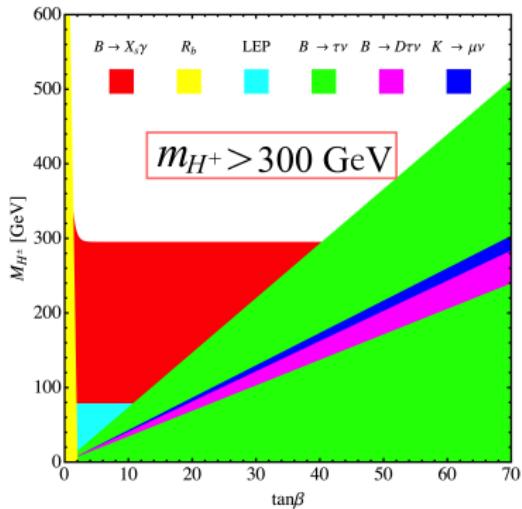
## Basic Constraints – $B$ -physics

$B$ -physics constraints ( $\text{BR}(B_s \rightarrow X_s \gamma)$ ,  $R_b$ ,  $\Delta M_{B_s}$ ,  $\epsilon_K$ ,  $\text{BR}(B^+ \rightarrow \tau^+ \nu_\tau)$  and  $\text{BR}(B^+ \rightarrow D \tau^+ \nu_\tau)$ ): set up lower bound on  $m_{H^\pm}$ .

Type I



Type II



Solid:  $R_b$  for  $Z \rightarrow b\bar{b}$ ,  $\epsilon_K$  and  $\Delta m_{B_s}$

Dash:  $\bar{B} \rightarrow X_s \gamma$  in models with FCNC

G. C. Branco et. al. Phys. Rept. 516 (2012) 1

# $\gamma\gamma - ZZ$ Correlation Analysis

A. Drozd, B. Grzadkowski, J. F. Gunion and YJ, JHEP 05(2013)072

$$r_s \equiv \frac{R_{gg}^s(\gamma\gamma)}{R_{gg}^s(ZZ)} = \frac{\Gamma(s \rightarrow \gamma\gamma)/\Gamma(h_{SM} \rightarrow \gamma\gamma)}{\Gamma(s \rightarrow ZZ)/\Gamma(h_{SM} \rightarrow ZZ)}$$

$$r_s \simeq \frac{(C_{WW}^s)^2}{(C_{ZZ}^s)^2} \left( \frac{\mathcal{A}_W^{SM} - \frac{C_{t\bar{t}}^s}{C_{WW}^s} \mathcal{A}_t^{SM} + \mathcal{A}_{H^\pm} \text{term}}{\mathcal{A}_W^{SM} - \mathcal{A}_t^{SM}} \right)^2 = \left( \frac{\mathcal{A}_W^{SM} - \frac{C_{t\bar{t}}^s}{C_{WW}^s} \mathcal{A}_t^{SM}}{\mathcal{A}_W^{SM} - \mathcal{A}_t^{SM}} \right)^2$$

$$r_s < 1 \implies 1 < \frac{C_{t\bar{t}}^s}{C_{WW}^s} < 2 \frac{\mathcal{A}_W^{SM}}{\mathcal{A}_t^{SM}} - 1 \simeq 9$$

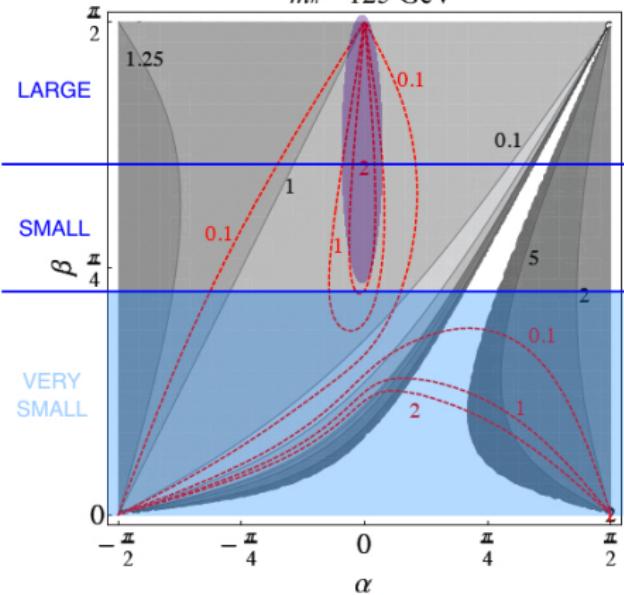
When  $C_{t\bar{t}}^s/C_{WW}^s$  is outside of the above interval then  $r_s > 1$ .

# $\gamma\gamma - ZZ$ Correlation Analysis (in Type II 2HDM)

A. Drozd, B. Grzadkowski, J. F. Gunion and YJ, JHEP 05(2013)072

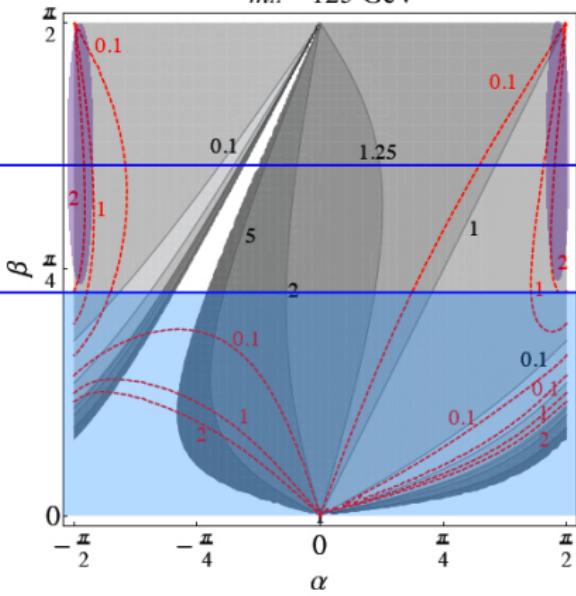
$$\frac{C_{t\bar{t}}^h}{C_{WW}^h} = \frac{\cos \alpha}{\sin \beta \sin(\beta-\alpha)}$$

$m_h = 125$  GeV



$$\frac{C_{t\bar{t}}^h}{C_{WW}^h} = \frac{\sin \alpha}{\sin \beta \cos(\beta-\alpha)}$$

$m_h = 125$  GeV



Red numbers give values of  $R_{gg}^s(\gamma\gamma)$  while black ones show constant  $r_s$  values.

The white region correspond to  $r_s > 10.75$ .