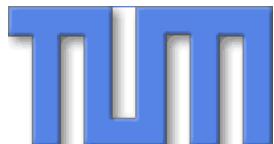


# Towards the Zeptouniverse with the Help of Correlations between Flavour Observables

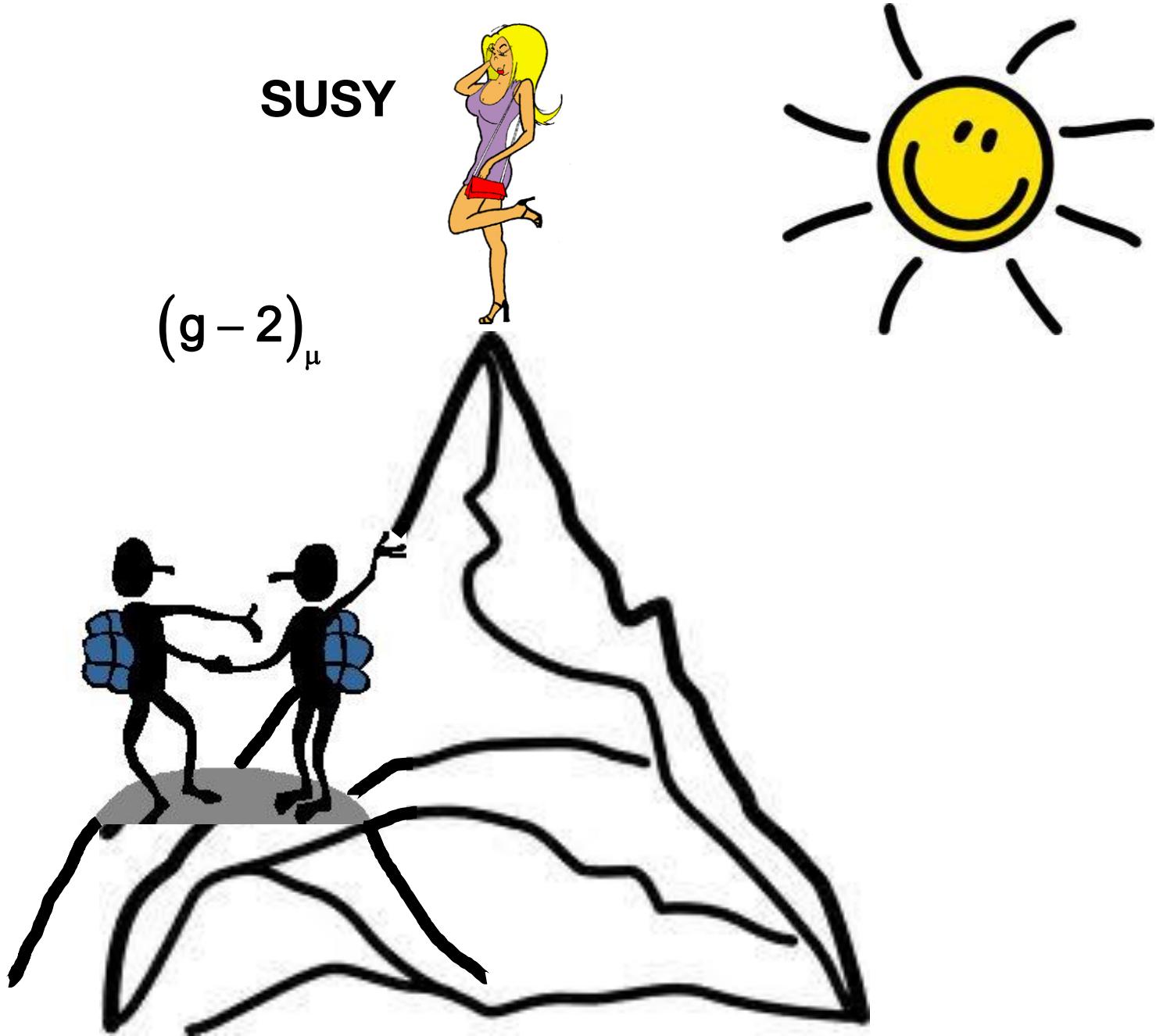


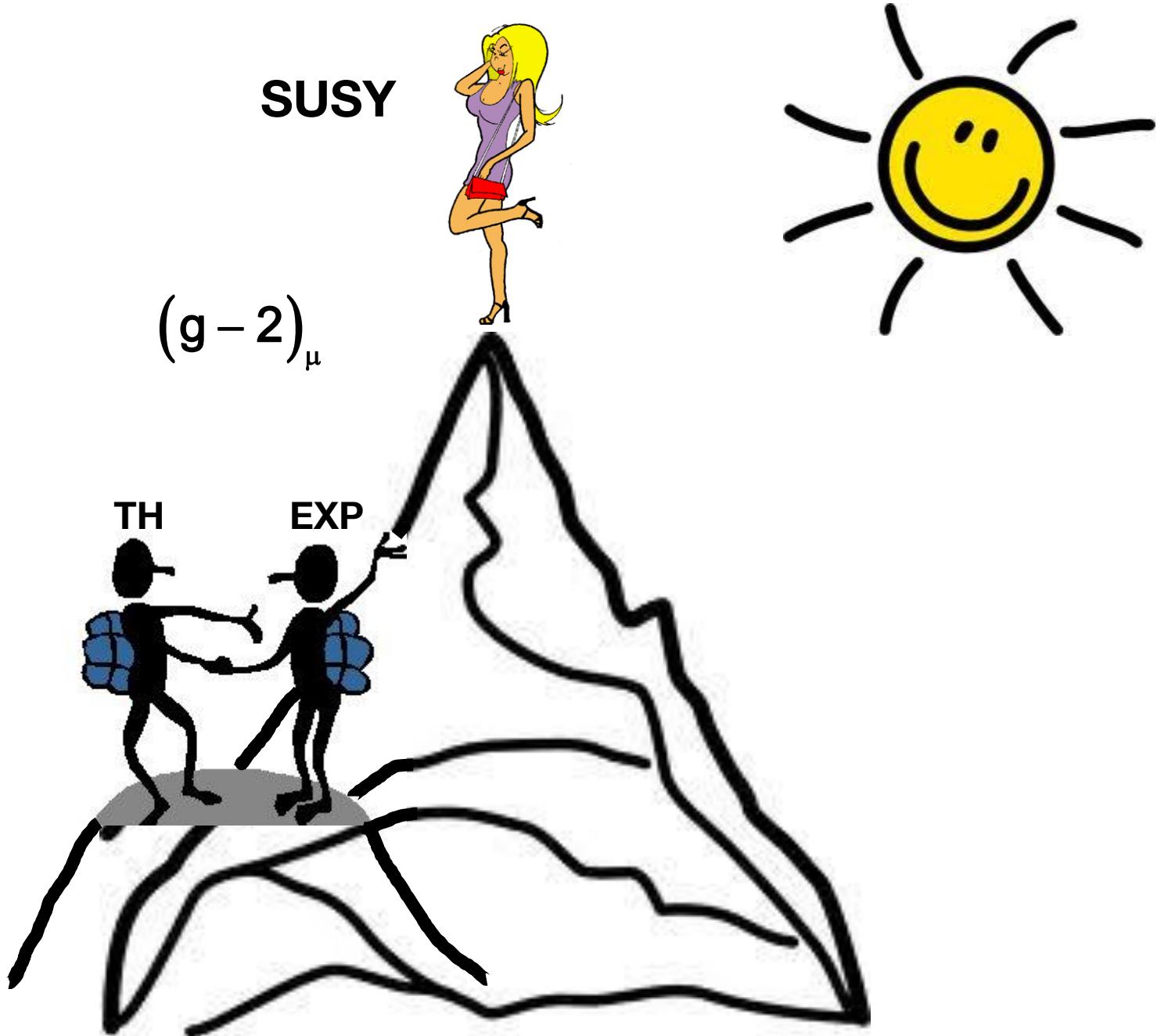
*Andrzej J. Buras*  
*(Technical University Munich, TUM-IAS)*

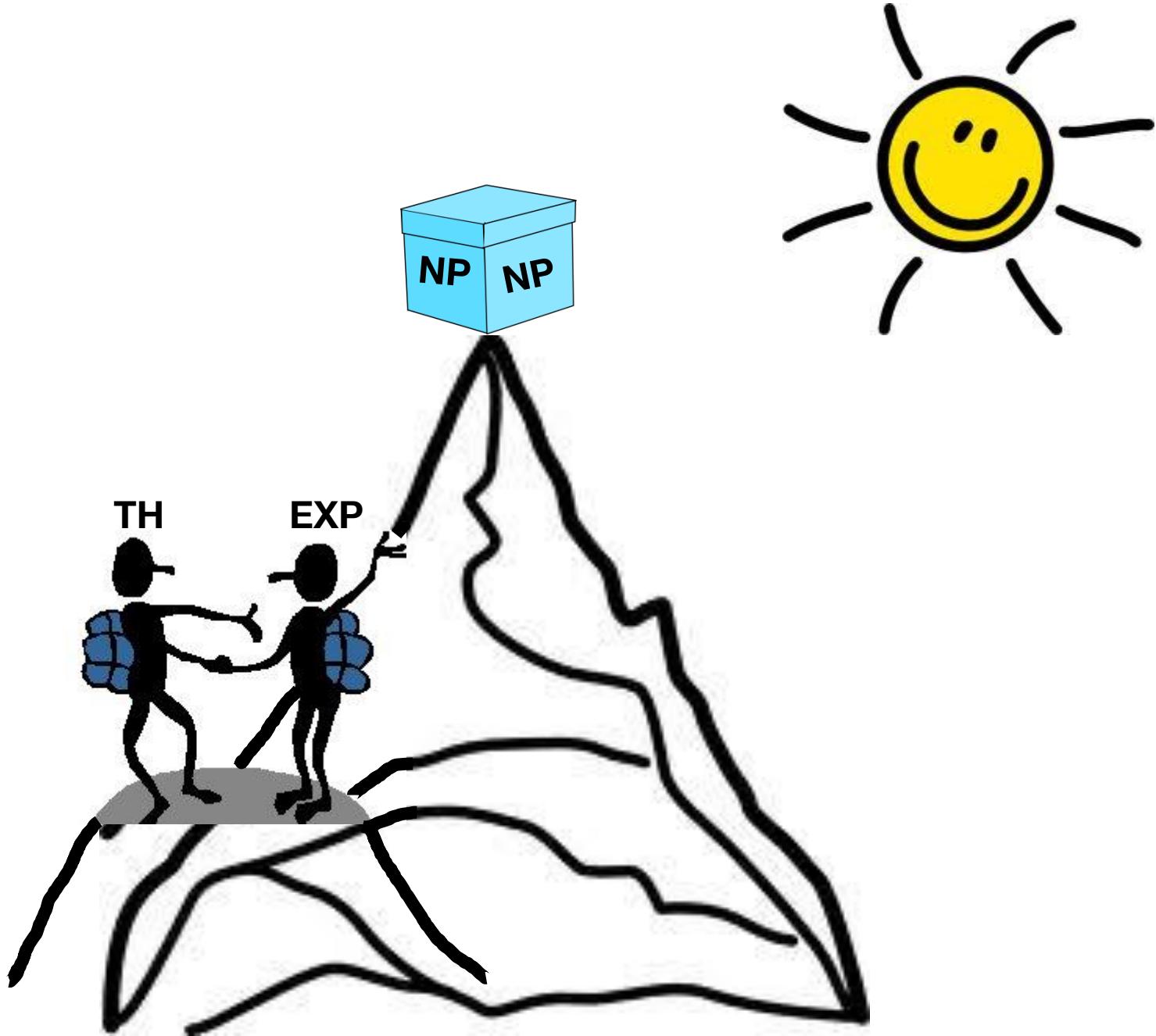


**Warsaw**  
**September 2013**





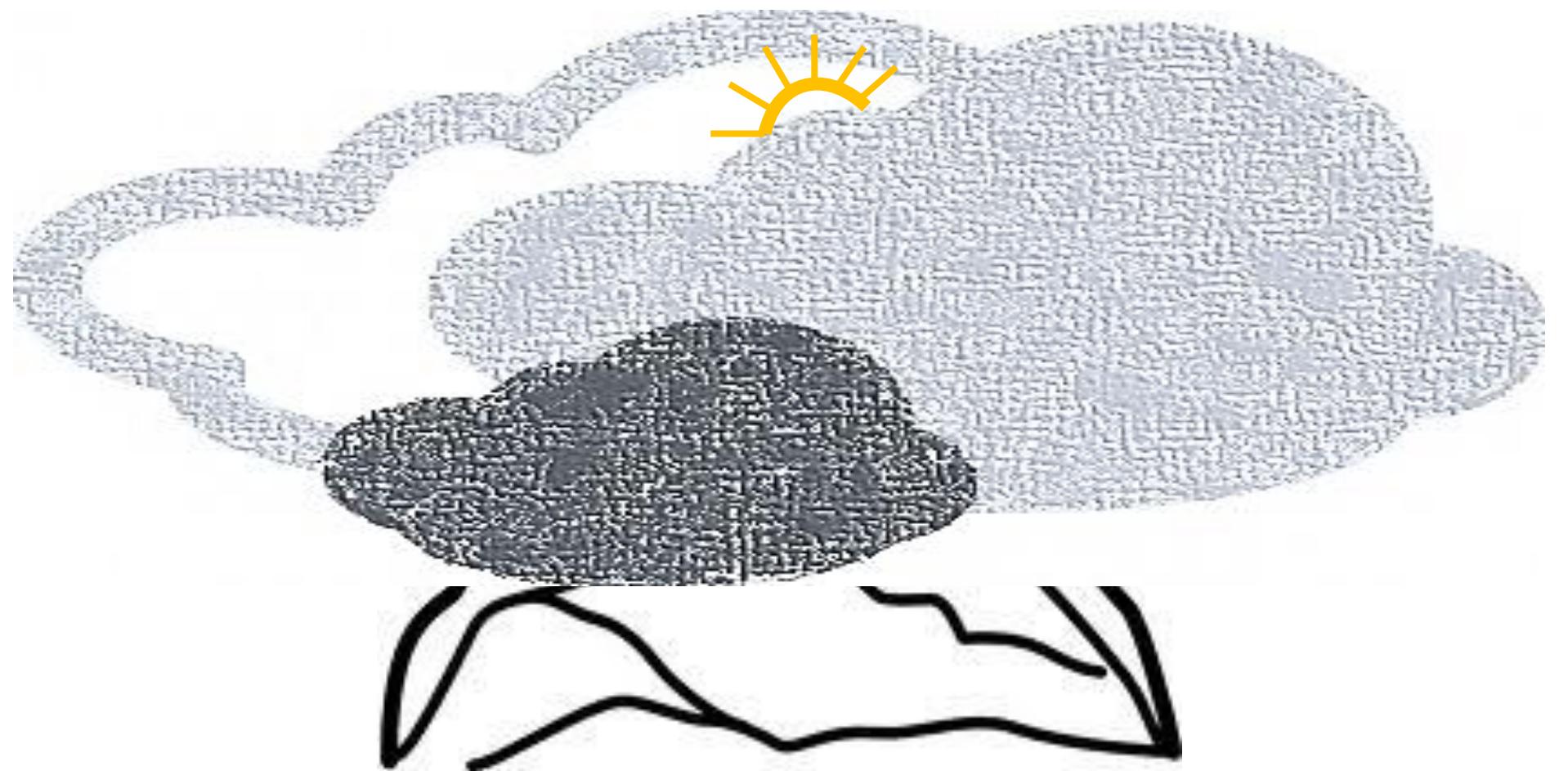




**June 2013**



**July 2013**



# EPS 2013 Flavour Highlights

1.

$$\frac{\text{Br}(B_d \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)} \approx (4.3 \pm 1.8) \left[ \frac{\text{Br}(B_d \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)} \right]_{\substack{\text{SM} \\ \text{CMFV}}}^{}$$

(LHCb, CMS)

2.

Anomalies in angular observables in  
 $B_d \rightarrow K^* \mu^+ \mu^-$  (LHCb)

3.

$B \rightarrow D^* \tau \nu$  (not in this talk)

# New Physics beyond the SM must exist !!!



**It is our duty to find it.  
If not at the LHC then through  
high precision experiments.**



**Quark Flavour Physics  
Lepton Flavour Violation  
EDMs +  $(g-2)_{\mu,e}$**

# A Journey to the Very Short Distance Scales:

1676 - 2046

Microuniverse

$10^{-6}\text{m}$

Bacteriology  
Microbiology

Nanouniverse

$10^{-9}\text{m}$

Nanoscience

Femtouniverse

$10^{-15}\text{m}$

Nuclear Physics  
Low Energy Elementary  
Particle Physics

Attouniverse

$10^{-18}\text{m}$

High Energy Particle  
Physics (present)

High Energy Proton-Proton  
Collisions at the LHC

$5 \cdot 10^{-20}\text{m}$

Frontiers of Elementary  
Particle Physics in 2010's

High Precision Measurements  
of Rare Processes (Europe,  
Japan, USA)

$10^{-21}\text{m}$

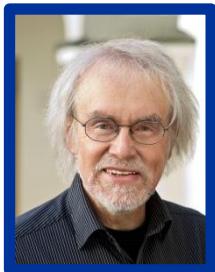
Zeptouniverse



# Advanced ERC Grant at the TUM Institute for Advanced Study Zeptouniverse Base Camp



# ERC Flavour Team



AJB



D. Buttazzo



F. De Fazio



J. Drobnak



K. Gemmeler



J. Girrbach



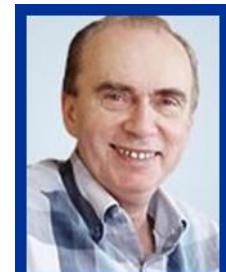
G. Isidori



L. Merlo



Y. Omura



S. Pokorski



E. Stamou



R. Ziegler



G. Buchalla



A. Ibarra



M. Ratz

# In Order to identify New Physics through Flavour Physics

We need

- 1.** Many precision measurements of many observables and precise theory.
- 2.** Study Patterns on Flavour Violation in various New Physics models (correlations between many flavour observables).

...and

3.

### **Correlations between low energy flavour observables and Collider Physics (LHC, Tevatron)**

**Here top-down approach more  
powerful in flavour physics**

## Patterns of Flavour Violation around the Flavour Clock

12  
11  
10  
9  
8  
7  
6  
5  
4  
3  
2  
1

$RS_c$

Gauged  
Flavour  
Models

CMFV, MFV

L-R Models

2HDM $\overline{\text{MFV}}$

RHMVF

LHT

FBMSSM

SM4

$U(2)^3$

SO(10)-GUT  
 $SSU(5)_{RN}$

SUSY  
Flavour

1012.1447  
1204.5065

1.

## Z' and Z FCNCs (tree level)

AJB, De Fazio, Girrbach: 1211.1896 (General)

AJB, De Fazio, Girrbach, Carlucci: 1211.1237 (331-Model)

AJB, Girrbach, Ziegler: 1301.5498 (Minimal Theory of Fermion Masses)

AJB, Girrbach, 1201.1302 (NLO QCD)

AJB, Girrbach, 1309.2466 (Facing new data)

2.

## Neutral Scalars FCNCs (tree level)

AJB, De Fazio, Girrbach, Knegjens, Nagai (1303.3723)

AJB, Girrbach, 1201.1302 (NLO QCD)

3.

## $B_{s,d} \rightarrow \mu^+ \mu^-$ Phenomenology

AJB, Fleischer, Girrbach, Knegjens (1303.3820)

AJB, Girrbach, Guadagnoli, Isidori (1208.0934)

# **Towards New SM in 12 Steps**

**AJB + Girrbach (1306.3755)**

# Towards New SM In 12 Steps

LFV, EDMs  
 $(g-2)_{\mu,e}$

CKM from  
Trees

$\epsilon'/\epsilon$

$B \rightarrow X_s v\bar{v}$   
 $B \rightarrow K^*(K)v\bar{v}$

$K \rightarrow \pi v\bar{v}$

$B \rightarrow X_s l^+l^-$   
 $B \rightarrow K^*(K)l^+l^-$

$B \rightarrow X_s \gamma$   
 $B \rightarrow K^* \gamma$

Lattice

$\Delta F=2$   
Observables

$B_{s,d} \rightarrow \mu^+\mu^-$   
 $B_{s,d} \rightarrow \tau^+\tau^-$

$B^+ \rightarrow \tau^+ \nu_\tau$

Charm  
Top

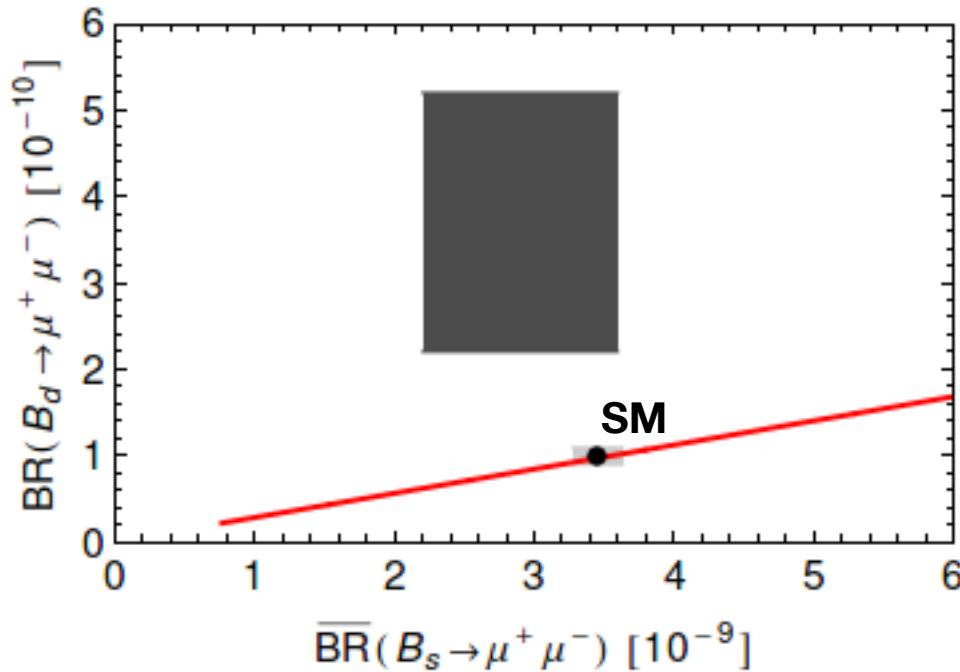
10  
9  
8  
7  
6  
5  
4  
3  
2  
1  
11  
12

# **Simplest Correlations**

# Constrained Minimal Flavour Violation

AJB

Hurth, Isidori, Kamenik, Mescia



$$\bar{Br}(B_s \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7) \cdot 10^{-9}$$

(LHCb + CMS)

**Golden Relation**

$$\frac{Br(B_s \rightarrow \mu^+ \mu^-)}{Br(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_d}{\hat{B}_s} \frac{\tau(B_s)}{\tau(B_d)} \frac{\Delta M_s}{\Delta M_d}$$

AJB 2003

$$\hat{B}_d / \hat{B}_s \simeq 0.99 \pm 0.02 \quad (\text{tmQCD})$$

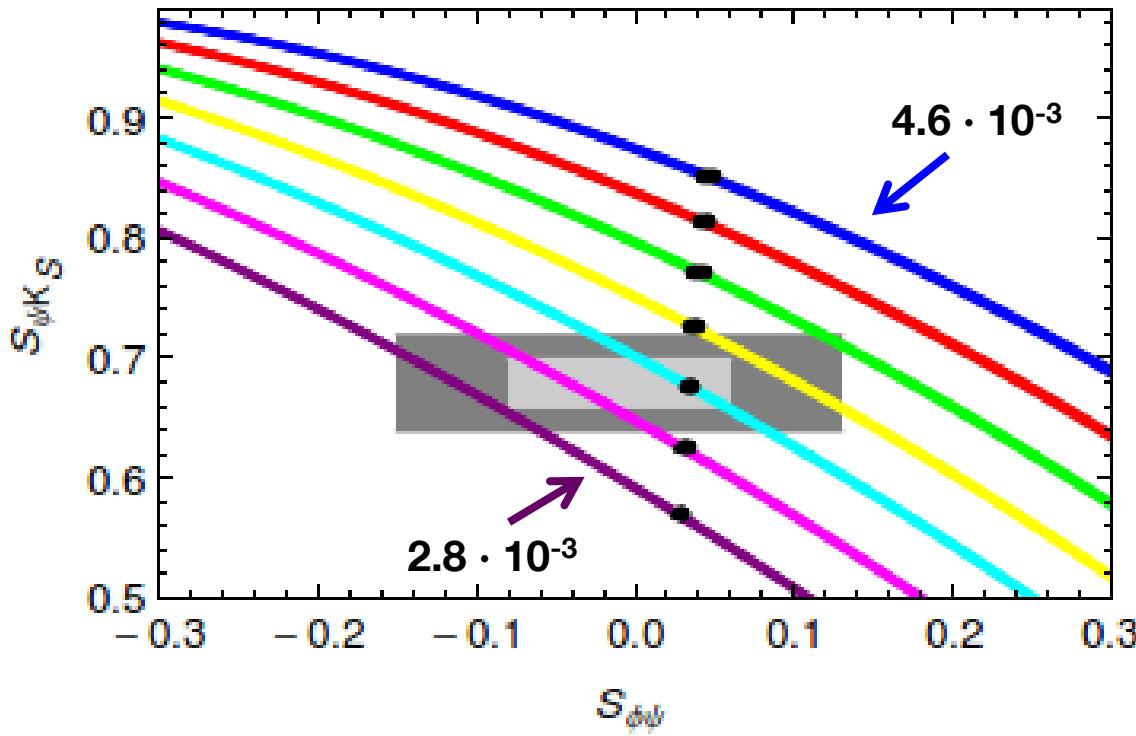
No CKM

No weak decay constants

$$Br(B_d \rightarrow \mu^+ \mu^-) = \left( 3.6 \begin{array}{l} +1.6 \\ -1.4 \end{array} \right) \cdot 10^{-10}$$

# $S_{\psi K_s} - S_{\psi\phi} - |V_{ub}|$ Correlation in $U(2)^3$

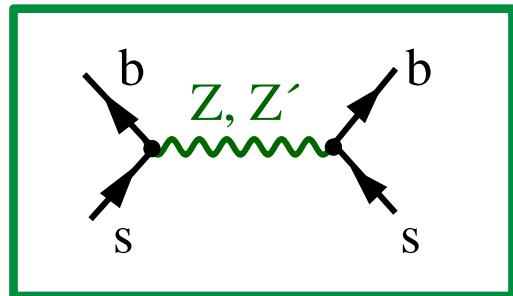
Important test of  $U(2)^3$  Models



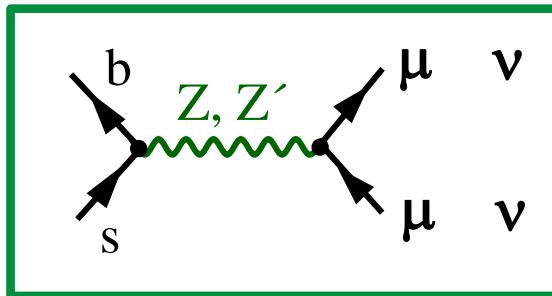
In the  $U(2)^3$  Symmetric World we could determine  $|V_{ub}|$  without significant hadronic uncertainties (QCD penguins)

# **Correlations between Flavour Observables in Tree Level FCNCs**

# Basics of Correlations in Tree-Level (Z,Z') FCNCs



$$\Delta F = 2$$



$$\Delta F = 1$$

$$M_Z \\ M_{Z'}$$

$Z, Z'$  couplings:

$$\Delta_{L,R}^{bs} \equiv \tilde{s}_{23} e^{-i\delta_{23}}$$

only two new quark parameters!

For fixed lepton couplings

$B_s^0$  :  $\Delta M_s, S_{\psi\phi}, B_s \rightarrow \mu^+ \mu^-, S_{\mu\mu}^s, B \rightarrow K^*(K)v\bar{v}, B \rightarrow X_s v\bar{v}, b \rightarrow sll$

$B_d^0$  :  $\Delta M_d, S_{\psi K_s}, B_d \rightarrow \mu^+ \mu^-, S_{\mu\mu}^d \quad \leftarrow \quad \Delta_{L,R}^{bd} \equiv \tilde{s}_{13} e^{-i\delta_{13}} \quad \Delta_{L,R}^{sd} \equiv \tilde{s}_{12} e^{-i\delta_{12}}$

$K$  :  $\epsilon_K, K^+ \rightarrow \pi^+ v\bar{v}, K_L \rightarrow \pi^0 v\bar{v}, K_L \rightarrow \mu^+ \mu^-, K_L \rightarrow \pi^0 l^+ l^-, \epsilon'/\epsilon \quad \leftarrow$

# Correlations depend strongly on the allowed Size of NP Contributions

SM

Data

$\Delta M_s$	$(18.0 \pm 1.8) / \text{ps}$	$17.7 / \text{ps}$	
$S_{\psi\phi}$	0.04	$-0.15 \leq S_{\psi\phi} \leq 0.15$	95% C.L.
$\bar{B}\text{r}(B_s \rightarrow \mu^+ \mu^-)$	$(3.5 \pm 0.2) \cdot 10^{-9}$	$(2.9 \pm 0.7) \cdot 10^{-9}$	

$\Delta M_d$	$(0.52 \pm 0.05) / \text{ps}$	$0.51 / \text{ps}$	
$S_{\psi K_s}$	0.67 (excl. $V_{ub}$ ) (S1)	$0.68 \pm 0.02$	
	0.81 (incl. $V_{ub}$ ) (S2)	$0.68 \pm 0.02$	
$B\text{r}(B_d \rightarrow \mu^+ \mu^-)$	$(1.1 \pm 0.1) \cdot 10^{-10}$	$(3.6 \pm 1.5) \cdot 10^{-10}$	

$\epsilon_K$	$1.80 \cdot 10^{-3}$ (excl. $V_{ub}$ ) (S1)	$2.23 \cdot 10^{-3}$	
	$2.20 \cdot 10^{-3}$ (incl. $V_{ub}$ ) (S2)	$2.23 \cdot 10^{-3}$	

## Lessons from Z' Studies

1.

All tensions in  $\Delta F=2$  observables can be removed.

2.

The present data on  $B_{s,d} \rightarrow \mu^+ \mu^-$  and  $B_d \rightarrow K^* \mu^+ \mu^-$  can be reproduced with  $M_{Z'} \sim 0$  (few TeV)

But:  $K^+ \rightarrow \pi^+ v\bar{v}$  and  $K_L \rightarrow \pi^0 v\bar{v}$  still  
sensitive to  $M_{Z'} \approx 10 - 20$  TeV



## Lessons from Z Studies

1.

Data on  $Br(B_{s,d} \rightarrow \mu^+ \mu^-)$  can be understood but not

$B_d \rightarrow K^* \mu^+ \mu^-$  (vector coupling to  $\mu^+ \mu^-$  too small)

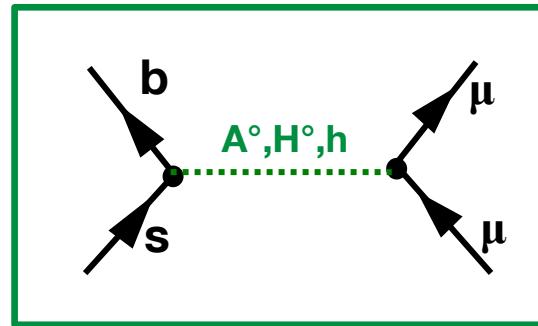
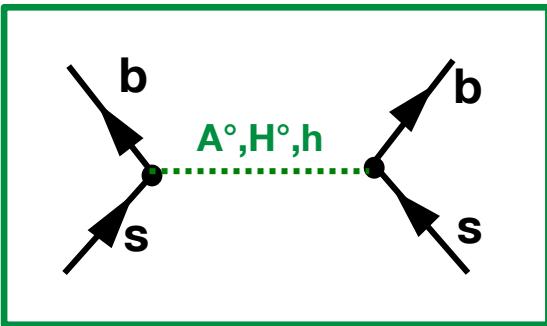
2.

$K^+ \rightarrow \pi^+ v\bar{v}$  and  $K_L \rightarrow \pi^0 v\bar{v}$  : much larger effects than for  $Z'$ .

(Bounded by  $K_L \rightarrow \mu^+ \mu^-$ )

# Lessons from Tree-Level ( $A^\circ$ , $H^\circ$ , $h$ ) FCNC's

(pseudo) scalar SM Higgs



1.

Correlations between  $\Delta F=1$  and  $\Delta F=2$  observables for  $A^\circ$  differ from  $Z'$  case because of pseudoscalar coupling  $i\gamma_5$ .

2.

Correlations between  $\Delta F=1$  and  $\Delta F=2$  observables for  $H^\circ$  differ from  $Z'$  case because of absence of interference with SM part.  
(only enhancements of branching ratios possible)

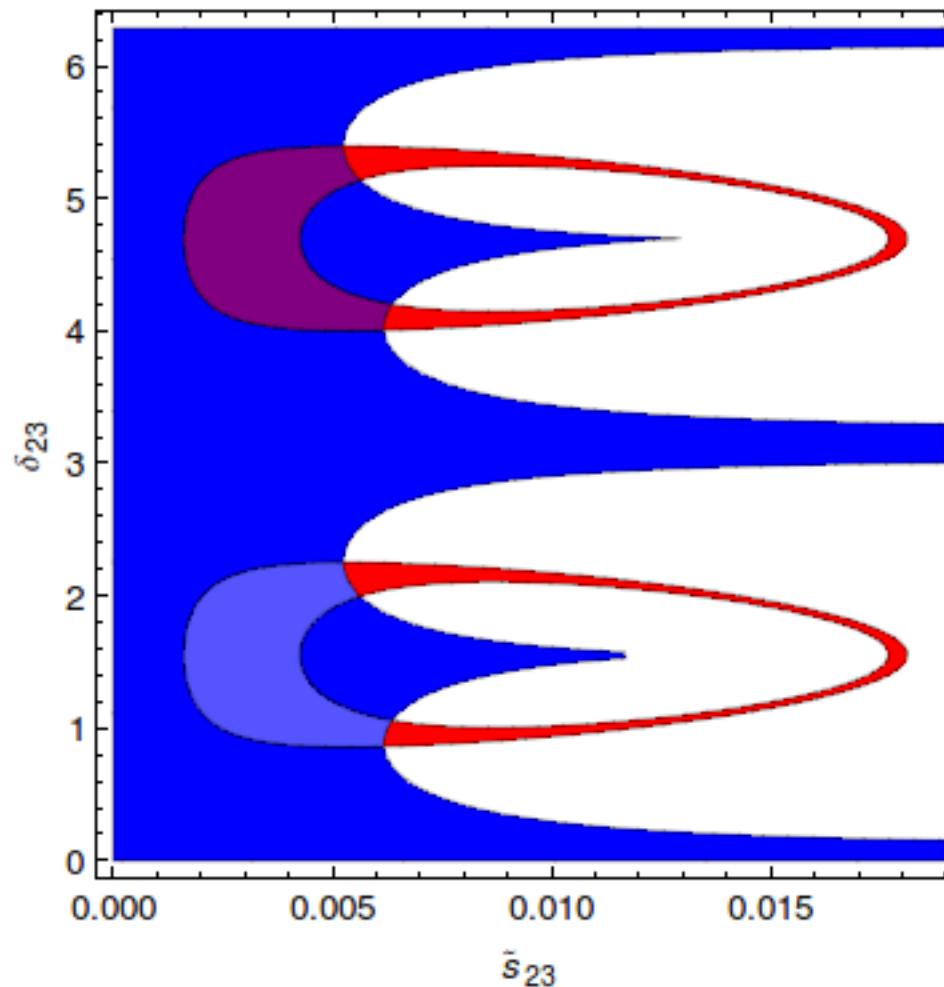
3.

SM Higgs contributions to  $\Delta F=1$  transitions negligible once  $\Delta F=2$  constraints satisfied because of small  $\mu\mu$  coupling.

# Oases in $B_s$ -System

 $\Delta M_s$  $S_{\psi\phi}$ 

$\Delta M_s$  &  $S_{\psi\phi}$ , LHS1



$$\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-), S_{\mu\mu}^s, \text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-), S_{\mu\mu}^d$$

**SM**

**Data (LHCb)**

$\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-) : (3.56 \pm 0.18) \cdot 10^{-9}$	$(2.9 \pm 0.7) \cdot 10^{-9}$
$\text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-) : (1.05 \pm 0.07) \cdot 10^{-10}$	$(3.6^{+1.6}_{-1.4}) \cdot 10^{-10}$

$$S_{\mu\mu}^s = S_{\mu\mu}^d = 0$$

De Bruyn, Fleischer, Knegjens et al. (1204.1735; 1204.1737)  
AJB, Fleischer, Girrbach, Knegjens (1303.3820)  
AJB, Girrbach, Guadagnoli, Isidori (1208.0934)

$$S_{\psi\phi} = 0.035 \pm 0.002$$

$$S_{\psi\phi} = -0.01 \pm 0.07$$

**Still New Physics could be discovered in these observables, in particular through correlations between them.**



# Historical Remarks

The first  
NLO QCD  
Calculation  
of  $B_{s,d} \rightarrow \mu^+ \mu^-$

Buchalla + AJB (Nucl. Phys. B400 (1993) 225)

- Reduction of  $\mu_t$  dependence in  $m_t(\mu_t)$
- Finding missing factor of two in branching ratios.



Values of  $\text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 3 - 4 \cdot 10^{-9}$

were  
with us  
for last  
15 years

$\text{Br}(B_d \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 1 \cdot 10^{-10}$

Theoretical Improvements  
over years

: Buchalla, AJB; Misiak, Urban (~1998)

September  
2013

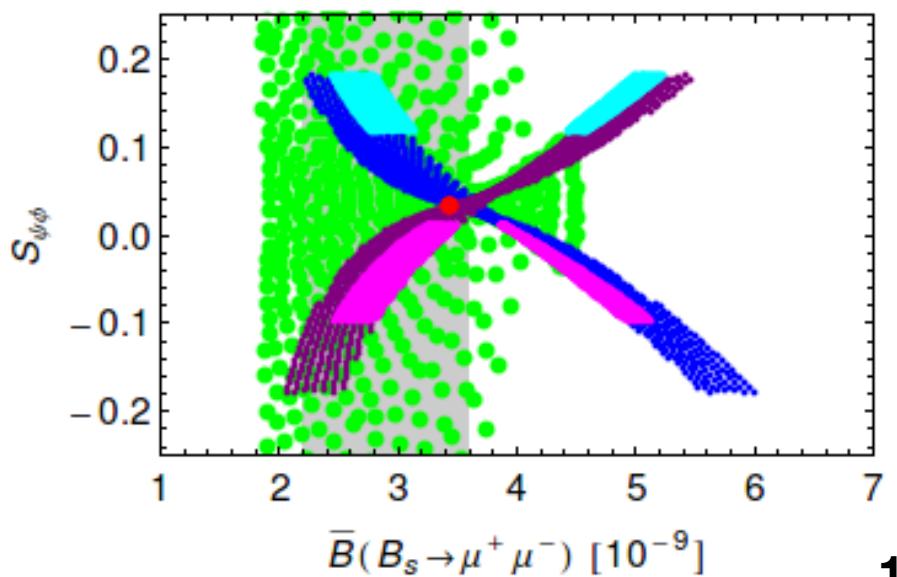
Recently: full NLO Electroweak, NNLO QCD

Bobeth, Gorbahn, Hermann, Misiak, Stamou, Steinhauser

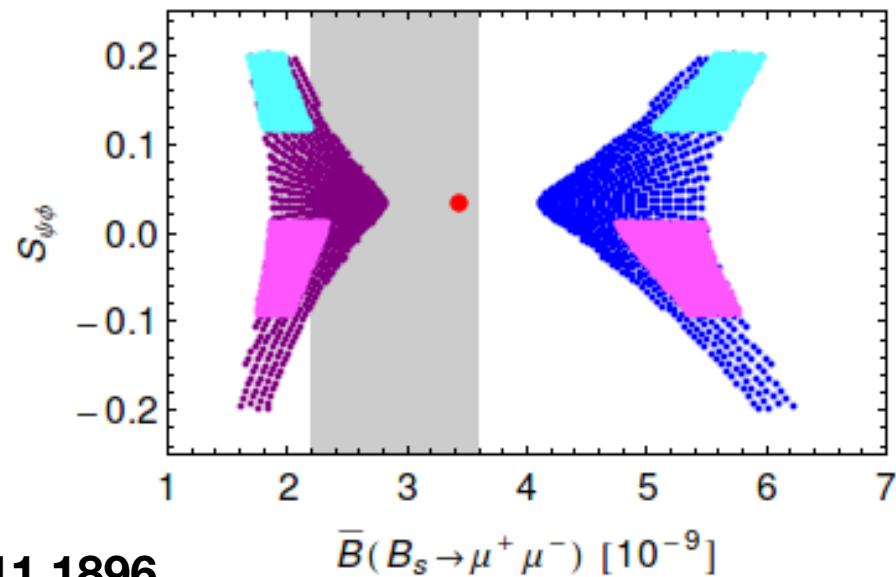
$$\text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = ( \quad \pm 0.16(\text{par}) \pm 0.02(\text{theo}) ) \cdot 10^{-9}$$

$$\text{Br}(B_d \rightarrow \mu^+ \mu^-)_{\text{SM}} = ( \quad \pm 0.07(\text{par}) \pm 0.01(\text{theo}) ) \cdot 10^{-10}$$

LHS &  $Z'$



LHS &  $A^0$



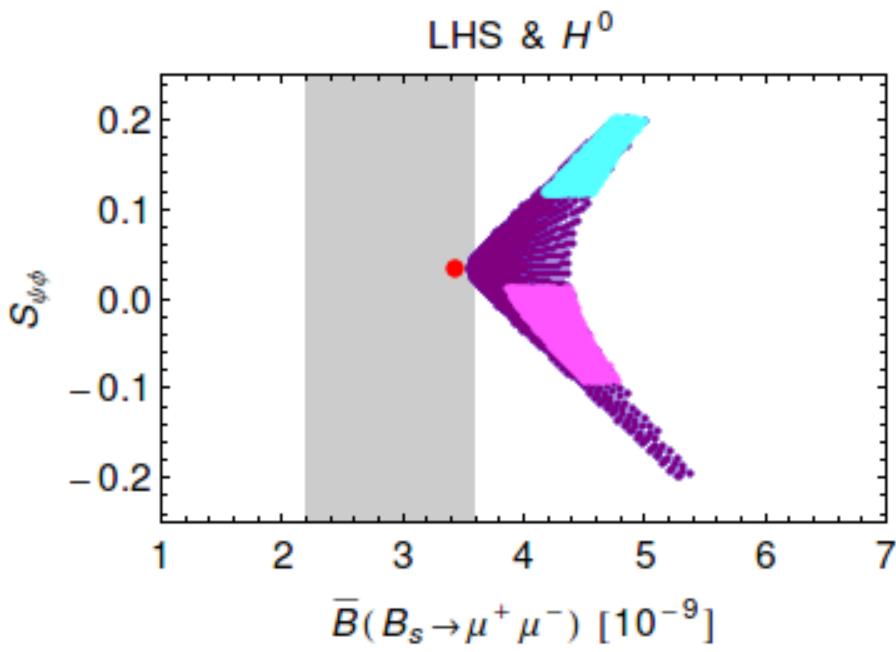
$$S_{\psi K_s} - B_s \rightarrow \mu^+ \mu^-$$

Correlations for  
 $Z'$ ,  $A^0$ ,  $H^0$

1 TeV

: allowed by  $b \rightarrow sll$

$\left. \begin{array}{c} \text{---} \\ \text{---} \end{array} \right\} U(2)^3$

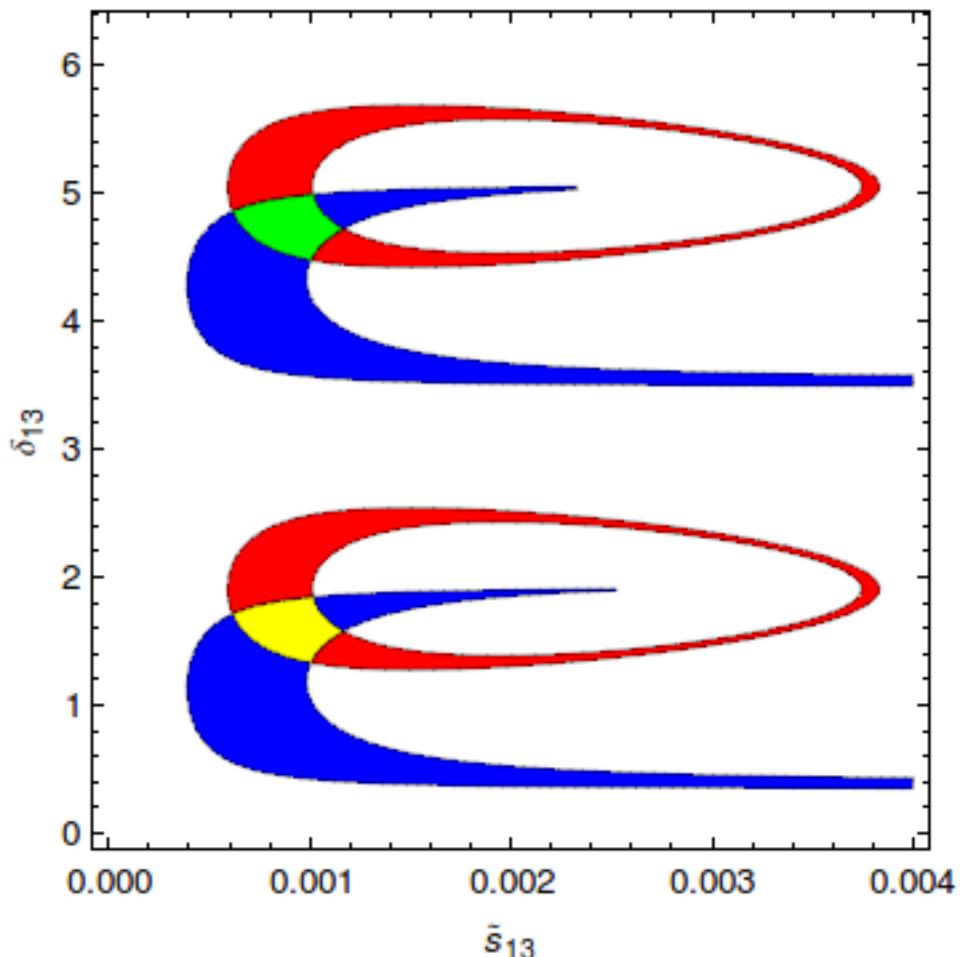


# Oases in $B_d$ -System

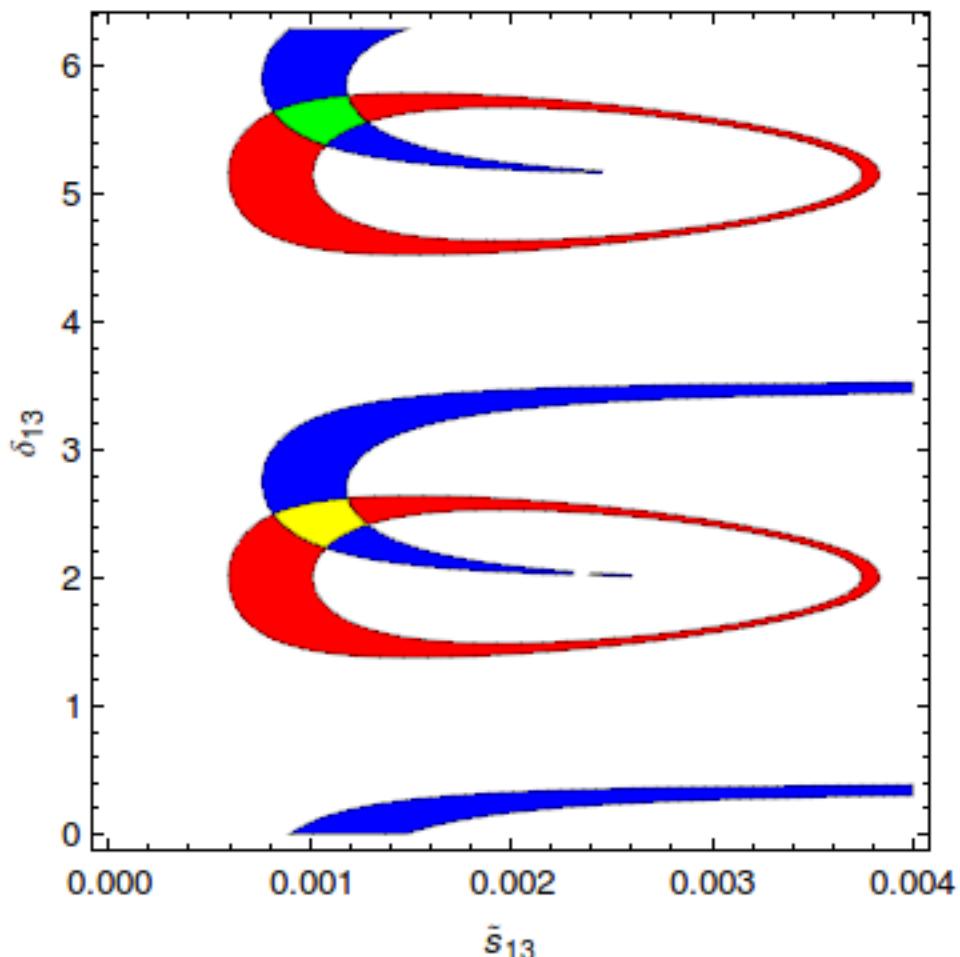
■  $\Delta M_d$

■  $S_{\psi K}$

$\Delta M_d$  &  $S_{\psi K_S}$ , LHS1

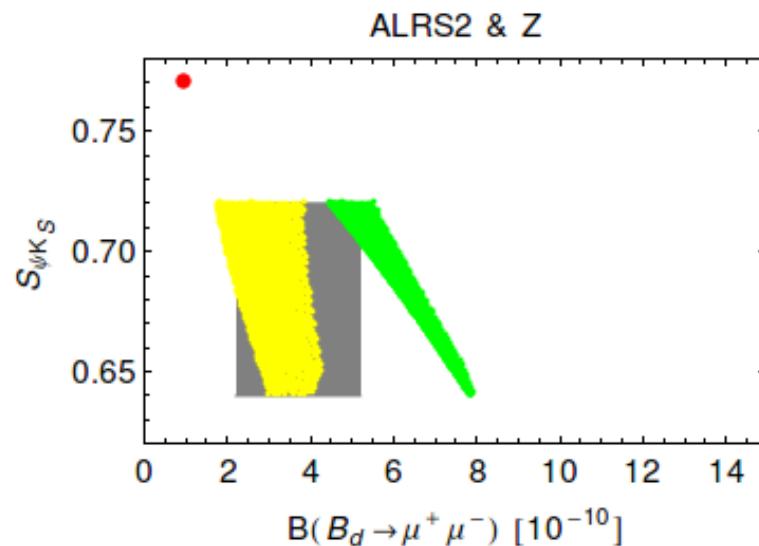
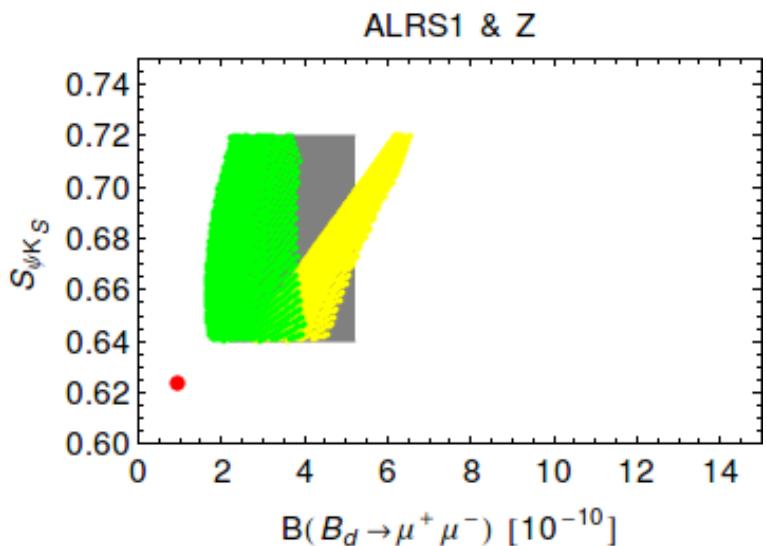
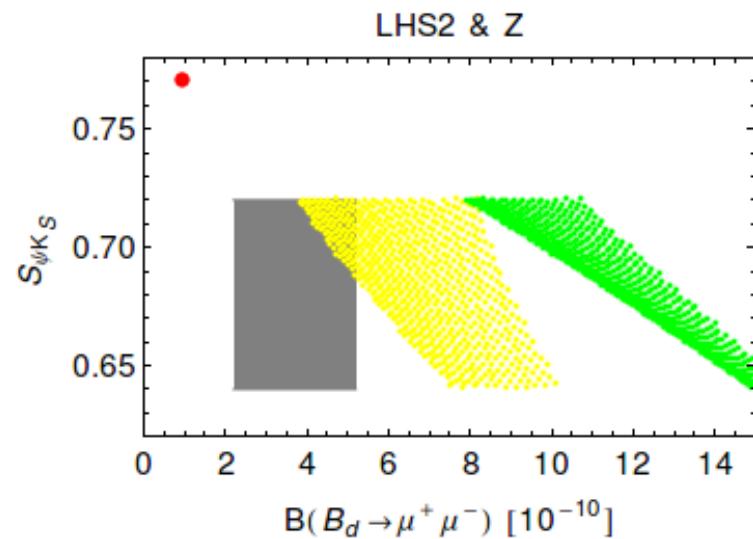
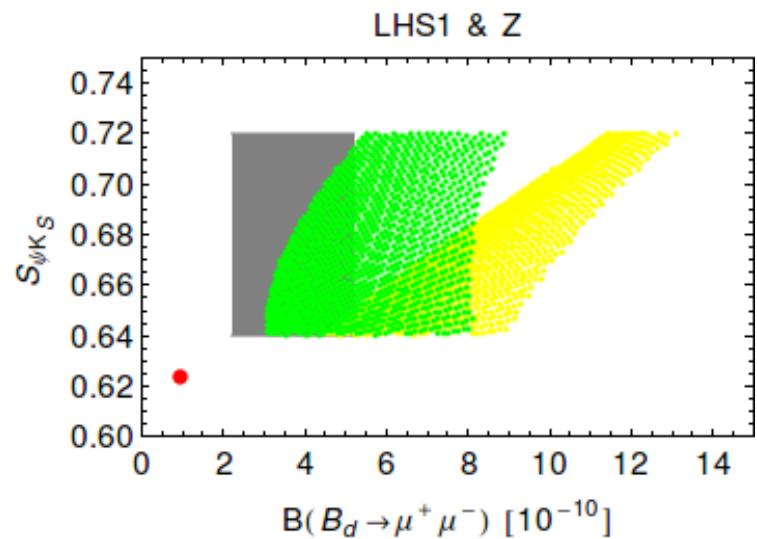


$\Delta M_d$  &  $S_{\psi K_S}$ , LHS2



$S_{\psi K_s} - B_d \rightarrow \mu^+ \mu^-$  Correlation for Z  
 "Confirmation" by LHCb + CMS

NP-effects can still be large !



$$|V_{ub}| = 3.1 \cdot 10^{-3}$$

$$|V_{ub}| = 4.0 \cdot 10^{-3}$$

# Left-handed Z' and Z FCNC Couplings Facing New $B_{s,d} \rightarrow \mu^+ \mu^-$ Data

Correlation  
with  
 $\Delta F=2$

(AJB + Girrbach, 1309.2466)

Both branching ratios can be put to agree with CMS + LHCb for Z and Z'

Z'

Favoured :

$$\frac{\Delta M_s}{(\Delta M_s)_{SM}} \approx 1.00 \pm 0.01 \quad \frac{\Delta M_d}{(\Delta M_d)_{SM}} \approx 1.04 \pm 0.01$$
$$S_{\psi\varphi} \neq (S_{\psi\varphi})_{SM} \quad \text{coupling} \rightarrow \frac{\Delta_A^{\mu\bar{\mu}}(Z')}{M_{Z'}} \approx \frac{1.0 - 2.0}{1\text{TeV}}$$

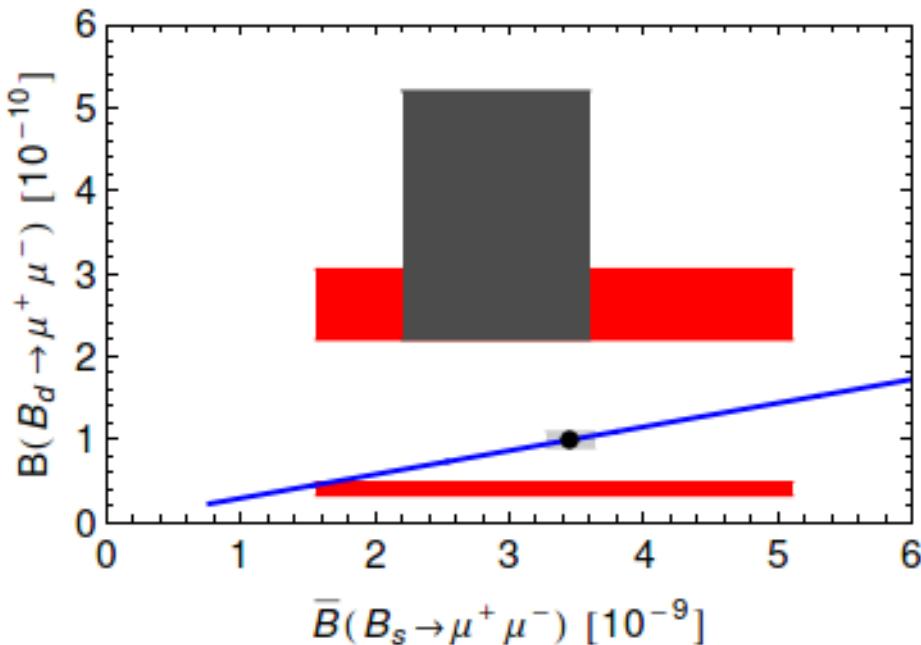
Z

Favoured :

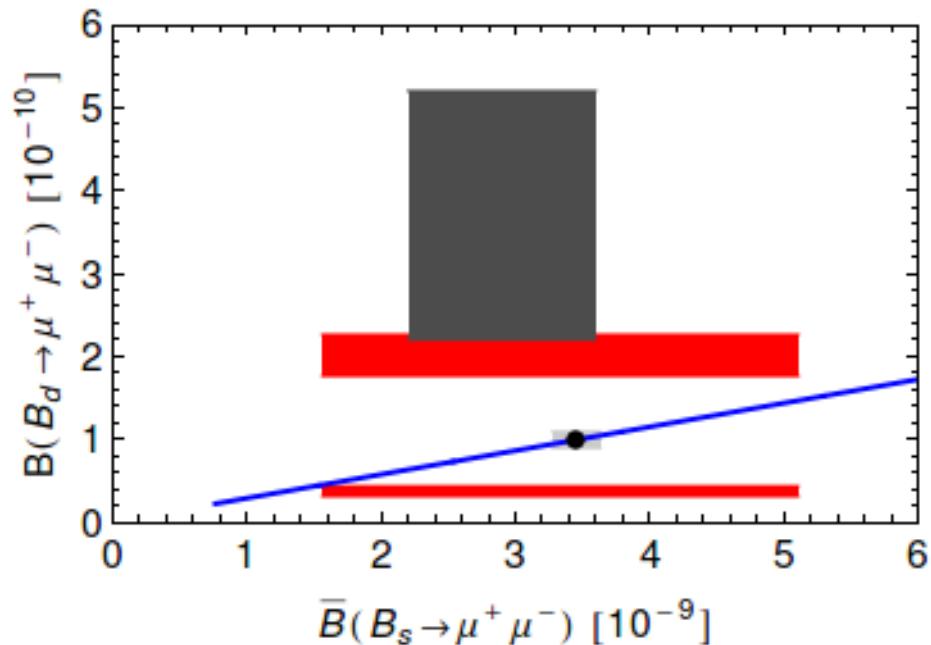
$$\frac{\Delta M_s}{(\Delta M_s)_{SM}} \approx 1.00 \pm 0.01 \quad \frac{\Delta M_d}{(\Delta M_d)_{SM}} \approx 0.96 \pm 0.01$$
$$S_{\psi\varphi} \approx (S_{\psi\varphi})_{SM} \quad \text{Note: } \frac{\Delta_A^{\mu\bar{\mu}}(Z)}{M_Z} = \frac{4.0}{1\text{TeV}} \quad \underline{\text{fixed}}$$

# Violation of CMFV (Z')

High  $V_{ub}$



Low  $V_{ub}$



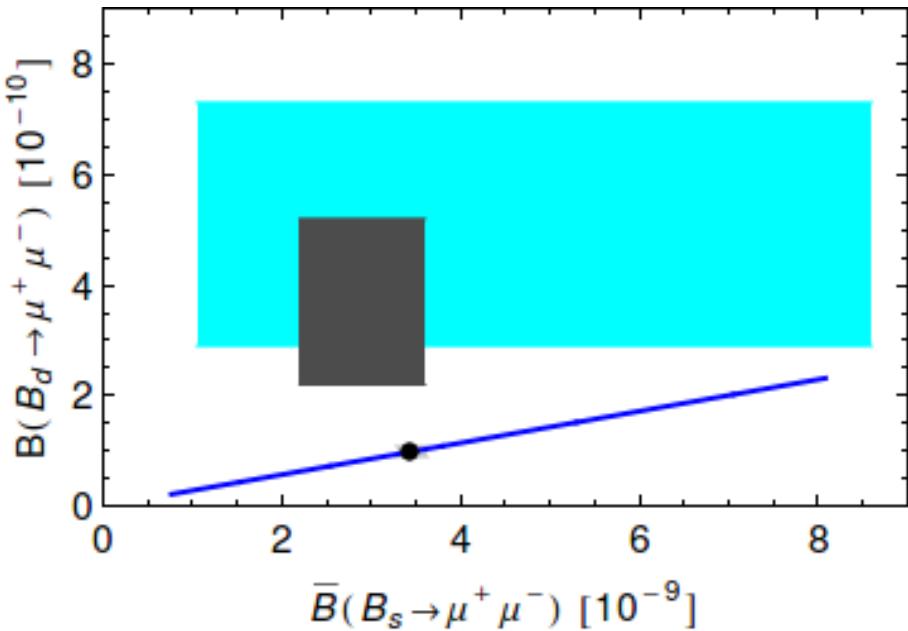
CMS + LHCb



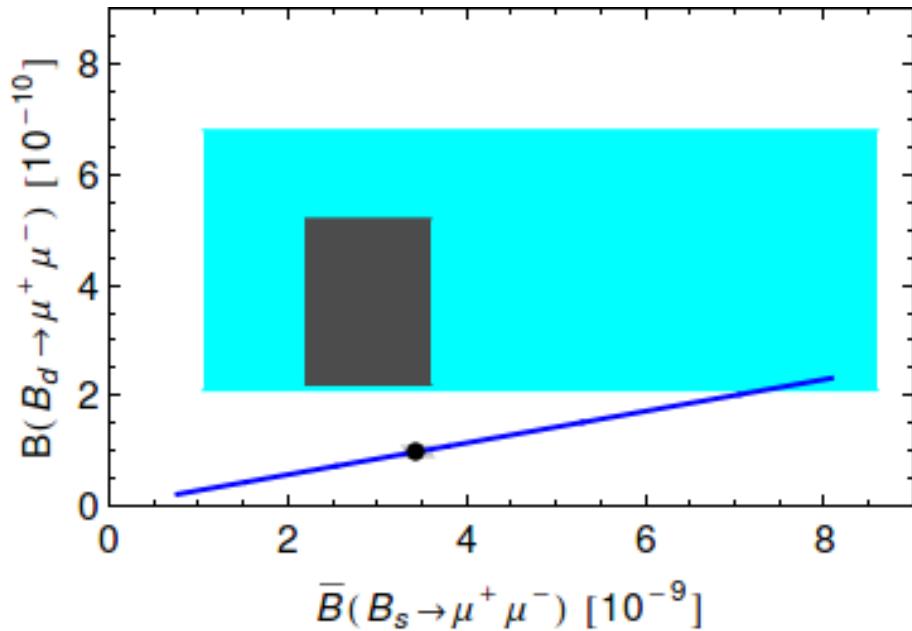
SM

# Violation of CMFV (Z)

High  $V_{ub}$



Low  $V_{ub}$



CMS + LHCb



SM

# Anomalies in $B_d \rightarrow K^* \mu^+ \mu^-$

(24 angular observables. Good agreement with SM but three deviations)

## LHCb

$$\langle F_L \rangle_{[1.6]} = 0.66 \pm 0.07$$

$$\langle S_5 \rangle_{[1.6]} = 0.10 \pm 0.10$$

$$\langle S_4 \rangle_{[14,16]} = -0.07 \pm 0.11$$

## SM

(Altmannshofer + Straub)

$$0.77 \pm 0.04$$

$$-0.14 \pm 0.02$$

$$0.29 \pm 0.07$$

(Not understood  
in any model)

## Extensive Analyses:

Descotes-Genon, Matias, Virto (1307.5683)  
Altmannshofer + Straub (1308.1501)



DMV  
AS

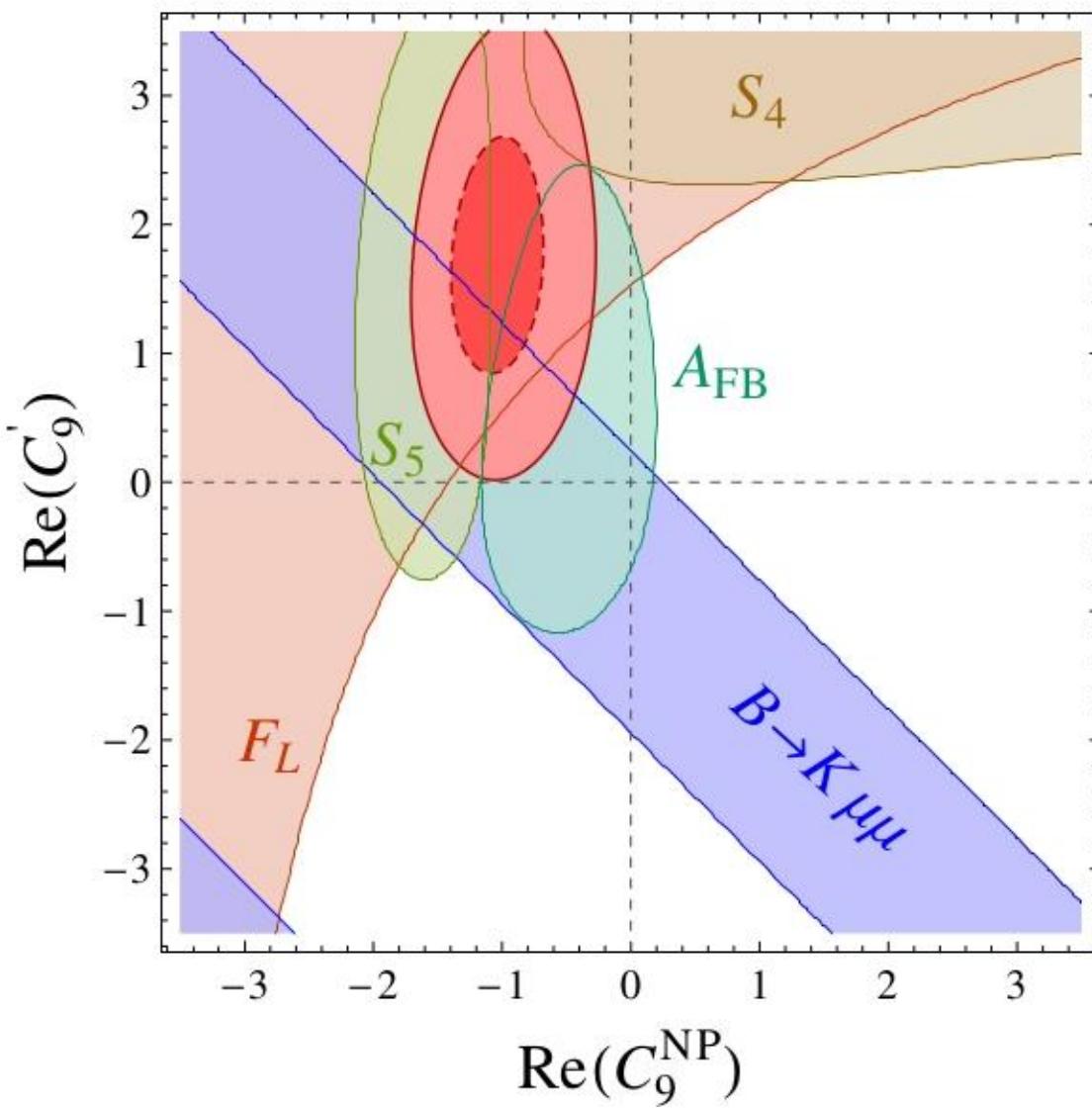
$$C_{7\gamma}^{NP} < 0, C_9^{NP} < 0$$

or

AS

$$C_9^{NP} < 0, C_9' \approx -C_9^{NP}$$

right-handed



**Altmannshofer  
Straub  
(1308.1501)**

# Left-handed Z' and Z FCNC Couplings Facing $B_d \rightarrow K^* \mu^+ \mu^-$ Anomalies

(AJB + Girrbach, 1309.2466)

Z

fails because of small vector coupling to muons  
when  $\Delta M_{s,d}$  constraints taken into account.

Z'

Suggested by Descotes-Genon, Matias, Virto  
(1307.5683)

Softens  $\langle F_L \rangle$ ,  $\langle S_5 \rangle$  anomalies

provided  $C_9^{NP} \approx -1.5$  in a correlated manner

See also  
Altmannshofer  
Straub  
(1308.1501)

Note: In Z' models  $C_{7\gamma}^{NP} = 0$  (1211.1896)



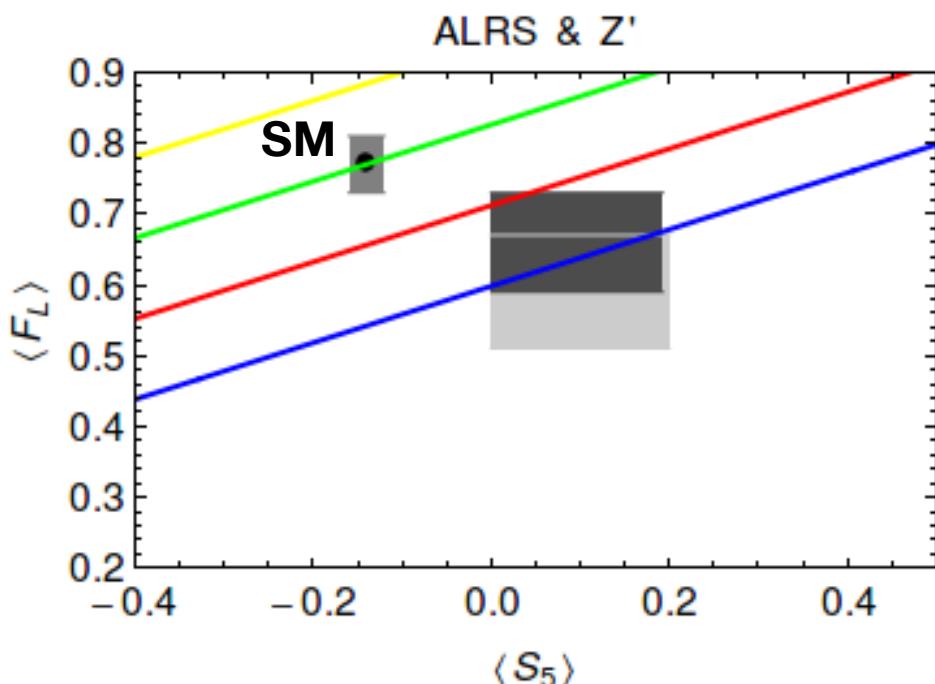
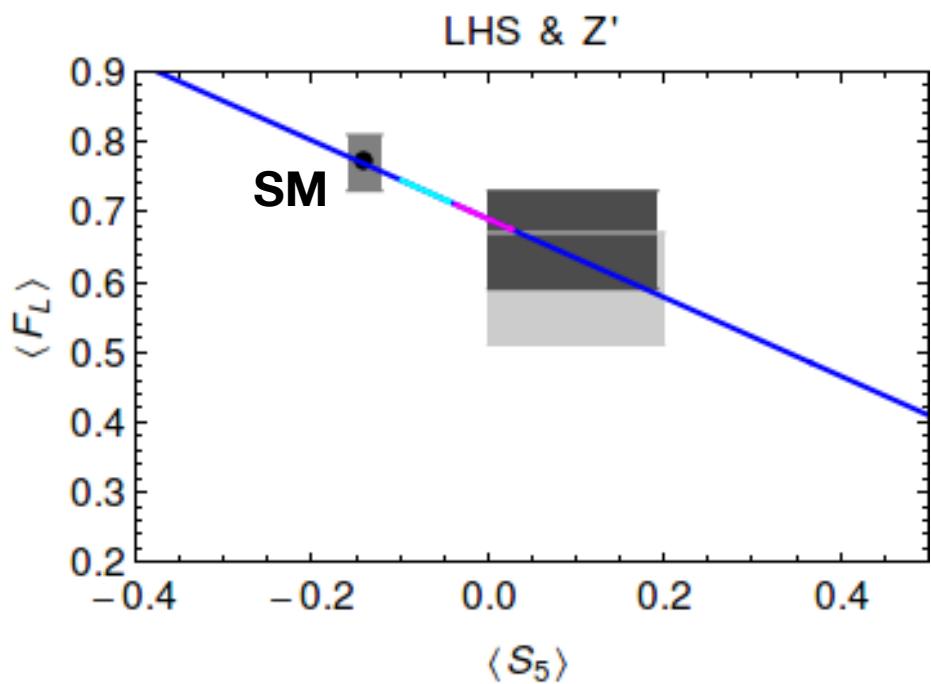
Optimal  
solutions to  $\langle F_L \rangle$ ,  $\langle S_5 \rangle$   
(1309.2466)

Fails for  $\langle S_4 \rangle$   
must be  
SM-like

$C_9^{NP} \neq 0$ ,  $C'_9 = 0$  (LHS)  
 $C_9^{NP} \neq 0$ ,  $C'_9 \approx -C_9^{NP}$  (ALRS)

# New Correlations

(AJB + Girrbach, 1309.2466)



—  $C_9^{\text{NP}} = -(0.8 \pm 0.3)$

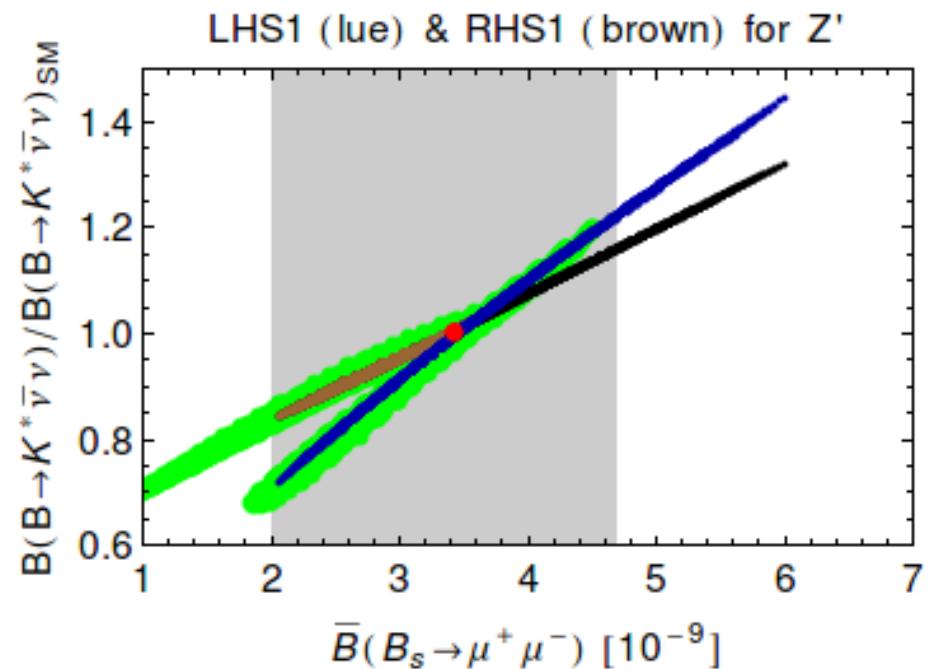
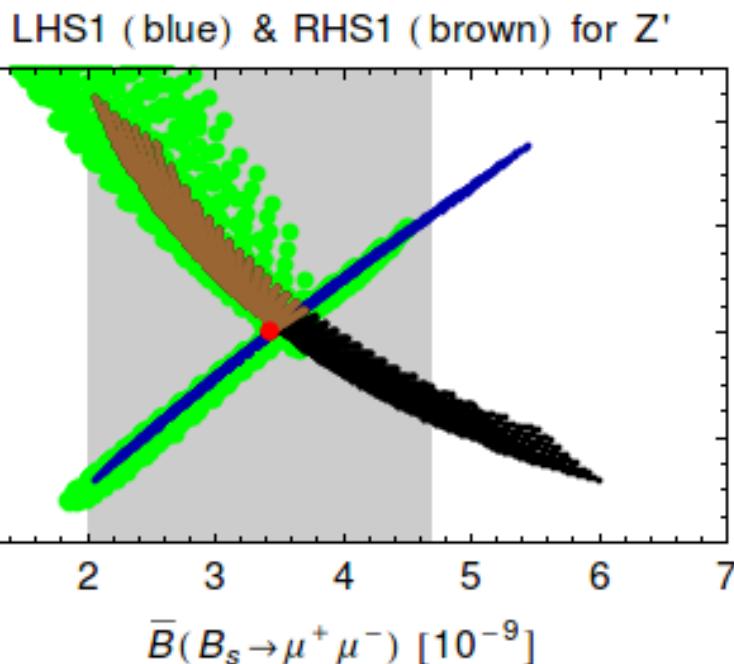
—  $C_9^{\text{NP}} = -(1.6 \pm 0.3)$

—  $C_9^{\text{NP}} = -1.0$

—  $C_9^{\text{NP}} = -2.0$

—  $C_9^{\text{NP}} = 0$

# Distinguishing Left-Handed Currents from Right-Handed Currents



AJB, De Fazio, Girrbach  
1211.1896

Altmannshofer et al.  
0902.0160



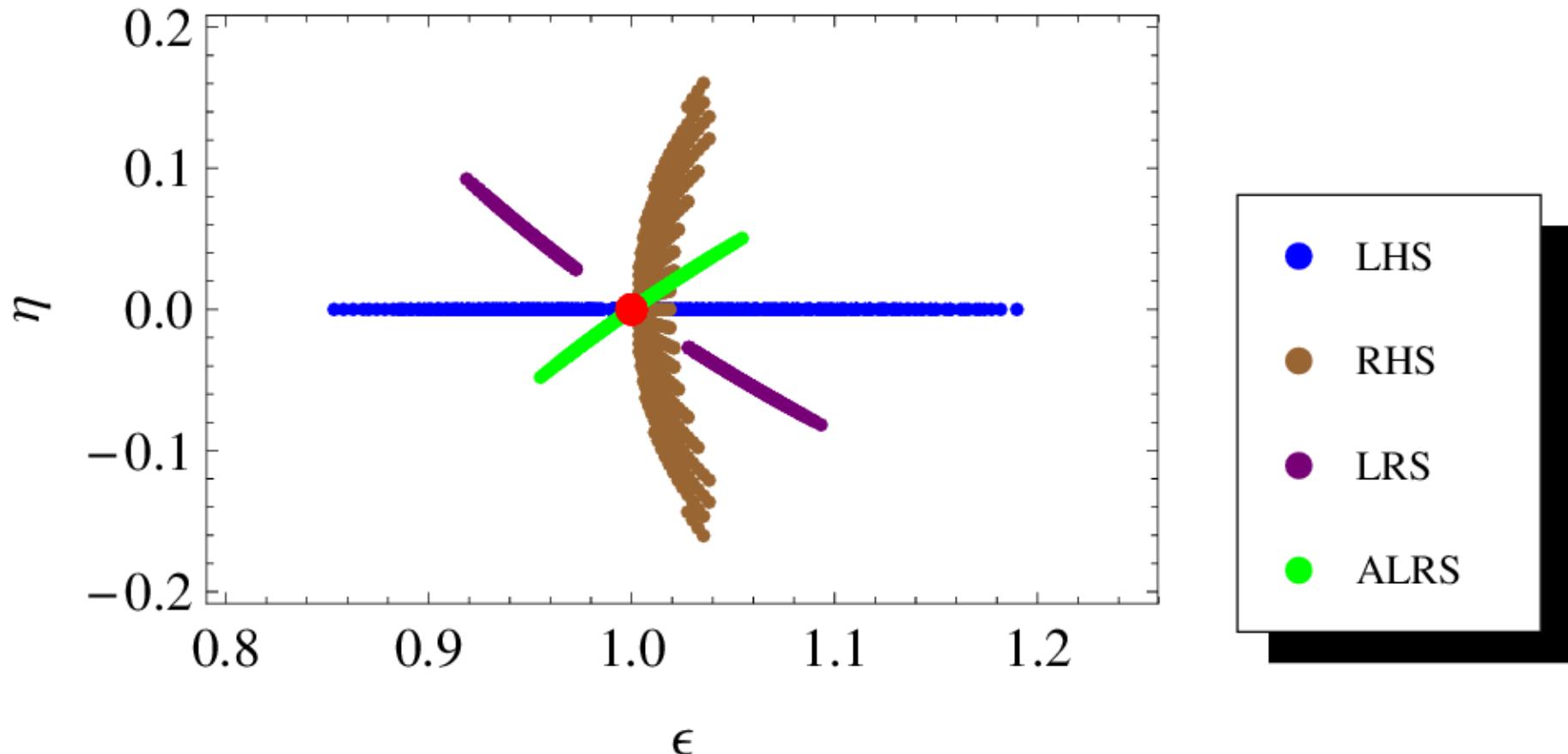
: forbidden by  
 $b \rightarrow sll$



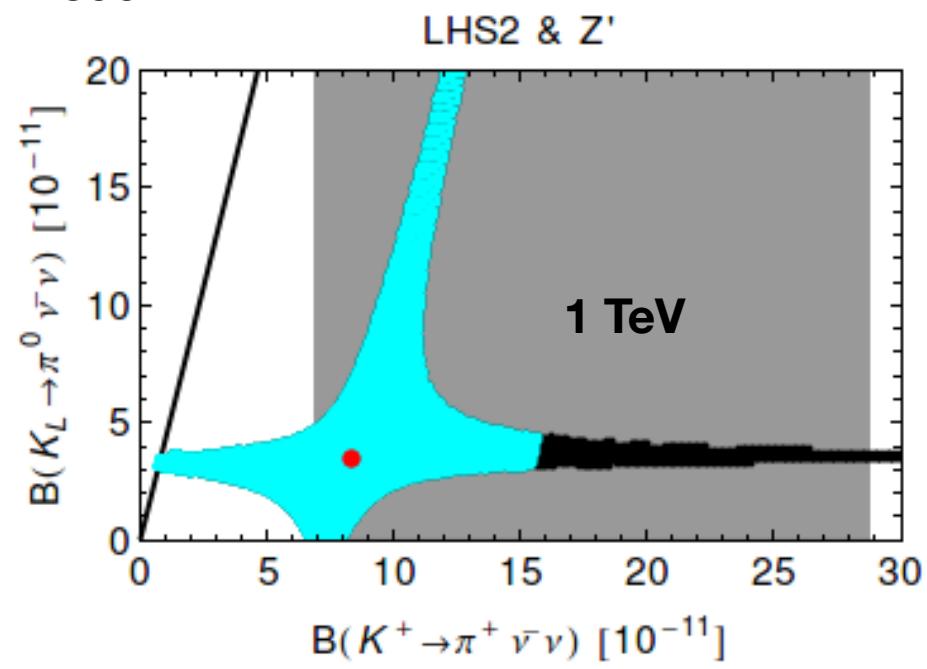
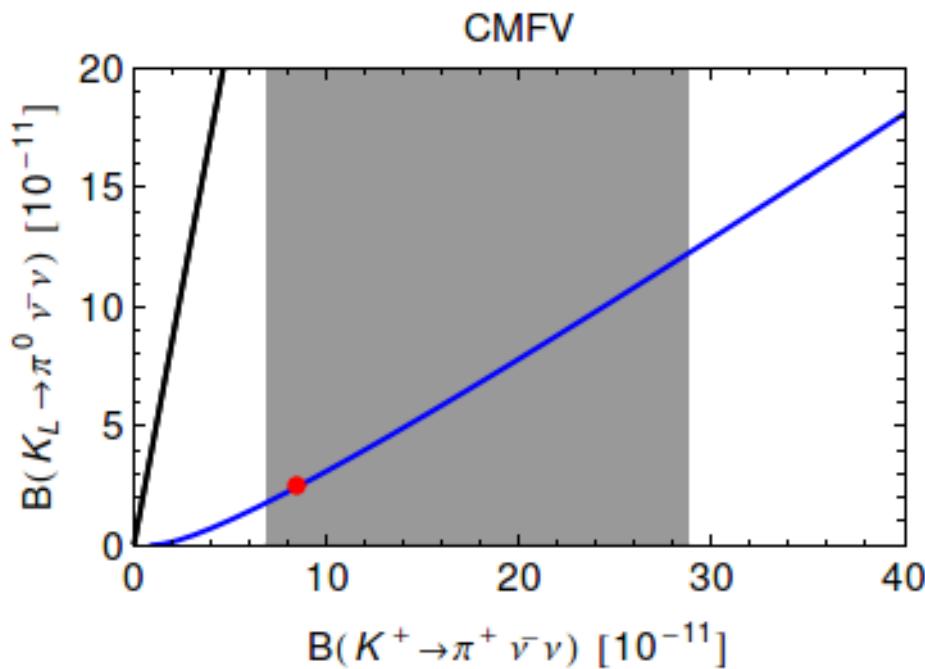
: allowed by  
 $b \rightarrow sll$

# $(\varepsilon, \eta)$ : Parameters for $b \rightarrow s\nu\bar{\nu}$ Transitions

1211.1896

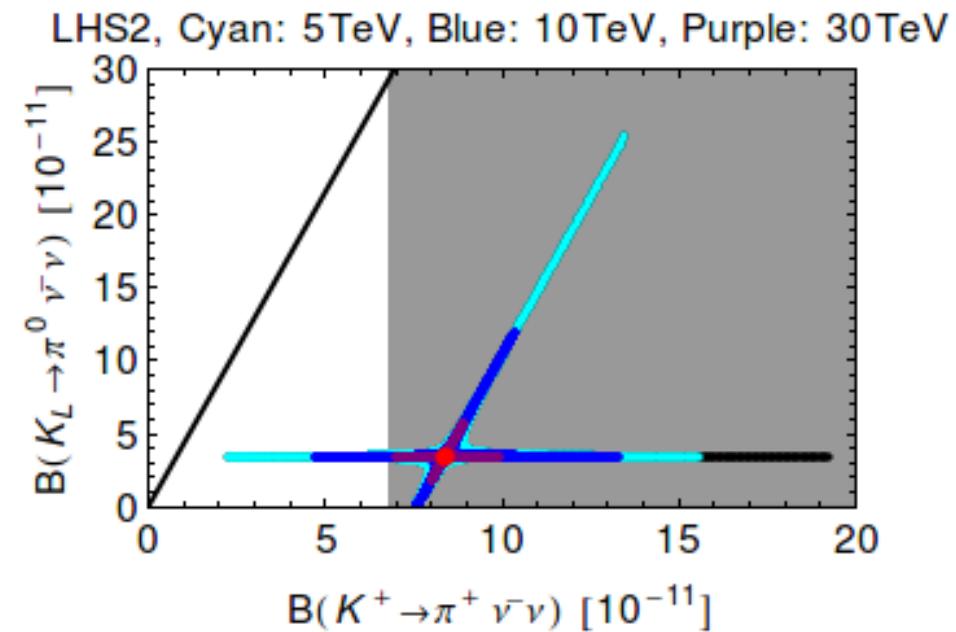


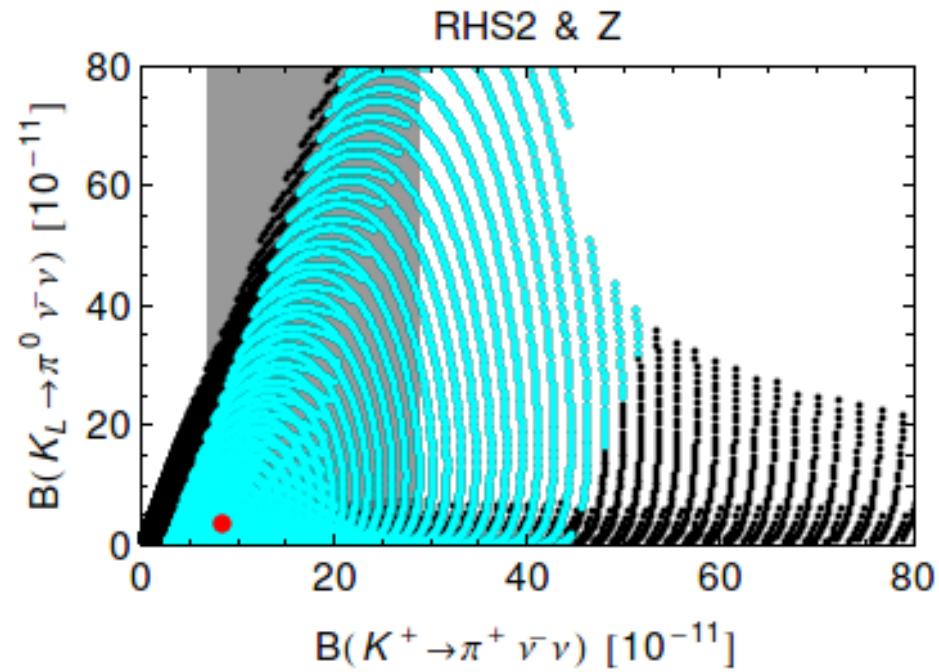
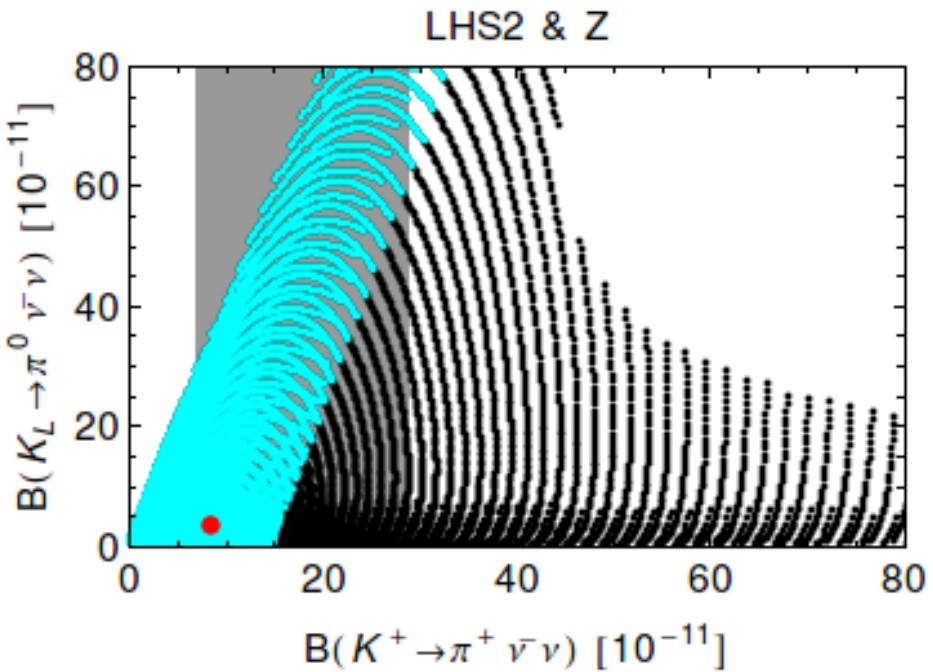
Altmannshofer, AJB, Straub, Wick  
0902.0160



Sensitivity to  
 $M_{Z'}$  beyond  
the LHC

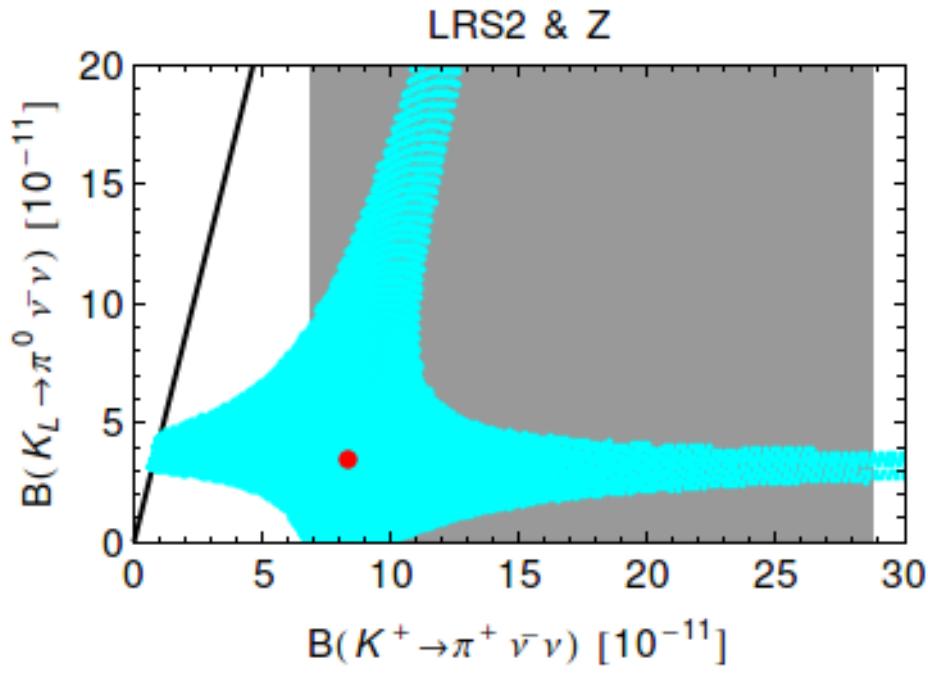
: forbidden by  
 $K_L \rightarrow \mu^+ \mu^-$





■ : forbidden by  
 $K_L \rightarrow \mu^+ \mu^-$

**LHS, RHS  
LRHS**



# DNA - Charts

1306.3755

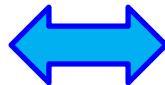
AJB + Girrbach



- suppression relative to SM



- enhancement relative to SM



correlation



anti-correlation

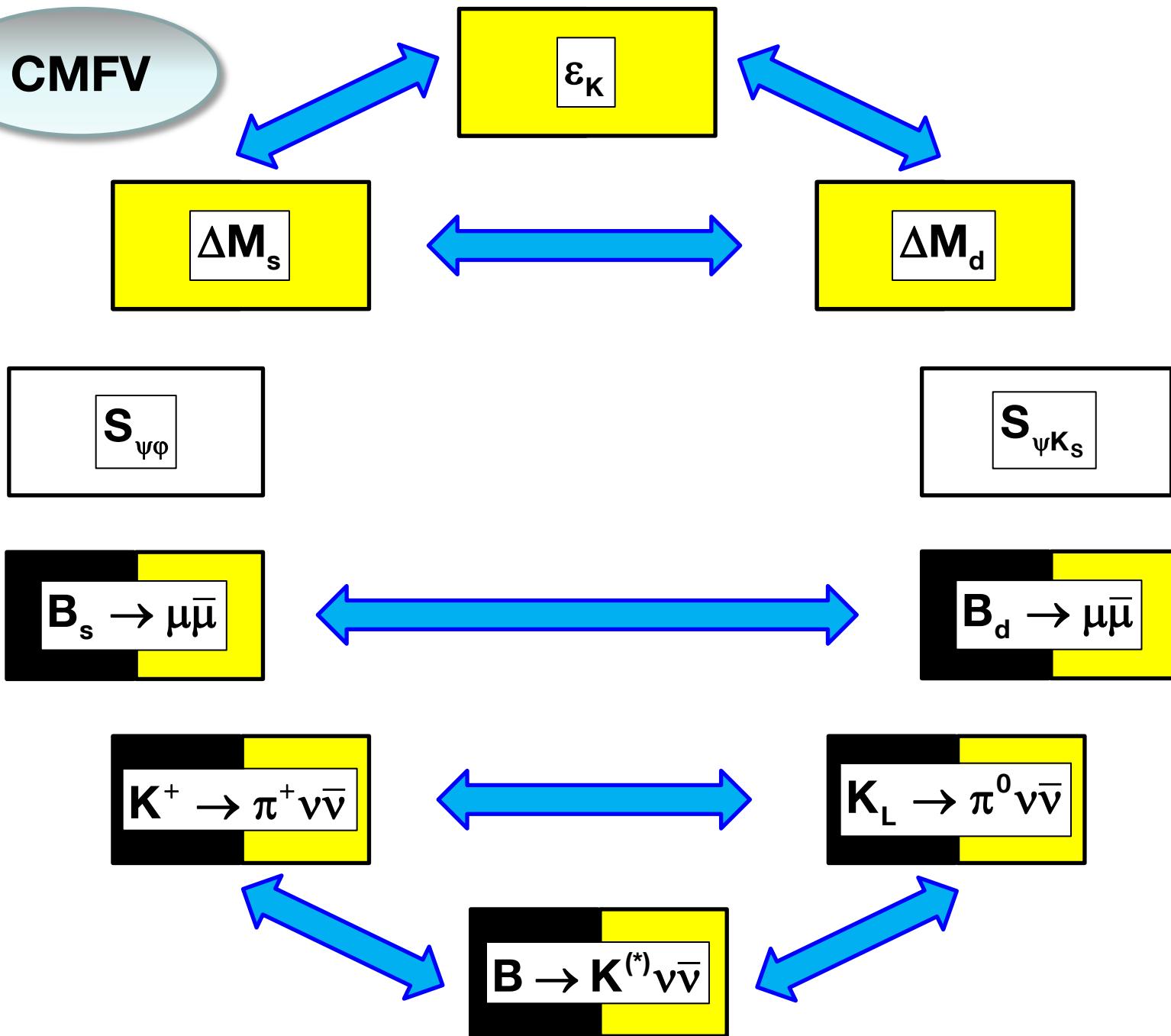
Previous proposals:

DNA tables:

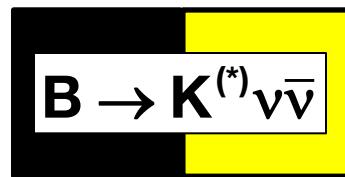
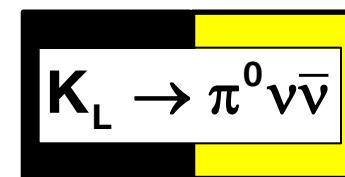
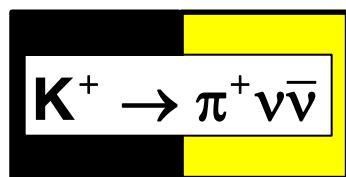
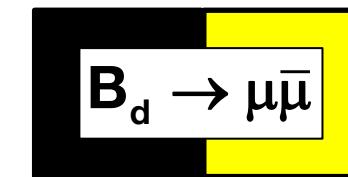
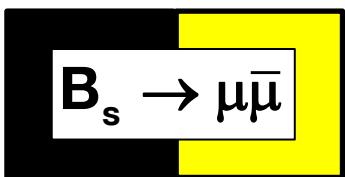
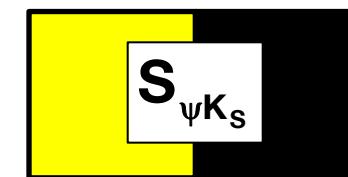
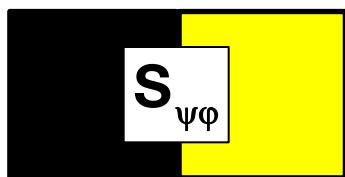
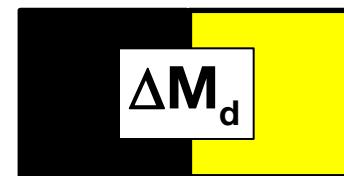
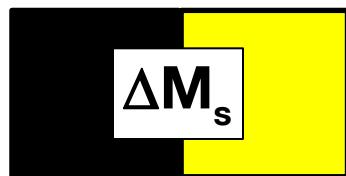
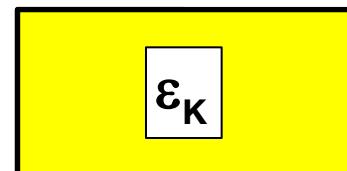
Altmannshofer, AJB, Gori,  
Paradisi, Straub 0909.1333

Flavour codes: AJB 1012.1447

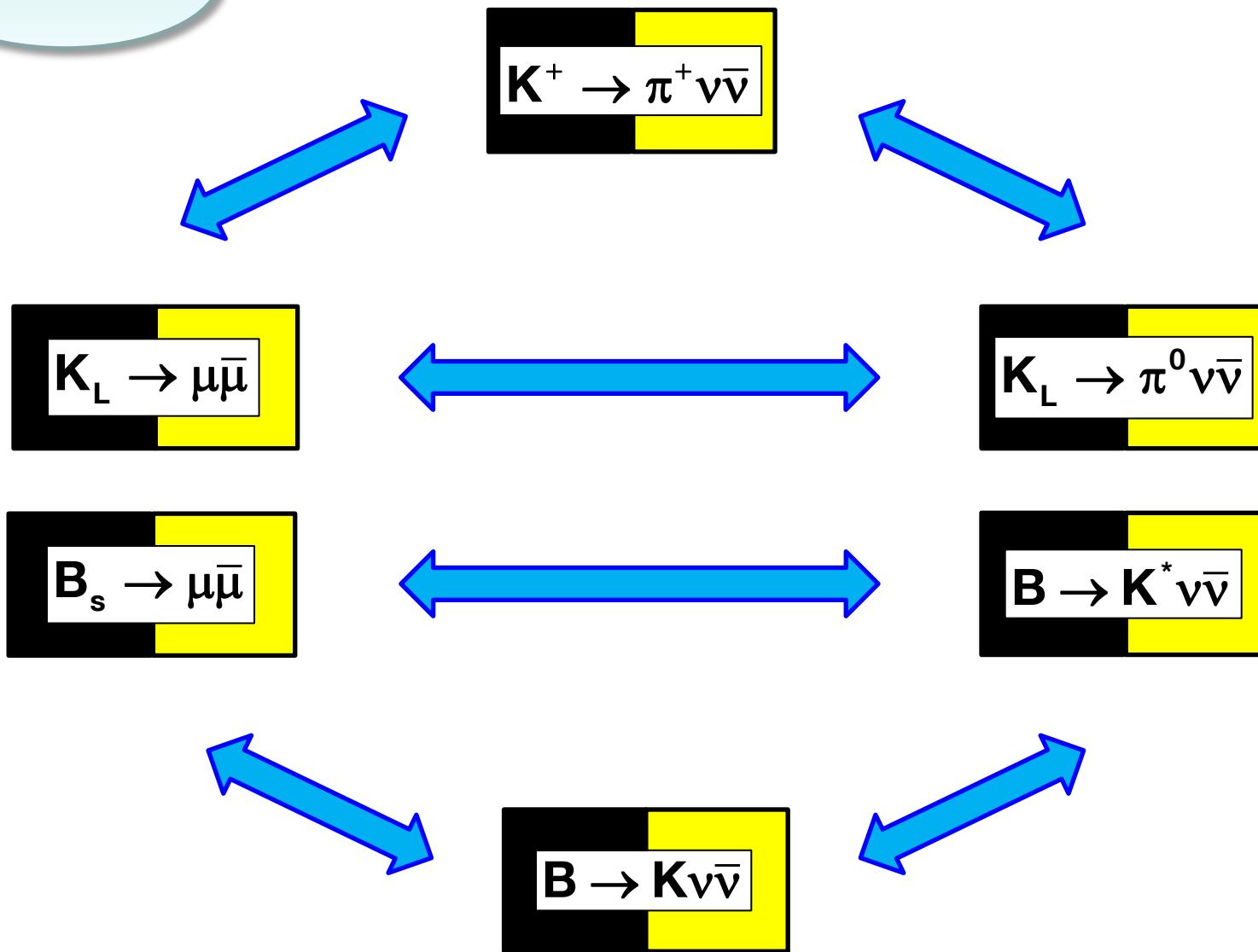
**CMFV**



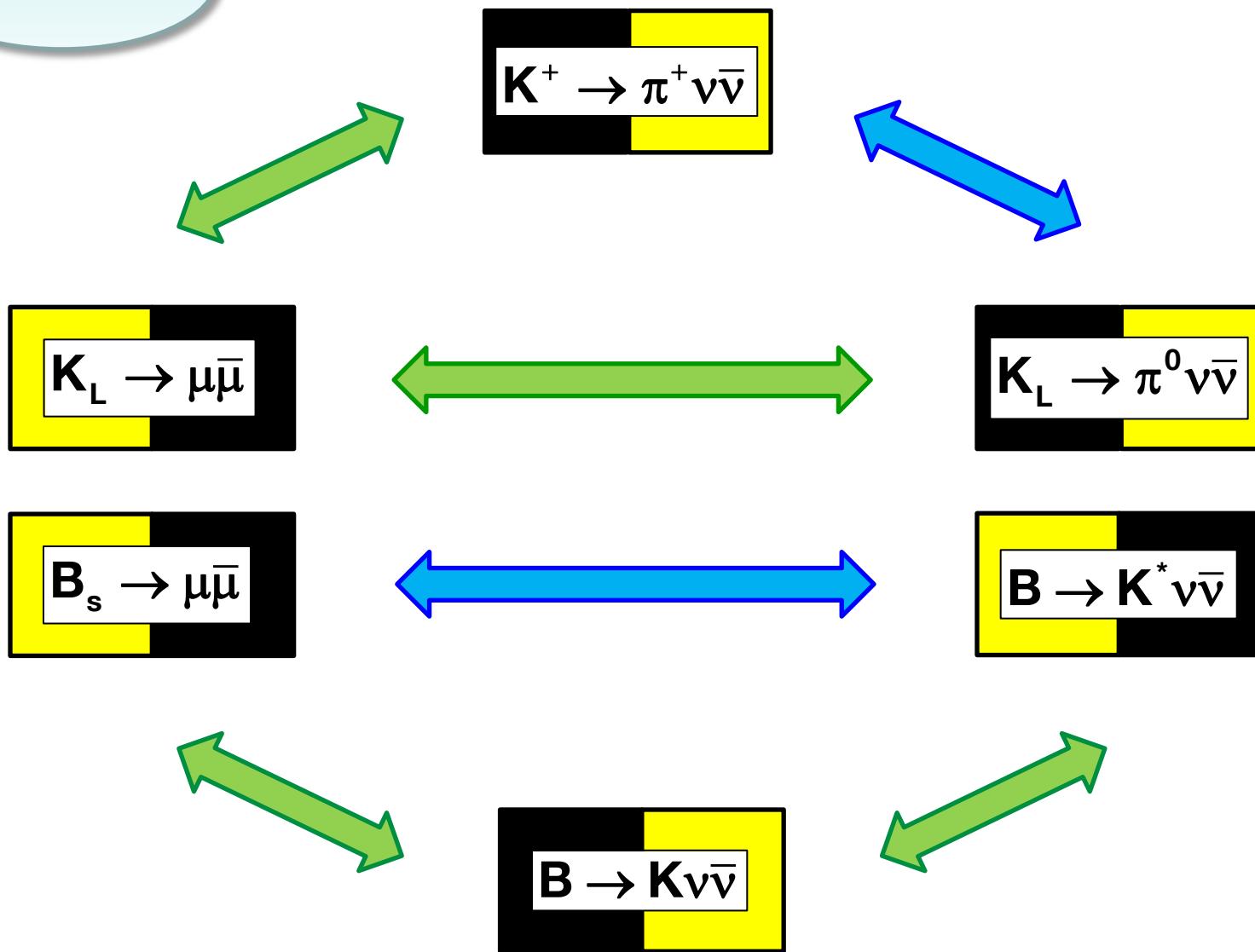
**U (2)<sup>3</sup>**



## Z'/Z LHS



## Z'/Z RHS



# **Finale: Vivace !**

**Exciting Times are just  
ahead of us !!!**

# Towards Zeptouniverse In 12 Steps

$\epsilon'/\epsilon$

$B \rightarrow X_s v\bar{v}$   
 $B \rightarrow K^*(K)v\bar{v}$

$K \rightarrow \pi v\bar{v}$

$B \rightarrow X_s l^+l^-$   
 $B \rightarrow K^*(K)l^+l^-$

$B \rightarrow X_s \gamma$   
 $B \rightarrow K^* \gamma$

$B^+ \rightarrow \tau^+ \nu_\tau$

$\Delta F=2$   
Observables

Lattice

CKM from  
Trees

LFV, EDMs  
 $(g-2)_{\mu,e}$

Charm  
Top

11 12 1

10

9

8

7

6

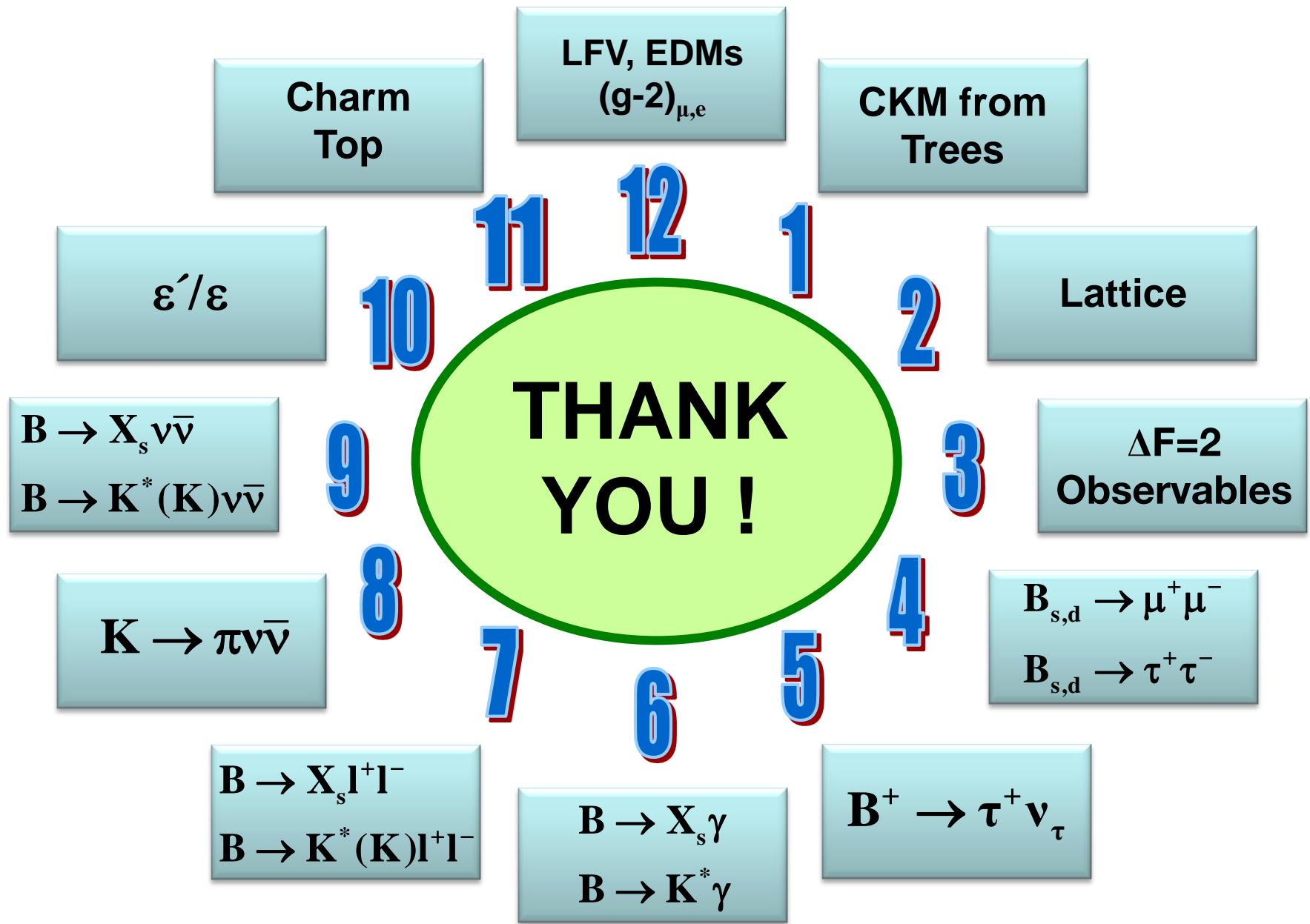
5

4

2

3

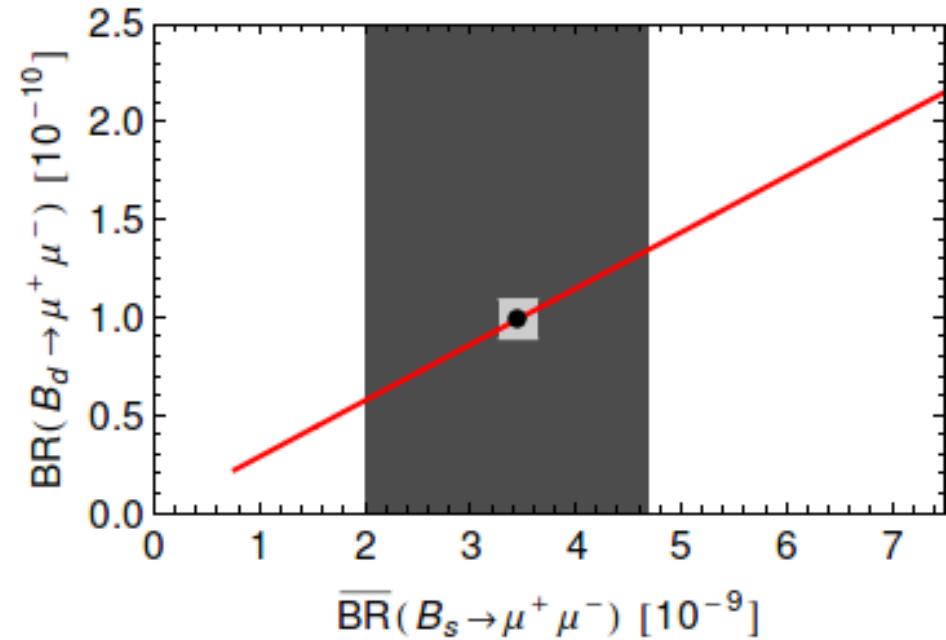
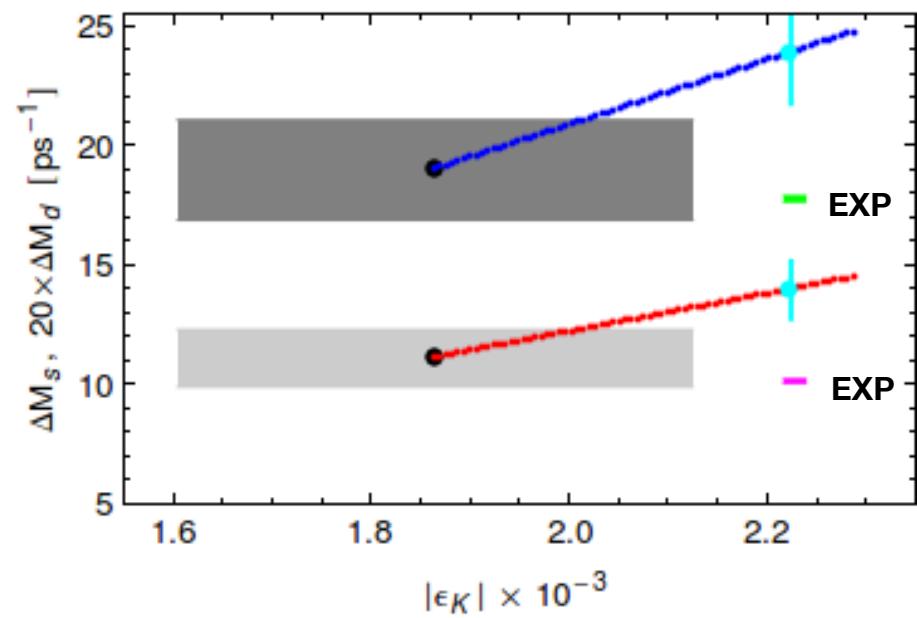
$B_{s,d} \rightarrow \mu^+\mu^-$   
 $B_{s,d} \rightarrow \tau^+\tau^-$



# **Backup**

# Constrained Minimal Flavour Violation

AJB + J. Girrbach (2012)



Tension within CMFV

Similar tension in  
Gauged Flavour Models:  
AJB, Merlo, Stamou (2011)

$$\bar{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = \left( 3.2^{+1.5}_{-1.2} \right) \cdot 10^{-9}$$

(LHCb)

# Departures from Standard Model Expectations

<del>CP</del>	$K^0 - \bar{K}^0$	$(\varepsilon_K)$	$\frac{ \varepsilon_K _{SM}}{ \varepsilon_K _{exp}} \approx 0.80 \pm 0.10$	(AJB, Guadagnoli) (Brod, Gorbahn)
	$B_d^0 - \bar{B}_d^0$	$(S_{\psi K_s})$	$(S_{\psi K_s}) \approx 0.82 \pm 0.04$ (SM) (Lunghi,Soni) $0.678 \pm 0.022$ (exp)	
	$B_s^0 - \bar{B}_s^0$	$(S_{\psi\phi})$	$S_{\psi\phi} = 0.035 \pm 0.002$ (SM) $-0.01 \pm 0.07$ (LHCb)	
	$\frac{\text{Br}(B^+ \rightarrow \tau^+ \nu)_{exp}}{\text{Br}(B^+ \rightarrow \tau^+ \nu)_{SM}} \approx 1.5 \pm 0.3$			
	$ V_{ub}  = \begin{cases} 4.3 \cdot 10^{-3} \\ 3.1 \cdot 10^{-3} \end{cases}$	Inclusive Decays ( $B \rightarrow X_u l \nu$ ) Exclusive Decays ( $B \rightarrow \rho l \nu$ ) and SM-CKM fit		(Right-handed currents? Crivellin; Mannel et al. AJB, Gemmeler, Isidori)

## Two Scenarios for $|V_{ub}|$

(Taking into account  $\Delta M_s, \Delta M_d \leftarrow B_{d,s}^0 - \bar{B}_{d,s}^0$  Mixing)

$$\{|V_{ub}| \approx 4.3 \cdot 10^{-3}\} \Rightarrow \left\{ \frac{(S_{\psi K_s})_{SM}}{(S_{\psi K_s})_{exp}} \right\} \approx 1.2$$

$$\frac{|\epsilon_K|_{SM}}{|\epsilon_K|_{exp}} \approx 1.0$$

New Physics  
in  $B_d^0 - \bar{B}_d^0$   
required

$$\{|V_{ub}| \approx 3.1 \cdot 10^{-3}\} \Rightarrow \left\{ \frac{(S_{\psi K_s})_{SM}}{(S_{\psi K_s})_{exp}} \right\} \approx 1.0$$

$$\frac{|\epsilon_K|_{SM}}{|\epsilon_K|_{exp}} \approx 0.8$$

New Physics  
in  $\epsilon_K$  required



Unfortunately to resolve this issue we have to wait for Belle II, Super-B and smarter Theorists

The size of CP Violation depends on the size of CKM elements:  
here  $|V_{ub}|$

# Important Messages on K Physics

1.

Many Models (SUSY, 4G, LHT, RS)  
can still accommodate

$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \sim 2 \text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}}$$

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \sim 3 \text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}}$$

2.

Even if no significant New Physics  
would be seen in B-decays  
large effects in  $K \rightarrow \pi \nu \bar{\nu}$  are possible.

3.

LHCb opened the road for large effects  
in LHT, RSc.

4.

$\varepsilon'/\varepsilon$  very important provided QCD Penguin  
hadronic matrix under control

# Simple Tests in the Coming Years



## Sign of $S_{\psi\phi}$



$$\frac{\text{Br}(B_d \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)} = \frac{\tau(B_d)}{\tau(B_s)} \frac{m_{B_d}}{m_{B_s}} \frac{F_{B_d}^2}{F_{B_s}^2} \left| \frac{V_{td}}{V_{ts}} \right|^2$$



$$\frac{\text{Br}(B_s \rightarrow \mu^+ \mu^-)}{\text{Br}(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_d}{\hat{B}_s} \frac{\tau(B_s)}{\tau(B_d)} \frac{\Delta M_s}{\Delta M_d}$$



$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}); \quad \text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$$



## Lepton Flavour Violation

$$\mu \rightarrow e\gamma, \quad \mu \rightarrow 3e, \quad \tau \rightarrow 3\mu$$

$$\tau \rightarrow e\gamma, \quad \tau \rightarrow 3e$$

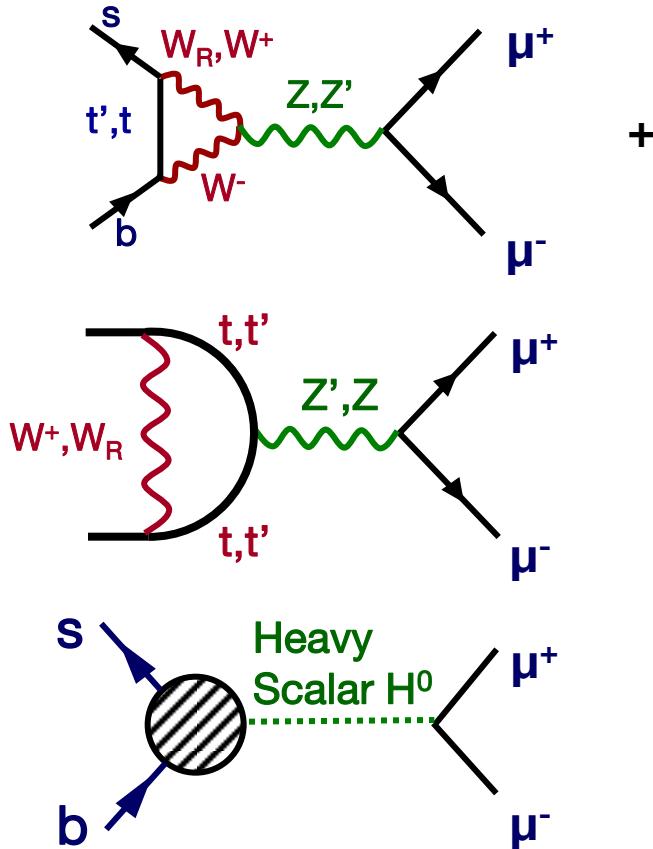
$$\tau \rightarrow \mu\gamma$$



$\varepsilon'/\varepsilon$  provided QCD Penguin hadronic matrix under control

Standard  
Candles  
of  
Flavour  
Physics

# $B_s \rightarrow \mu^+ \mu^-$ Beyond the Standard Model



Other Z-Penguins  
and Boxes

SM:  $(3.2 \pm 0.2) \cdot 10^{-9}$

Model Independent  
Limit (95% C.L.)

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) < 5.6 \cdot 10^{-9}$$

Altmannshofer, Paradisi,  
Straub 1111.1257

$$\frac{(\tan \beta)^6}{M_H^4}$$

in SUSY

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) < 11 \cdot 10^{-9}$$

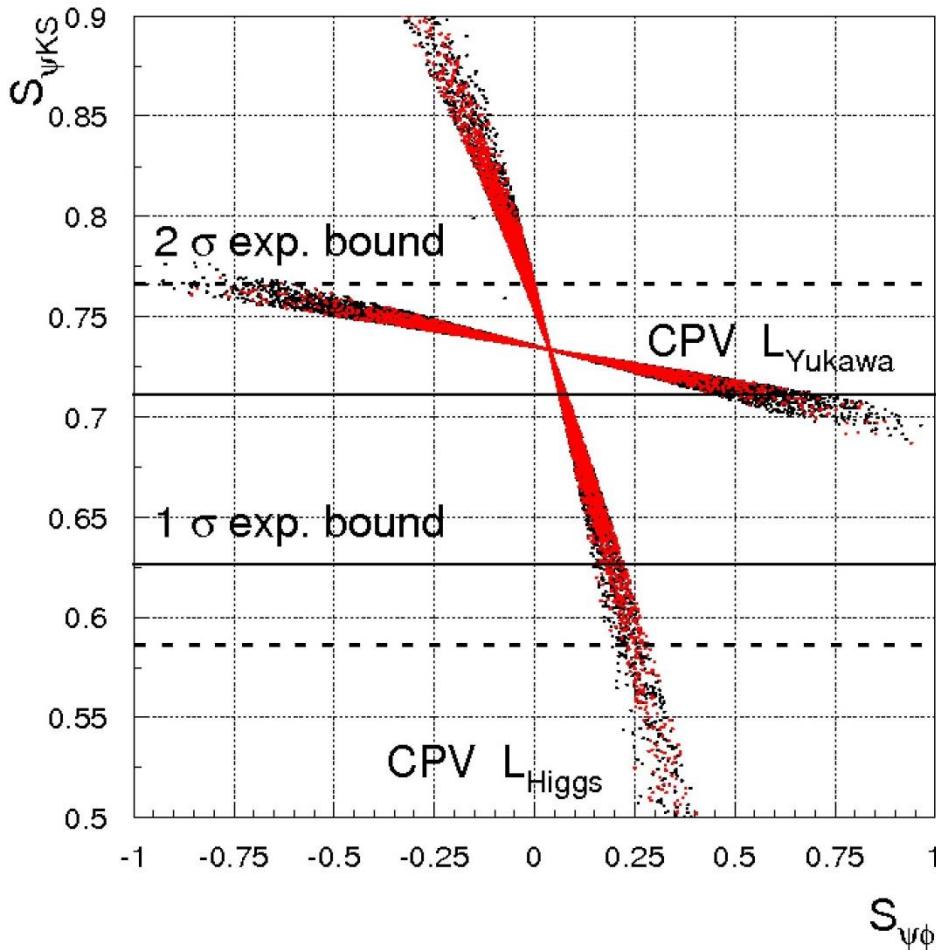
In the case of

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) > 6 \cdot 10^{-9}$$

distinction between  $Z, Z'$  and  $H^0$   
possible

# More on 2HDM with MFV and Flavour Blind Phases

## Correlation between $\mathcal{CP}$ Effects



$$S_{\psi K_s} = \sin(2\beta - \theta_d^H) \quad S_{\psi \phi} \approx \sin(\theta_s^H)$$

$L_{\text{Yukawa}}$ :

$$\frac{\theta_d^H}{\theta_s^H} \approx \frac{m_d}{m_s} \approx \frac{1}{17}$$

BCGI

$L_{\text{Higgs}}$ :  
(potential)

$$\frac{\theta_d^H}{\theta_s^H} = 1$$

After  
LHCb

Kagan, Perez, Volansky, Zupan  
Paradisi, Straub  
Dobrescu, Fox, Martin  
Blum, Hochberg, Nir  
Ligeti, Papucci, Perez, Zupan

AJB, Isidori, Paradisi 1007.5291

# Minimal Effective Model with Right-Handed Currents

AJB, Gemmeler, Isidori (1007.1993)

- Explains the difference  $|V_{ub}|_{\text{excl}} \neq |V_{ub}|_{\text{incl}}$
- Softens  $B^+ \rightarrow \tau^+ \nu_\tau$  problem (large  $V_{ub}$ )

But with large  $S_{\psi\phi}$  predicted: (2010)

Large  $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ , SM-like  $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ , too large  $S_{\psi K_s}$

Impact of small  $S_{\psi\phi}$  from LHCb (2012) (Relief !!)

SM-like  $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ ,  $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ ,  $S_{\psi K_s}$  ok  
can be large

$$K^+ \rightarrow \pi^+ \bar{v} \bar{v} \text{ and } K_L \rightarrow \pi^0 \bar{v} \bar{v} \quad (Z^\circ\text{-penguins})$$

(TH cleanest FCNC decays in Quark Sector)

Extensive TH efforts over 20 years

: Buchalla, AJB; Misiak, Urban (NLO QCD)  
AJB, Gorbahn, Haisch, Nierste (NNLO QCD)  
Brod, Gorbahn, Stamou (QED, EW two loop)  
Isidori, Mescia, Smith (several LD analyses)  
Buchalla, Isidori (LD in  $K_L \rightarrow \pi^0 \bar{v} \bar{v}$ )

$$\frac{\text{Br}(K^+ \rightarrow \pi^+ \bar{v} \bar{v})}{\text{Br}(K_L \rightarrow \pi^0 \bar{v} \bar{v})} = 3.2 \pm 0.2$$

SM	:	$\text{Br}(K^+ \rightarrow \pi^+ \bar{v} \bar{v}) = (8.4 \pm 0.7) \cdot 10^{-11}$	$\text{Br}(K_L \rightarrow \pi^0 \bar{v} \bar{v}) = (2.6 \pm 0.4) \cdot 10^{-11}$
Exp	:	$\text{Br}(K^+ \rightarrow \pi^+ \bar{v} \bar{v}) = \left( 17 \begin{array}{l} +11 \\ -10 \end{array} \right) \cdot 10^{-11}$	$\text{Br}(K_L \rightarrow \pi^0 \bar{v} \bar{v}) \leq 6.8 \cdot 10^{-8}$
		(E787, E949 Brookhaven)	(E391a, KEK)

Future :

NA62  
ORCA (FNAL)

CP-conserving  
TH uncertainty 2-3%

Both very sensitive to New Physics

J-PARC KOTO

CP-Violation in Decay  
TH uncertainty 1-2%





## Littlest Higgs Model with T-Parity

$$\text{SU}(3)_c \otimes [\text{SU}(2) \otimes \text{U}(1)]_1 \otimes [\text{SU}(2) \otimes \text{U}(1)]_2$$

**Non-MFV sources in interactions  
between SM-quarks, Mirror Fermions  
and new Gauge Bosons.**

**Can remove  $\Delta F=2$  tensions and have  $S_{\psi\phi} < 0$**

# LHT after LHCb Data

Our 2006  
Predictions  
(Blanke et al.)

:  $\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)$  within 40% from SM

$$|S_{\psi\phi}| \leq 0.25$$

$\{S_{\psi\phi} > 0.20\} \Rightarrow \begin{cases} \text{No New Physics Effects} \\ \text{in } K^+ \rightarrow \pi^+ v\bar{v}, K_L \rightarrow \pi^0 v\bar{v} \end{cases}$

Concerning  
B-Physics

: LHCb Data = Relief for LHT model

\*)

Concerning  
K-Physics

: LHCb opened the road to large NP effects  
in rare K-decays within LHT model

\*)

\*) The same impact of LHCb on Rare B  
and K decays within RS<sub>c</sub> model

Effects in  
 $B_{s,d} \rightarrow \mu^+ \mu^-$   
even smaller

ABGPS

(0909.1333)

# $\text{Br}(B_d \rightarrow \mu^+ \mu^-) \text{ vs } \text{Br}(B_s \rightarrow \mu^+ \mu^-)$

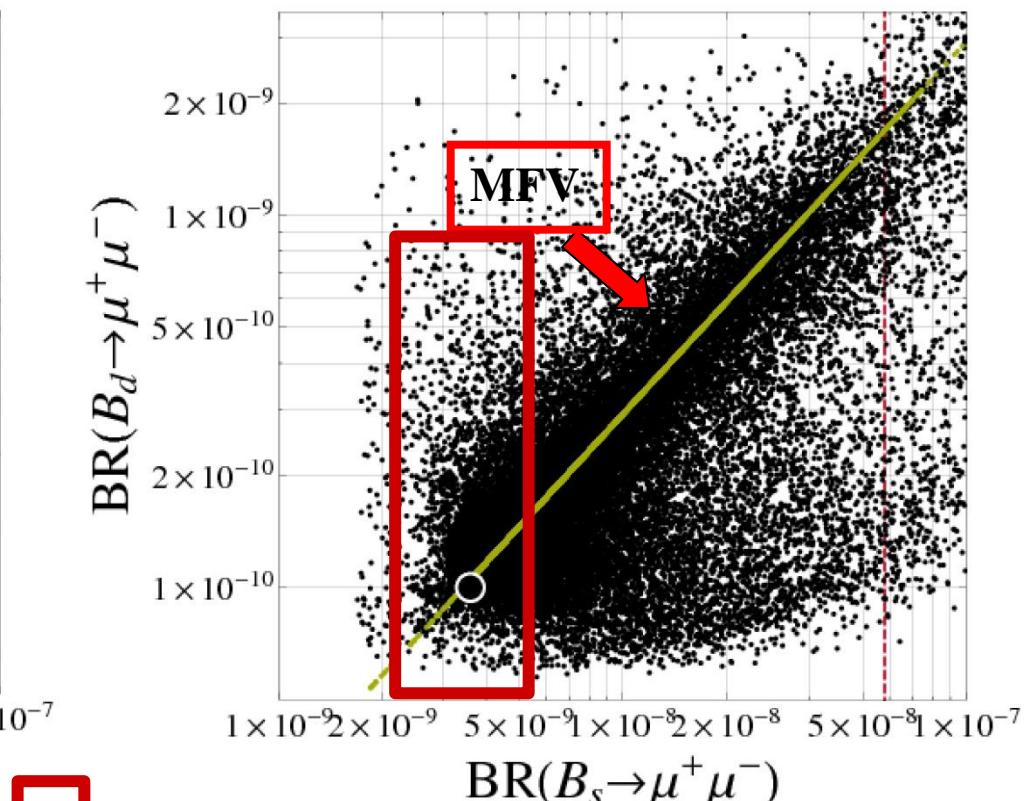
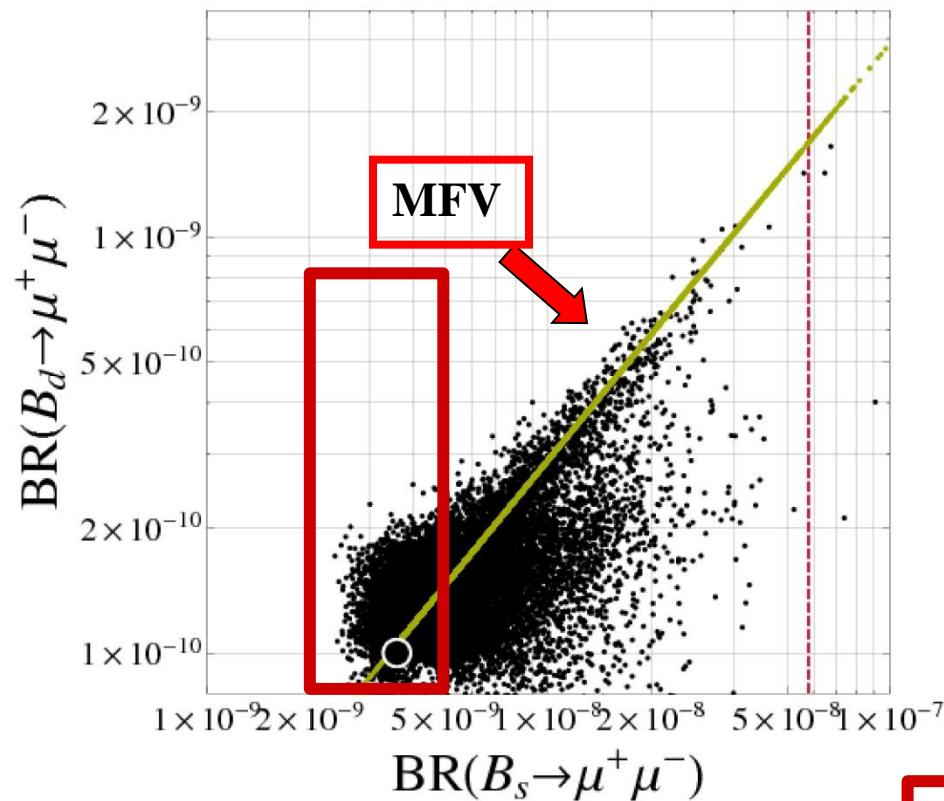
SUSY  
(Flavour)

Altmannshofer, AJB, Gori, Paradisi, Straub

● = SM

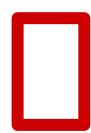
MFV

AJB; Hurth, Isidori, Kamenik, Mescia



RVV2

(RH currents)



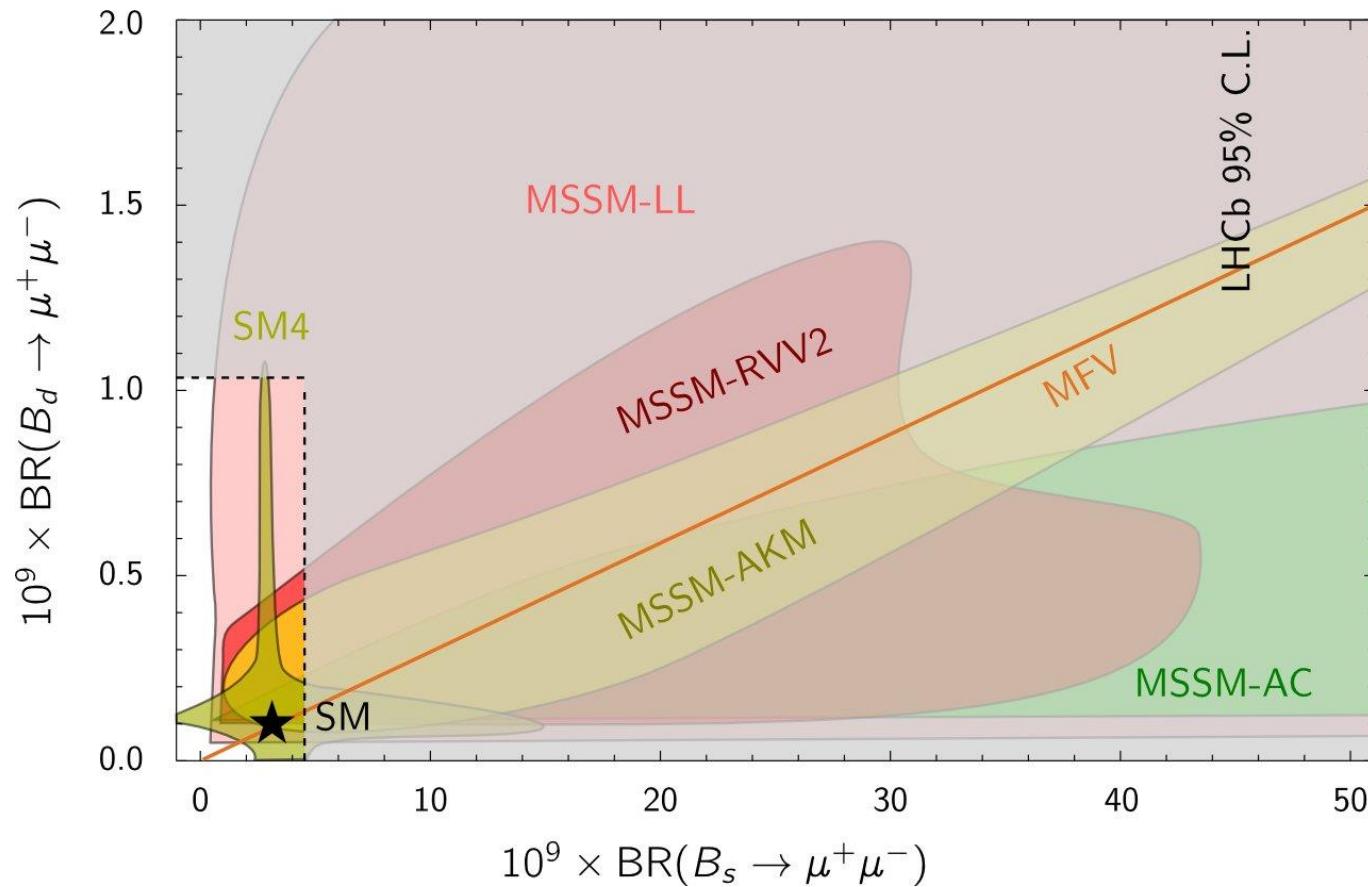
LHCb

LH currents

# Supersymmetric Models Facing LHCb Data

ABGPS

Straub 1012.3893



**Models with new left-handed currents favoured**

Can  $|V_{ub}|_{\text{excl}} \neq |V_{ub}|_{\text{incl}}$  be explained through right-handed currents?

Crivellin; Chen + Nam; Feger, Mannel et al.; AJB, Gemmeler, Isidori

RHMFV

Works better with small  $S_{\psi\varphi}$

$$|V_{ub}|_{\text{excl}} = 3.12 \text{ (26)} \cdot 10^{-3}$$

$$|V_{ub}|_{\text{inc}} = 4.27 \text{ (38)} \cdot 10^{-3}$$

$$\varepsilon \approx \frac{v_L}{v_R}$$

$$|V_{ub}|_{\text{excl}} = |V_{ub}^L + a\varepsilon^2 V_{ub}^R|$$

$$|V_{ub}|_{\text{inc}} \approx |V_{ub}^L|$$

Generally: in principle yes

But a very detailed analysis of  $SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$  with  $g_L \neq g_R$ ;  $V_L \neq V_R$  (mixing) including FCNC constraints + EWP constraints shows that in this concrete model the effect of RH currents too small !!

Blanke  
AJB  
Gemmeler  
Heidsieck  
(1111.5014)

# Comparison of Simplest Models

	$\Delta  \varepsilon_K $	$\Delta M_d$	$\Delta M_s$	$\Delta S_{\psi K_s}$	$\Delta S_{\psi \phi}$	Favoured $ V_{ub} $
<b>CMFV</b>	+	+	+	0	0	<b>exclusive</b>
<b>2HDM<sub>MFV</sub></b>	0	$\pm$	$\pm$	-	+	<b>inclusive</b>
<b>U(2)<sup>3</sup></b>	+	$\pm$	$\pm$	- 0 +	+ 0 -	<b>inclusive</b> <b>exclusive</b>

$$\left( \frac{\Delta M_s}{\Delta M_d} \right)_{CMFV} = \left( \frac{\Delta M_s}{\Delta M_d} \right)_{MU(2)^3} = \left( \frac{\Delta M_s}{\Delta M_d} \right)_{SM}$$

$$S_{\psi K_s} = \sin(2\beta + 2\phi_{new})$$

$$S_{\psi \phi} = \sin(2|\beta_s| - 2\phi_{new})$$

(the same relation for  $B_{s,d} \rightarrow \mu^+ \mu^-$ )

$\beta = F(|V_{ub}|, \gamma)$   
(weak)

# Impose Constraints

Set all input parameters at central values but require:

( $\pm 5\%$ )

$$16.9 \text{ / ps} \leq \Delta M_s \leq 18.7 \text{ / ps}$$

$$0.48 \text{ / ps} \leq \Delta M_d \leq 0.53 \text{ / ps}$$

( $\pm 2\sigma$ )

$$-0.20 \leq S_{\psi\varphi} \leq 0.20$$

$$0.64 \leq S_{\psi K_s} \leq 0.72$$

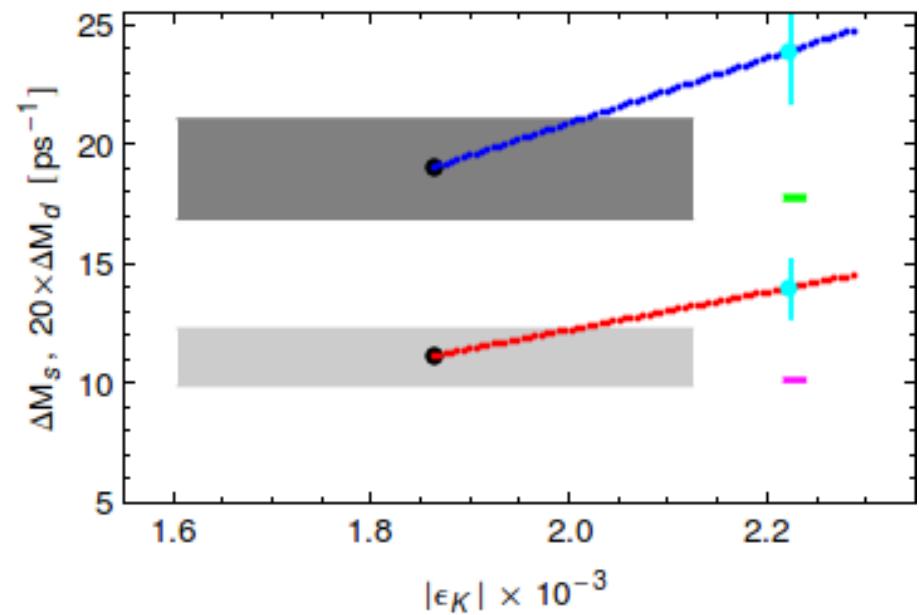
$$0.75 \leq \frac{\Delta M_K}{(\Delta M_K)_{\text{SM}}} \leq 1.25$$

$$2.0 \cdot 10^{-3} \leq \varepsilon_K \leq 2.5 \cdot 10^{-3}$$

# Constrained Minimal Flavour Violation

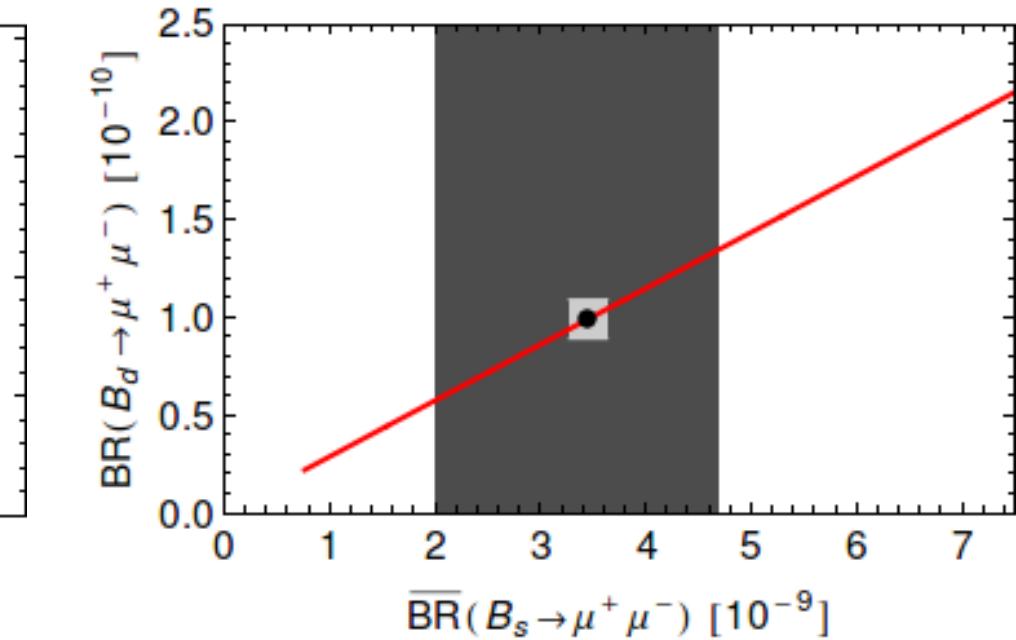
AJB + J. Girrbach (2012)

0007085  
0310208  
0604057



Tension within CMFV

Similar tension in  
Gauged Flavour Models:  
AJB, Merlo, Stamou (2011)



EXP

EXP

$$\bar{Br}(B_s \rightarrow \mu^+ \mu^-) = \left( 3.2^{+1.5}_{-1.2} \right) \cdot 10^{-9}$$

# Stringent Tests of CMFV through $\Delta F=2$ Processes

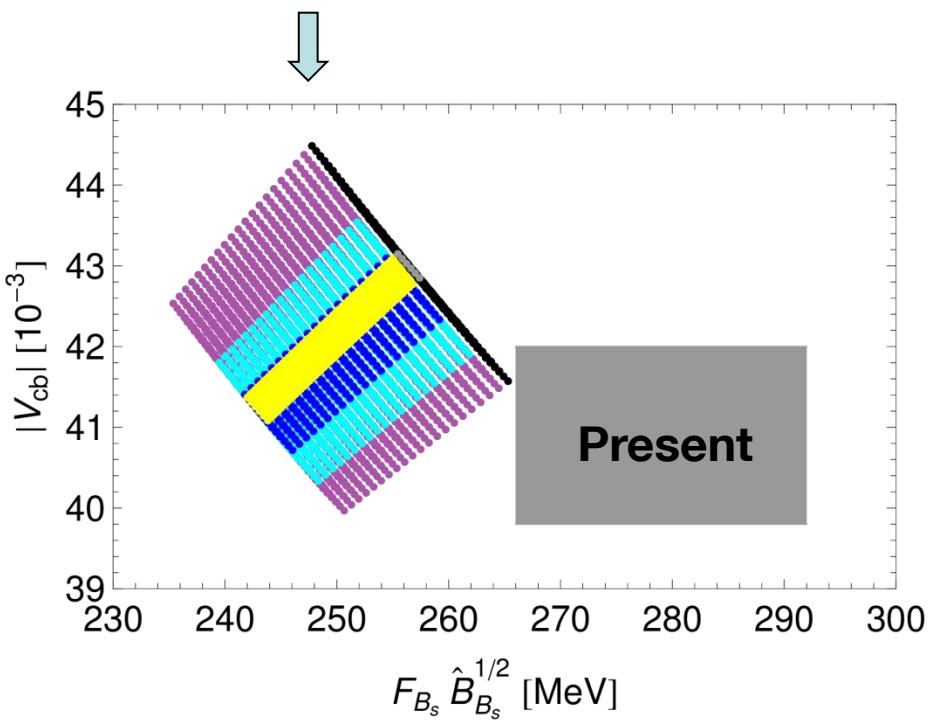
AJB + Girrbach 1304.6835

Which values of

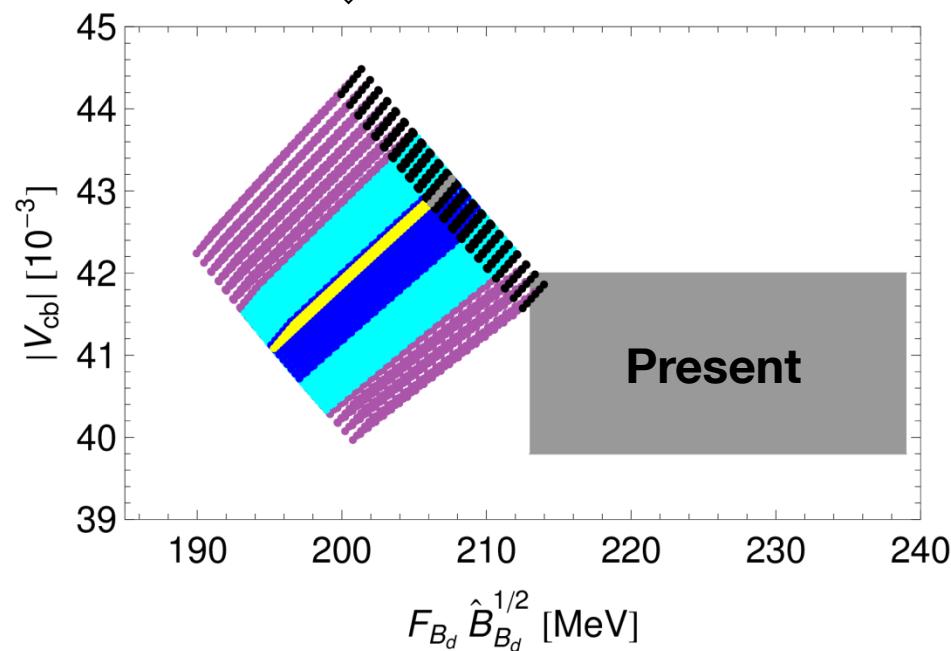
$$|V_{cb}|, \sqrt{\hat{B}_d} F_{B_d}, \sqrt{\hat{B}_s} F_{B_s}$$

Would save CMFV ?

**Required  
by CMFV**



**Required  
by CMFV**



: SM



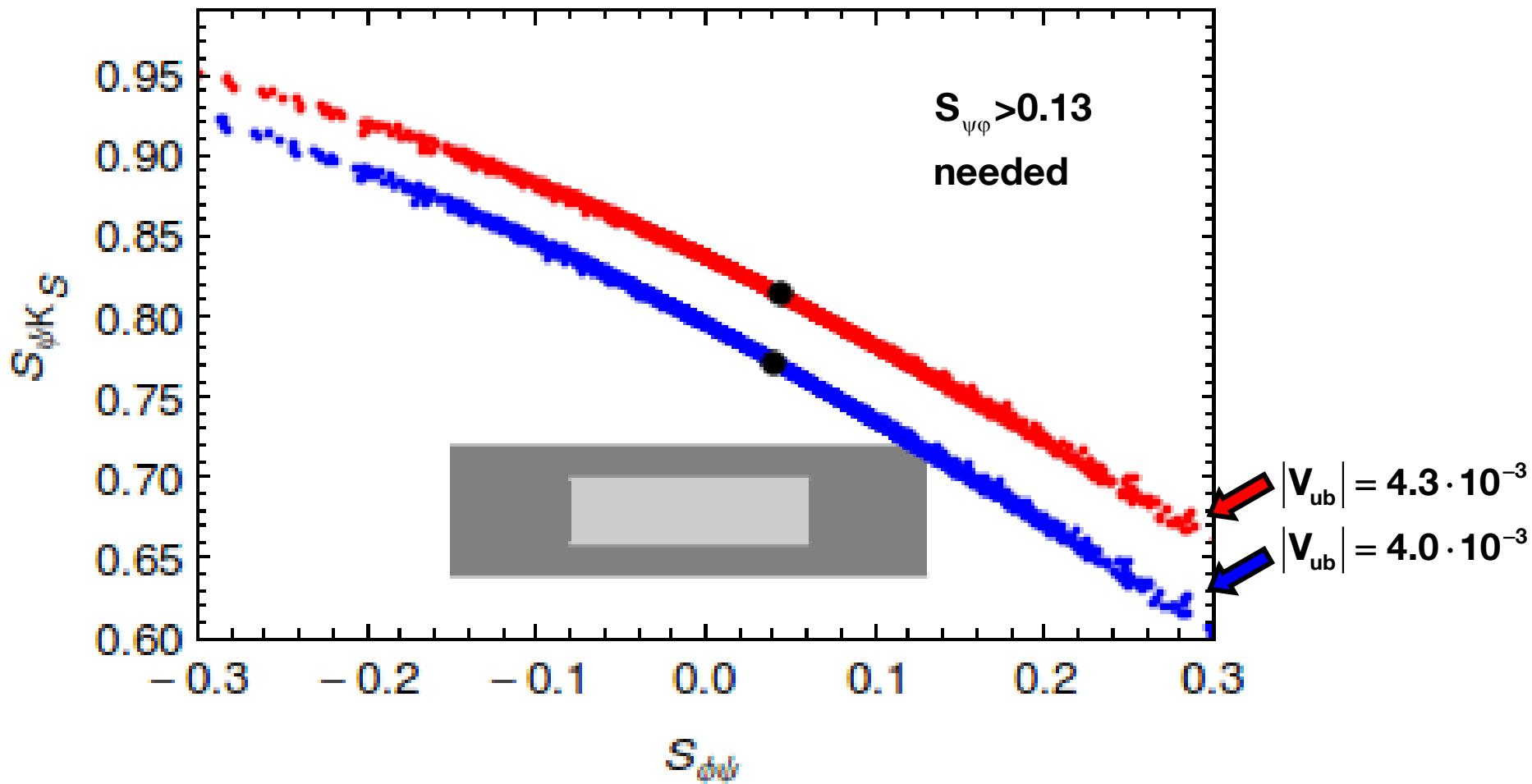
:  $\eta_{cc} = 1.87 \pm 76$  (Brod + Gorbahn)



:  $\eta_{cc} = 1.70 \pm 0.21$  (using  $\Delta M_K$ ) AJB + Girrbach,  
**1304.6835**

# 2HDM <sub>MFV</sub> Facing LHCb Data

AJB, Girrbach, Nagai (2013)



AJB, Carlucci, Gori, Isidori; 1005.5310  
 AJB, Isidori, Paradisi; 1007.5291

## Conclusion on 2HDM<sub>MFV</sub>

**Still alive but finding**

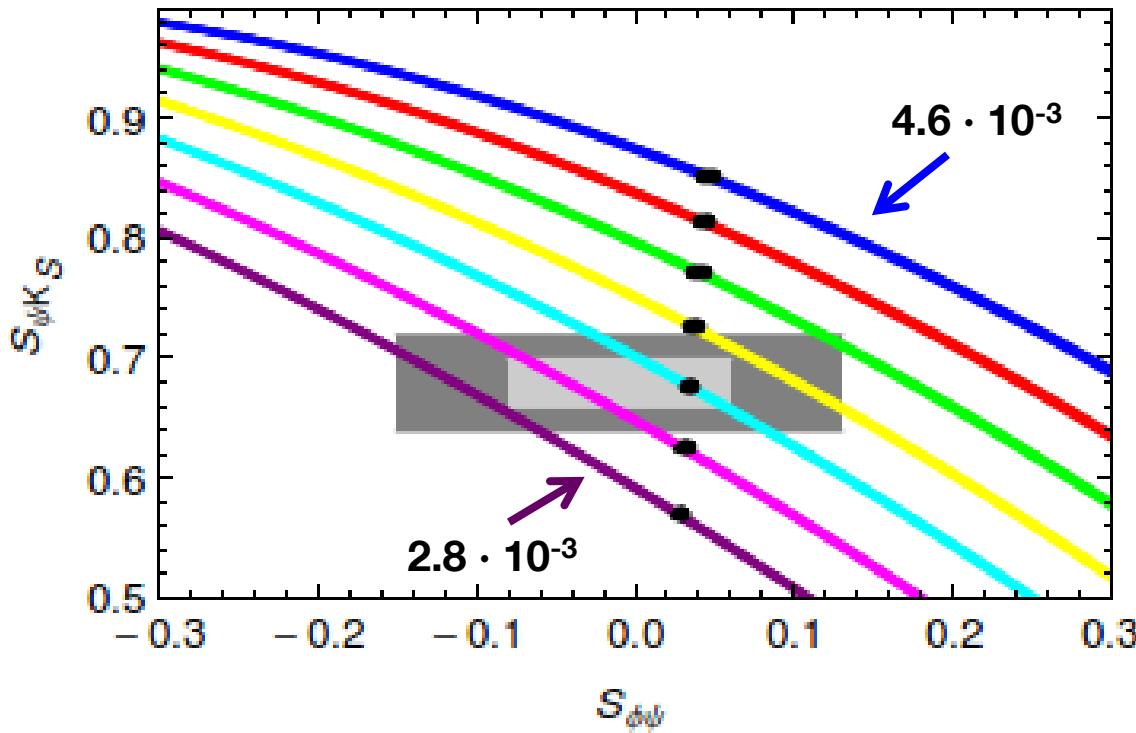
**$S_{\psi\varphi} < 0$  or very close to SM**

**will rule it out.**

**Let us see what  $U(2)^3$  symmetry  
can do for us ? (Barbieri et al.  
Nierste et al.)**

# $S_{\psi K_s} - S_{\psi\phi} - |V_{ub}|$ Correlation in $U(2)^3$

## Important test of $U(2)^3$ Models



$\gamma = 68^\circ$

In the  $U(2)^3$  Symmetric World we could determine  $|V_{ub}|$  without significant hadronic uncertainties (QCD penguins)

$$\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-), S_{\mu\mu}^s, \text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-), S_{\mu\mu}^d$$

**SM**

**Data**

$$\bar{\text{Br}}(\text{B}_s \rightarrow \mu^+ \mu^-) : (3.56 \pm 0.18) \cdot 10^{-9} \quad \left(3.2^{+1.5}_{-1.2}\right) \cdot 10^{-9}$$

$$\text{Br}(\text{B}_d \rightarrow \mu^+ \mu^-) : (1.05 \pm 0.07) \cdot 10^{-10} \quad \leq 9.4 \cdot 10^{-10}$$

$$S_{\mu\mu}^s = S_{\mu\mu}^d = 0$$

De Bruyn, Fleischer, Knegjens et al. (1204.1735; 1204.1737)

AJB, Fleischer, Girrbach, Knegjens (1303.3820)

AJB, Girrbach, Guadagnoli, Isidori (1208.0934)

$$S_{\psi\phi} = 0.035 \pm 0.002$$

$$S_{\psi\phi} = -0.01 \pm 0.07$$

**Still New Physics could be discovered in these observables, in particular through correlations between them.**



# Scenarios for Z' and Z Couplings

**Left-handed scenario (LHS)**  $\Delta_L^{ij} \neq 0$      $\Delta_R^{ij} = 0$

**Right-handed scenario (RHS)**  $\Delta_R^{ij} \neq 0$      $\Delta_L^{ij} = 0$

**Left-right symmetric scenario (LRS)**  $\Delta_L^{ij} = \Delta_R^{ij} \neq 0$

**Left-right asymmetric scenario (ALRS)**  $\Delta_L^{ij} = -\Delta_R^{ij} \neq 0$

**LRS** : no New Physics contributions to  $K_L \rightarrow \mu^+ \mu^-$ ,  $B_{s,d} \rightarrow \mu^+ \mu^-$

**ALRS** : no New Physics contributions to  $K^+ \rightarrow \pi^+ v \bar{v}$ ,  $K_L \rightarrow \pi^0 v \bar{v}$

See also:

Altmannshofer, AJB, Straub, Wick 0902.0160

Altmannshofer, AJB, Gori, Paradisi, Straub (Flavour SUSY) 0909.1333

Altmannshofer, Paradisi, Straub 1111.1257

Altmannshofer, Straub 1206.0273